

Introduction to Monte Carlo event generators

part III

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Outline

Higher order corrections in event generators

- Next-to-leading order matrix elements

- Matrix element corrections

- NLO matching

- Multi-jet merging

MC event generators at work

- LEP: $e^+ + e^- \rightarrow \text{jets}$

- LHC: $Z + \text{jets}$

- LHC: jets

- LHC: other processes

Other tools

Summary

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LEP: $e^+ + e^- \rightarrow \text{jets}$

LHC: $Z + \text{jets}$

LHC: jets

LHC: other processes

Other tools

Summary

Next-to-leading order matrix elements

$$\left. \begin{array}{l} \text{Born term: } \mathcal{B} = \text{Diagram} \\ \text{Virtual terms: } \mathcal{V} = 2 \operatorname{Re} \left\{ \text{Diagram} \right\} \\ \text{Real terms: } \mathcal{R} = \text{Diagram} \end{array} \right\} \text{NLO calculation}$$

- UV divergences in \mathcal{V} removed by renormalization procedure
 - \mathcal{V} and \mathcal{R} both still infrared divergent
 - IR divergences cancel between \mathcal{V} and \mathcal{R} (KLN theorem)
→ finite result for IR safe observables

Real and virtual correction

Real correction: $\mathcal{R} =$  \Rightarrow tree-level, same technologies as for β

Virtual correction: $\mathcal{V} =$

- ▶ reduce 1-loop matrix element to master integrals

$$\mathcal{M}^{1\text{-loop}} = D \begin{array}{c} \text{Diagram A} \\ \text{(square loop)} \end{array} + C \begin{array}{c} \text{Diagram B} \\ \text{(crossed lines)} \end{array} + B \begin{array}{c} \text{Diagram C} \\ \text{(double loop)} \end{array} + A \begin{array}{c} \text{Diagram D} \\ \text{(single loop)} \end{array} + R$$

- ▶ compute coefficients with tensor reduction or unitarity cuts
 - ▶ problem: numerical stability, may need quad-precision

Cancellation of IR divergencies

NLO calculation

$$\langle O \rangle^{\text{NLO}} = \int d\Phi_N \left[\mathcal{B}(\Phi_N) + \mathcal{V}(\Phi_N) \right] O(\Phi_N)$$

$$+ \int d\Phi_{N+1} \mathcal{R}(\Phi_{N+1}) O(\Phi_{N+1})$$

- ▶ IR divergences cancel between \mathcal{V} and \mathcal{R} (KLN theorem), but live in different phase spaces
 - IR divergences in \mathcal{V} arise from integral over loop momentum
 - IR divergences in \mathcal{R} arise from integral over soft-collinear external momentum
 - ▶ **subtraction method:** construct universal integrable terms that reproduce \mathcal{R} in the soft-collinear limit

Subtraction method

Frixione, Kunszt, Signer NPB467(1996); Catani, Seymour NPB485(1997)291; Kosower PRD57(1998)5410

$$\langle O \rangle^{\text{NLO}} = \int d\Phi_N \left[\mathcal{B}(\Phi_N) + \mathcal{V}(\Phi_N) + \mathcal{I}(\Phi_N) \right] O(\Phi_N)$$

$$+ \int d\Phi_{N+1} \left[\mathcal{R}(\Phi_{N+1}) O(\Phi_{N+1}) - \mathcal{D}(\Phi_N \cdot \Phi_1) O(\Phi_N) \right]$$

- subtraction method: construct universal integrable terms \mathcal{D} that reproduce \mathcal{R} in the soft-collinear limit
 - holds for infrared-safe observables, i.e. $O(\Phi_{N+1}) \rightarrow O(\Phi_N)$ in IR limit
 - assume phase space factorisation: $\Phi_{N+1} = \Phi_N \cdot \Phi_1$
 - need to add $\int d\Phi_1 \mathcal{D}(\Phi_N \cdot \Phi_1) = \mathcal{I}(\Phi_N)$ back
→ cancels divergences in \mathcal{V} (KLN)
 - ⇒ integrands of both phase space integrals separately finite

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Subtraction method

- subtraction term for N particle process

$$\mathcal{D}(\Phi_N \cdot \Phi_1) = \mathcal{B}(\Phi_N) \otimes \mathcal{K}^{(S)}(\Phi_1)$$

$$\mathcal{I}(\Phi_N) = \int d\Phi_1 \mathcal{B}(\Phi_N) \otimes \mathcal{K}^{(S)}(\Phi_1)$$

with universal, i.e. process independent, kernel $\mathcal{K}^{(S)}(\Phi_1)$

- ▶ subtraction kernels can be used as splitting kernels in dipole shower
 - ▶ need invertible phase space mapping $\Phi_{N+1} \longleftrightarrow \Phi_N \cdot \Phi_1$

Reminder and notation: the parton shower

- ▶ Sudakov form factor: no-splitting probability for dipole ik

$$\Delta_{ik}^{(\mathcal{K})}(t, t_0) = \exp \left\{ - \int_{t_0}^t \frac{dt}{t} \int dz \frac{d\phi}{2\pi} \frac{\alpha_s}{2\pi} \mathcal{K}_{ik}(t, z, \phi) \right\}$$

- ▶ will replace $\frac{dt}{t} dz \frac{d\phi}{2\pi} \rightarrow d\Phi_1$
- ▶ Sudakov form factor for emission off N particle configuration

$$\Delta_N^{(\mathcal{K})}(t, t_0) = \exp \left\{ - \int_{t_0}^t d\Phi_1 \mathcal{K}_N(\Phi_1) \right\} \text{ with } \mathcal{K}_N(\Phi_1) = \sum_{\{ik\}} \frac{\alpha_s}{2\pi} \mathcal{K}_{ik}(\Phi_1)$$

Reminder and notation: the parton shower

- ▶ consider first parton shower emission off Born configuration

$$d\sigma_{PS}^{(LO)} = d\Phi_N \mathcal{B}(\Phi_N)$$

$$\times \underbrace{\left[\Delta_N^{(K)}(\mu_F^2, t_0) + \int_{t_0}^{\mu_F^2} d\Phi_1 \mathcal{K}_N(\Phi_1) \Delta_N^{(K)}(\mu_F^2, t(\Phi_1)) \right]}_{=1 \quad (\text{unitarity of parton shower})}$$

- ▶ parton shower is unitary
- ▶ further emissions by recursion

Matrix element corrections

Matrix element corrections

- parton shower not a good description for hard emissions
- form many processes $\mathcal{R} < \mathcal{B} \times \mathcal{K}_N$
- procedure: generate emission with parton shower and reject with probability $\mathcal{P} = \mathcal{R}/(\mathcal{B} \times \mathcal{K}_N)$

$$d\sigma_{\text{MEC}}^{(\text{LO})} = d\Phi_N \mathcal{B}(\Phi_N)$$

$$\times \left[\Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_F^2, t_0) + \int_{t_0}^{\mu_F^2} d\Phi_1 \frac{\mathcal{R}(\Phi_N \cdot \Phi_1)}{\mathcal{B}(\Phi_N)} \Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_F^2, t(\Phi_1)) \right]$$

$= 1$

where $\Delta_N^{(\mathcal{R}/\mathcal{B})}(t, t_0) = \exp \left\{ - \int_{t_0}^t d\Phi_1 \frac{\mathcal{R}(\Phi_N \cdot \Phi_1)}{\mathcal{B}(\Phi_N)} \right\}$

Matrix element corrections

Matrix element corrections

- ▶ cross section still LO
- ▶ first emission described by \mathcal{R} (correct at order α_s)
- ▶ but: phase space constrained by μ_F^2
- ▶ “power shower”: replace $\mu_F^2 \rightarrow s$ and apply ME correction
- ▶ problem: generates wrong log
- ▶ extends resummation built into parton shower beyond region of its validity

NLO matching: Basic idea

- ▶ parton shower resums logarithms
 - ▶ fair description of collinear/soft emissions
 - ▶ jet evolution
- where the logs are large
- ▶ matrix elements exact at given order
 - ▶ fair description of hard/large-angle emissions
 - ▶ jet production
- where the logs are small
- ▶ adjust ("match") terms:
 - ▶ cross section at NLO accuracy & correct hardest emission in PS to exactly reproduce ME at order α_s (\mathcal{R} -part of the NLO calculation)
 - ▶ maintain (N)LL-accuracy of parton shower

review: Nason, Webber, Ann. Rev. Nucl. Part. Sci. 62 (2012) 187

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POWHEG

Nason, JHEP 0411 (2004) 040; Frixione, Nason, Oleari, JHEP 0711 (2007) 070

- ▶ promote ME correction to NLO accuracy by defining Born configuration with NLO weight local K-factor

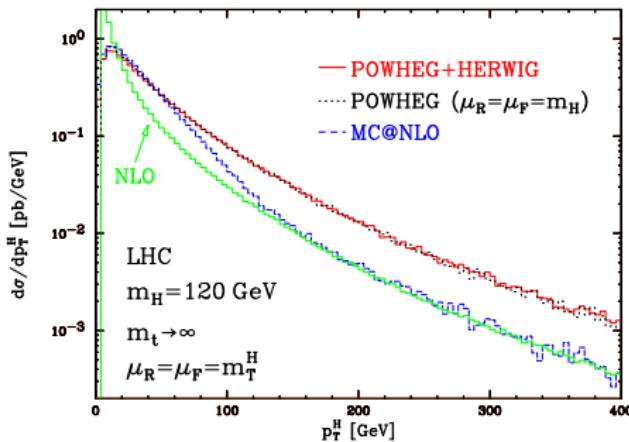
$$\bar{\mathcal{B}}(\Phi_N) = \mathcal{B}(\Phi_N) + \mathcal{V}(\Phi_N) + \mathcal{I}(\Phi_N) \\ + \int d\Phi_1 [\mathcal{R}(\Phi_N \cdot \Phi_1) - \mathcal{D}(\Phi_N \cdot \Phi_1)]$$

- ▶ integrates to NLO cross section
- ▶ radiation pattern like in ME correction

$$d\sigma_{\text{POWHEG}}^{(\text{NLO})} = d\Phi_N \bar{\mathcal{B}}(\Phi_N) \\ \times \left[\Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_F^2, t_0) + \int_{t_0}^{\mu_F^2} d\Phi_1 \frac{\mathcal{R}(\Phi_N \cdot \Phi_1)}{\mathcal{B}(\Phi_N)} \Delta_N^{(\mathcal{R}/\mathcal{B})}(\mu_F^2, t(\Phi_1)) \right]_{=1}$$

POWHEG

- ▶ pitfall, again: have to replace $\mu_F^2 \rightarrow s$ to fill entire phase space for first emission same implications as for MEC
- ▶ leads to formally sub-leading but numerically large deviations from NLO in distributions



Alioli, Nason, Oleari, Re, JHEP 0904 (2009) 002

POWHEG

- ▶ pitfall, again: have to replace $\mu_F^2 \rightarrow s$ to fill entire phase space for first emission same implications as for MEC
- ▶ leads to formally sub-leading but numerically large deviations from NLO in distributions
- ▶ \mathcal{R}/\mathcal{B} generates sub-leading logs that get exponentiated not clear whether they should be exponentiated
- ▶ all configurations enhanced by local K -factor K -factor for inclusive production of X adequate for $X + \text{jet}$ at large p_\perp ?
- ▶ some \mathcal{R} configurations cannot be generated by adding an extra emission to \mathcal{B}
- ▶ all events have positive weights

Improved POWHEG

- ▶ split real-emission matrix element

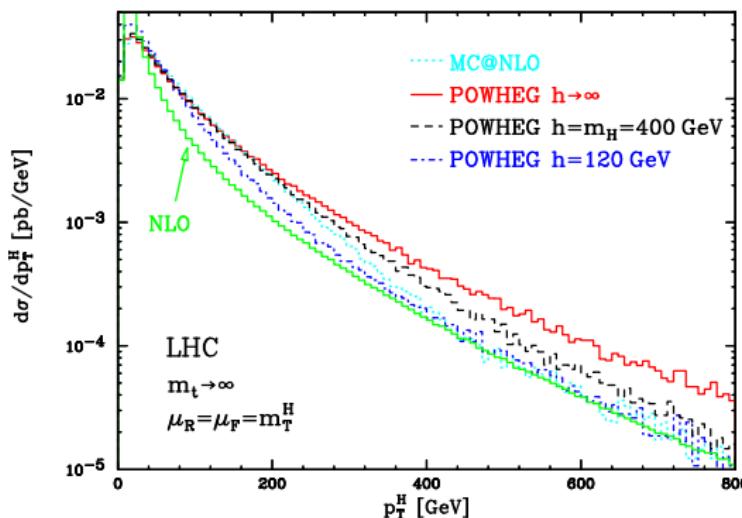
$$\mathcal{R} = \mathcal{R} \left(\frac{h^2}{p_\perp^2 + h^2} + \frac{p_\perp^2}{p_\perp^2 + h^2} \right) = \mathcal{R}^{(S)} + \mathcal{R}^{(F)}$$

- ▶ can “tune” h to mimick NNLO or other (resummation) result
- ▶ differential event rate up to first emission

$$\begin{aligned} d\sigma_{\text{POWHEG}}^{(\text{NLO})} &= d\Phi_N \bar{\mathcal{B}}^{(\mathcal{R}^{(S)})} \left[\Delta_N^{(\mathcal{R}^{(S)}/\mathcal{B})}(s, t_0) + \int_{t_0}^s d\Phi_1 \frac{\mathcal{R}^{(S)}}{\mathcal{B}} \Delta_N^{(\mathcal{R}^{(S)}/\mathcal{B})}(s, t) \right] \\ &\quad + d\Phi_{N+1} \mathcal{R}^{(F)}(\Phi_{N+1}) \end{aligned}$$

NLO matching

Improved POWHEG



Alioli, Nason, Oleari, Re, JHEP 0904 (2009) 002

MC@NLO

Frixione, Webber, JHEP 0206 (2002) 029; Hoeche, Krauss, Schonherr, Siegert, JHEP 1209 (2012) 049

- divide \mathcal{R} in IR-singular (soft) and IR-regular (hard) part

$$\mathcal{R} = \mathcal{R}^{(S)} + \mathcal{R}^{(H)} = \mathcal{D} + \mathcal{H}$$

- NLO weighted Born configuration simplifies

$$\bar{\mathcal{B}}^{(\mathcal{R}^{(S)})}(\Phi_N) \longrightarrow \tilde{\mathcal{B}}(\Phi_N) = \mathcal{B}(\Phi_N) + \mathcal{V}(\Phi_N) + \mathcal{I}(\Phi_N)$$

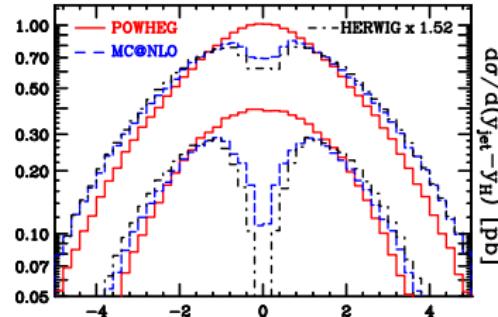
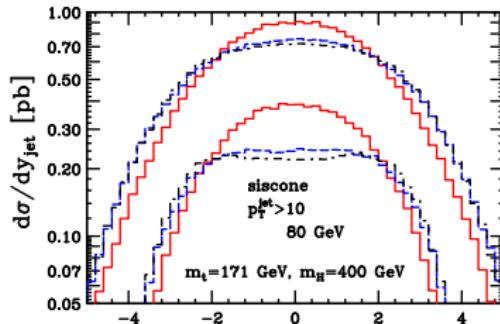
- use subtraction kernels as splitting kernels in PS $\mathcal{K}_N = \mathcal{D}$

$$\begin{aligned} d\sigma_{\text{MC@NLO}}^{(\text{NLO})} &= d\Phi_N \tilde{\mathcal{B}}(\Phi_N) \left[\Delta_N^{(\mathcal{K})}(\mu_F^2, t_0) + \int_{t_0}^{\mu_F^2} d\Phi_1 \mathcal{K}_N(\Phi_1) \Delta_N^{(\mathcal{K})}(\mu_F^2, t(\Phi_1)) \right] \\ &\quad + d\Phi_{N+1} \mathcal{H}(\Phi_{N+1}) \end{aligned}$$

NLO matching

MC@NLO

- ▶ only resummed parts modified with local K -factor
- ▶ process independent no tuning of h
- ▶ makes high demands on parton shower:
 - ▶ parton shower must reproduce full IR structure problem with soft singularities in monopole showers
 - ▶ first emission must be full colour correct
 - ▶ parton shower has to fill phase space properly
- ▶ events can have negative weights



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 - ▶ first emission must be full colour correct
 - ▶ parton shower has to fill phase space properly
- ▶ events can have negative weights
- ▶ some formally sub-leading terms can become numerically largevisible in some observables in processes with large NLO corrections
can be cured by NLO multi-jet merging

Multi-jet merging: Basic idea

- ▶ parton shower resums logarithms
 - ▶ fair description of collinear/soft emissions
 - ▶ jet evolution

where the logs are large
- ▶ matrix elements exact at given order
 - ▶ fair description of hard/large-angle emissions
 - ▶ jet production

where the logs are small
- ▶ combine (“merge”) both:
results in “towers” of MEs with increasing number of jets evolved with PS
 - ▶ multi-jet cross sections at Born accuracy
 - ▶ maintain (N)LL accuracy of parton shower

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Multi-jet merging

Multi-jet merging: Basic idea

Problem: Overlap between ME and PS

- ▶ cross sections in fixed order perturbation theory are **inclusive**
- ▶ parton shower reproduces leading-log approximation of cross section

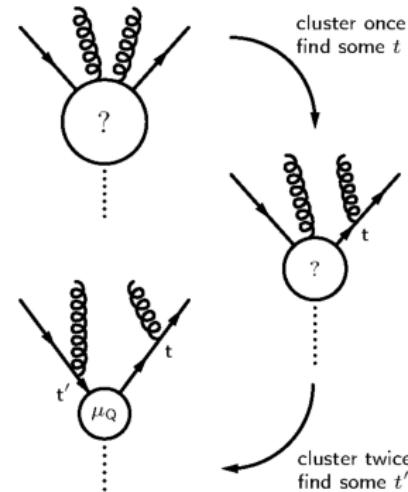
Solution

- ▶ introduce merging scale t_{MS} to divide phase space in
 - ▶ $t > t_{\text{MS}}$: hard regime to be populated by matrix elements
 - ▶ $t < t_{\text{MS}}$: soft/collinear regime to be populated by PS
- ▶ make matrix elements exclusive above t_{MS}
- ▶ restrict parton shower to radiate only below t_{MS}

Translating MEs to PS language: Parton shower histories

Andre, Sjostrand, Phys. Rev. D 57 (1998) 5767

- ▶ translate matrix element into branching sequence
- ▶ can be achieved by “running PS backwards”
 - ▶ identify most likely splitting according to PS emission probability
 - ▶ combine partons into mother according to PS kinematics
 - ▶ continue until core process is reached
- ▶ core process is considered inclusive
- ▶ it sets the resummation scale t_{\max}



MLM merging

Mangano, Moretti, Piccinini, Treccani, JHEP 0701 (2007) 013

MLM procedure

1. generate parton configuration from matrix element with $E_{\perp} > E_{\perp}^{\min}$ and angular separation $\Delta R_{jj} > R_{\min}$
2. shower event without restrictions on parton shower
3. cluster jets with cone radius R_{\min} and $E_{\perp} > E_{\perp}^{\min}$
4. match partons and jets
5. reject event if not all partons and jets match or additional jets have been produced
6. add all accepted events

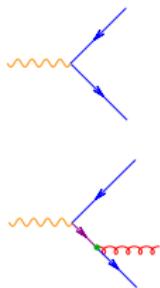
- ▶ works in practice
- ▶ theoretically not fully under control

Multi-jet merging

CKKW/CKKW-L merging

Catani, Krauss, Kuhn, Webber, JHEP 0111 (2001) 063 & Lonnblad, JHEP 0205 (2002) 046

- ▶ configurations generated by parton shower are exclusive
- ▶ e.g. jet rates in $e^+ + e^- \rightarrow \text{jets}$
- ▶ Durham jet definition: relative transverse momentum $k_\perp > t_{\text{MS}}$



$$\mathcal{P}_2(t_{\text{MS}}) = [\Delta_q(t_{\text{max}}, t_{\text{MS}})]^2$$

$$\begin{aligned} \mathcal{P}_3(t_{\text{MS}}) = & 2\Delta_q(t_{\text{max}}, t_{\text{MS}}) \int_{t_{\text{MS}}}^{t_{\text{max}}} \frac{dk_\perp^2}{k_\perp^2} \left[\int dz \frac{\alpha_s}{2\pi} \mathcal{K}_q(k_\perp^2, z) \right. \\ & \times \left. \Delta_q(t_{\text{max}}, k_\perp^2) \Delta_q(k_\perp^2, t_{\text{MS}}) \Delta_g(k_\perp^2, t_{\text{MS}}) \right] \end{aligned}$$

- ▶ Sudakov factors prevent further emissions

Truncated & vetoed parton shower

- ▶ make ME exclusive by multiplying Sudakov factors
- ▶ can be done using analytic Sudakov factors (CKKW) or the parton shower (CKKW-L)

METS procedure

1. regularise matrix element with t_{MS} and generate configuration
2. cluster backwards until core process is reached
3. starting from t_{max} evolve until predefined branching
 ↪ “truncated parton shower”
4. insert branching defined by matrix element
5. continue until t_0 is reached
6. emissions with $t > t_{\text{MS}}$ lead to rejection of event ↪ “veto”

Multi-jet merging

LO merging in MC@NLO notation

- vetoed shower generates Sudakov form factor

$$\Delta_N^{(\mathcal{K})}(t_{\max}, t; > t_{\text{MS}}) = \exp \left\{ - \int_{t_0}^t d\Phi_1 \mathcal{K}_N(\Phi_1) \theta(t - t_{\text{MS}}) \right\}$$

- expression for first emission

$$d\sigma_{\text{CKKW}} = d\Phi_N \mathcal{B} \left[\Delta_N^{(\mathcal{K})}(t_{\max}, t_0) + \int_{t_0}^{t_{\max}} d\Phi_1 \mathcal{K}_N \Delta_N^{(\mathcal{K})}(t_{\max}, t) \theta(t_{\text{MS}} - t) \right] \\ + d\Phi_{N+1} \mathcal{B}_{N+1}(\Phi_{N+1}) \Delta_N^{(\mathcal{K})}(t_{\max}, t; > t_{\text{MS}}) \theta(t - t_{\text{MS}})$$

- can add more matrix elements in the same way

Other techniques and approaches

UMEPS: unitary (process independent) multi-jet merging

Lönnblad, Prestel, JHEP 1302 (2013) 094 & Plätzer, JHEP 1308 (2013) 114

FxFx: MLM at NLO

Frixione, Frederix, JHEP 1212 (2012) 061

MEPS@NLO: process independent multi-jet merging at NLO

Höche, Krauss, Schönher, Siegert JHEP 1304 (2013) 027 & JHEP 1301 (2013) 144

UNLOPS: UMEPS at NLO

Lönnblad, Prestel, JHEP 1303 (2013) 166 & Plätzer, JHEP 1308 (2013) 114

MinLO: NLO+PS for Higgs and DY without merging cut

Hamilton, Nason, Oleari, Zanderighi, JHEP 1305 (2013) 082

UN²LOPS: UMEPS at NNLO for Higgs and Drell-Yan

Höche, Li, Prestel, Phys. Rev. D 91 (2015) no.7, 074015

NNLOPS: MinLO based NNLO+PS for Higgs and Drell-Yan

Hamilton, Nason, Re, Zanderighi, JHEP 1310 (2013) 222

NLO QCD+EW: including multi-jet merging

Kallweit, Lindert, Maierhofer, Pozzorini, Schönher, JHEP 1604 (2016) 021

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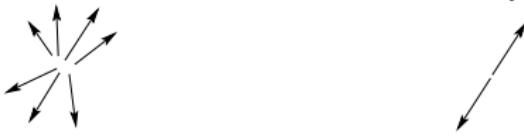
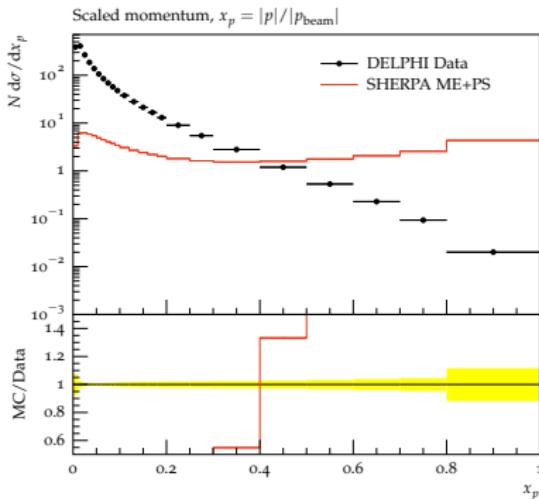
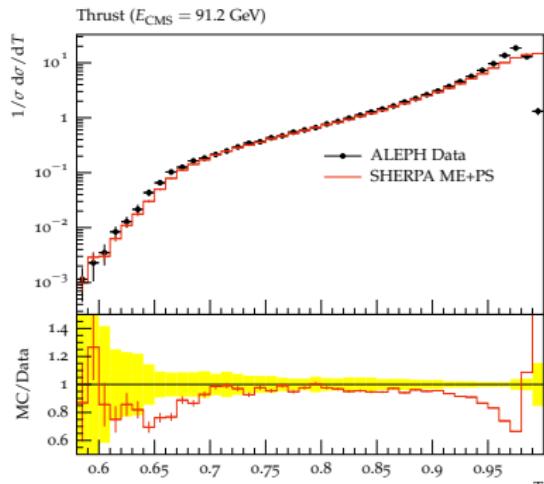
LHC: other processes

Other tools

Summary

LEP: $e^+ + e^- \rightarrow$ jets

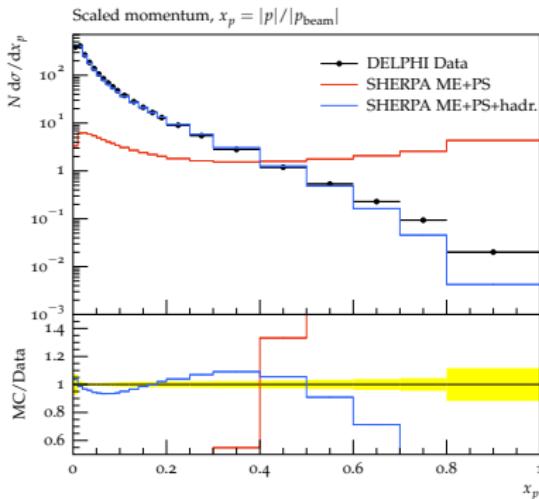
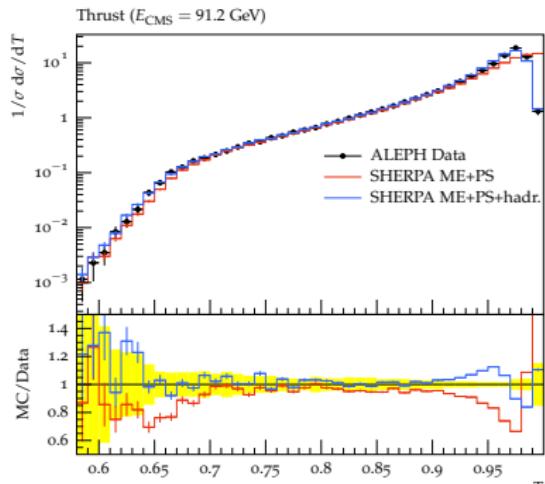
$e^+ + e^- \rightarrow \text{jets at LEP}$



ALEPH, Eur. Phys. J. C35 (2004) 457; DELPHI, Z. Phys. C73 (1996) 11

LEP: $e^+ + e^- \rightarrow \text{jets}$

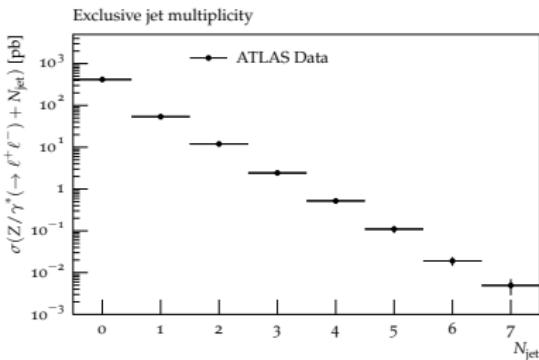
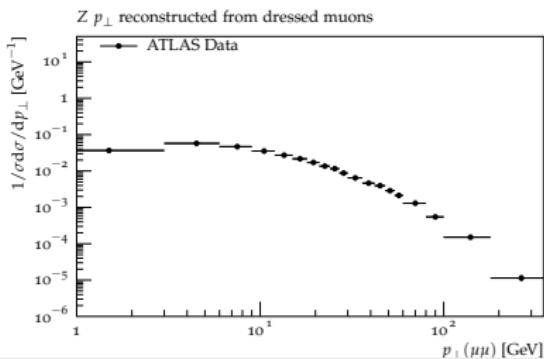
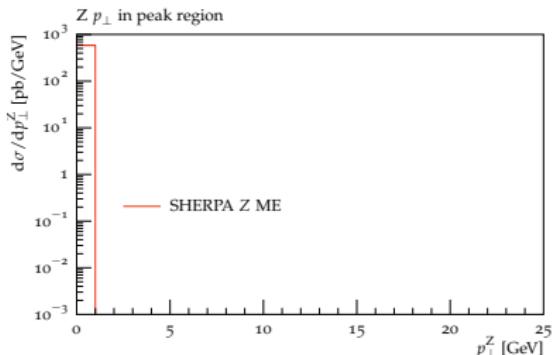
$e^+ + e^- \rightarrow \text{jets at LEP}$



ALEPH, Eur. Phys. J. C35 (2004) 457; DELPHI, Z. Phys. C73 (1996) 11

LHC: $Z + \text{jets}$

Z + jets at LHC

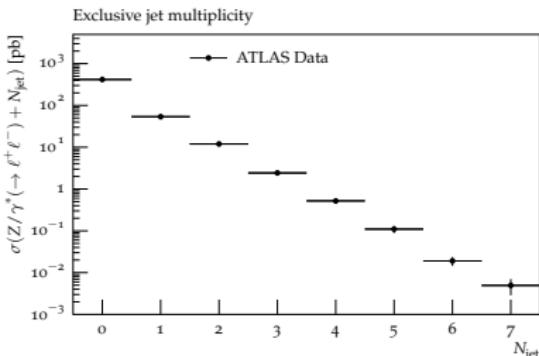
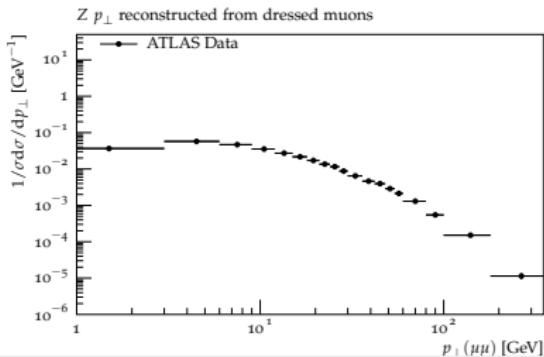
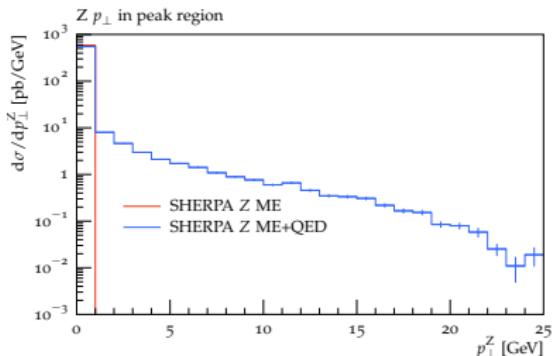


ATLAS, JHEP 1307 (2013) 032

ATLAS, Phys. Lett. B 705 (2011) 415

LHC: $Z + \text{jets}$

Z + jets at LHC

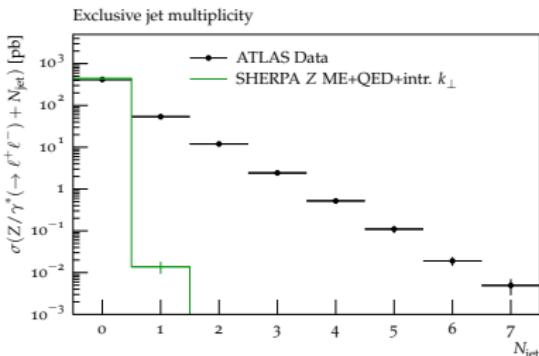
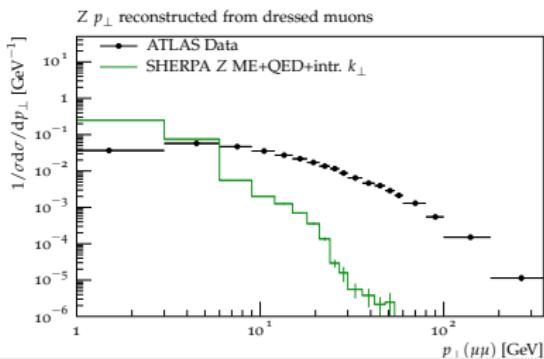
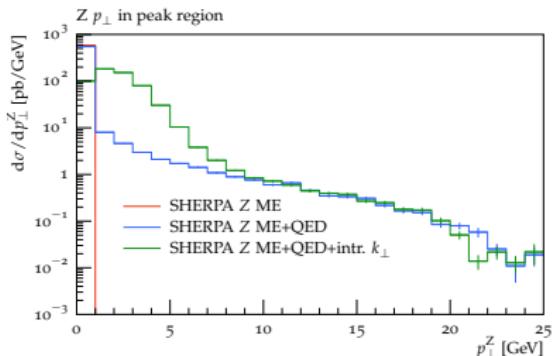


ATLAS, JHEP 1307 (2013) 032

ATLAS, Phys. Lett. B 705 (2011) 415

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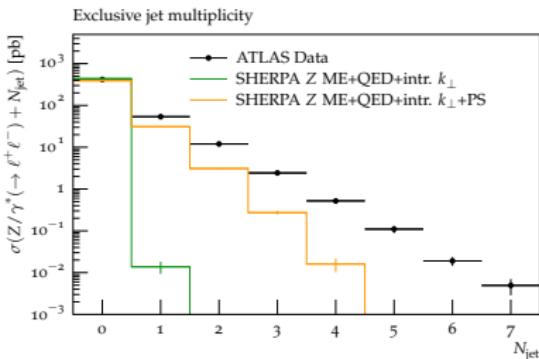
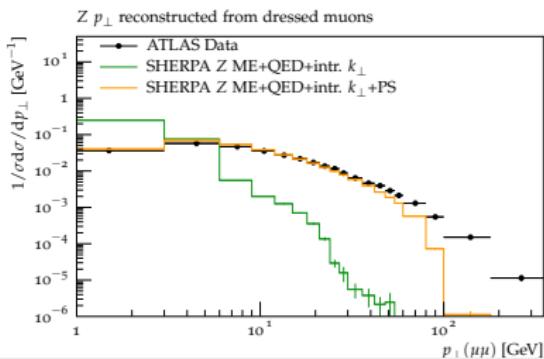
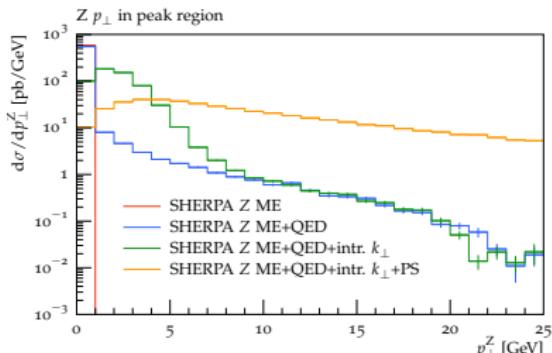


ATLAS, JHEP 1307 (2013) 032

ATLAS, Phys. Lett. B 705 (2011) 415

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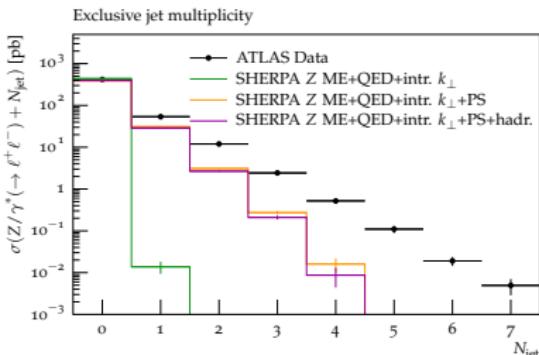
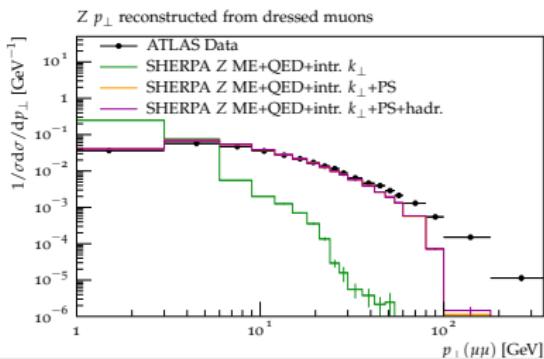
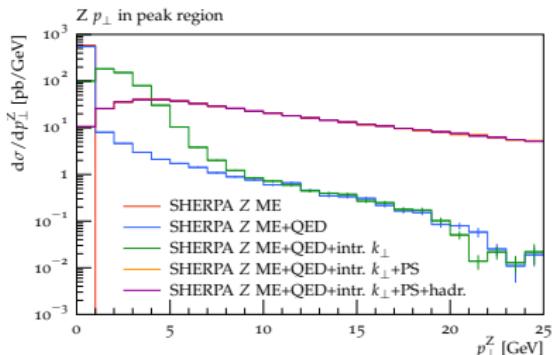


ATLAS, JHEP 1307 (2013) 032

ATLAS, Phys. Lett. B 705 (2011) 415

LHC: $Z + \text{jets}$

Z + jets at LHC

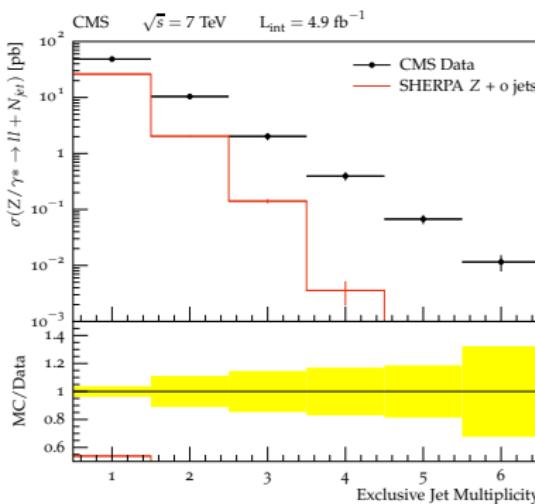
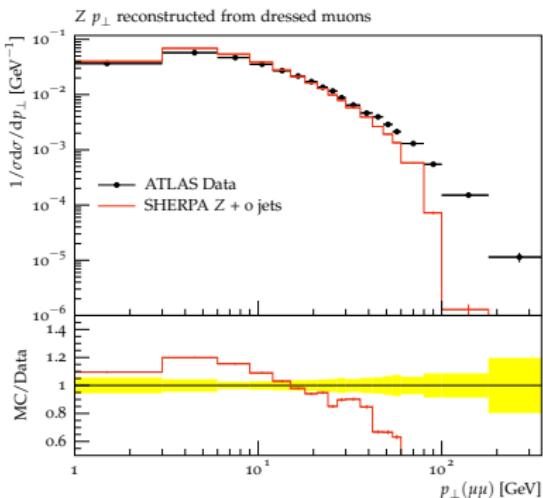


ATLAS, JHEP 1307 (2013) 032

ATLAS, Phys. Lett. B 705 (2011) 415

LHC: $Z + \text{jets}$

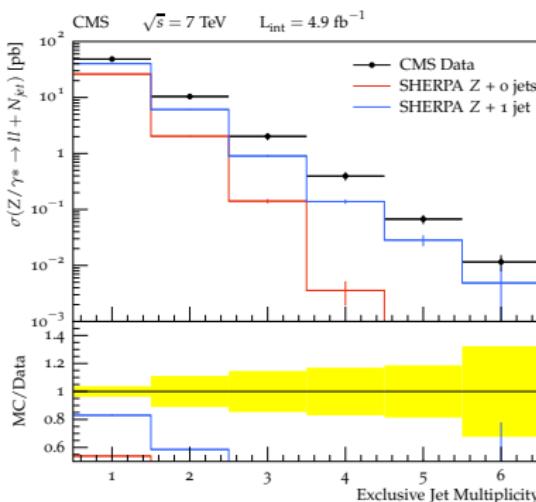
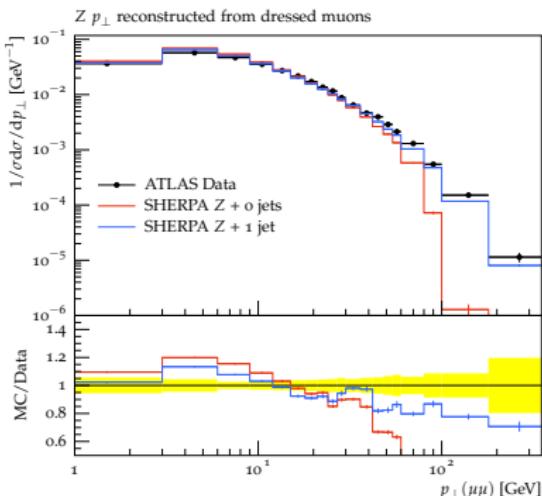
Now let's do LO multi-jet merging



ATLAS, Phys. Lett. B 705 (2011) 415; CMS, Phys. Rev. D 91 (2015) no.5, 052008

LHC: $Z + \text{jets}$

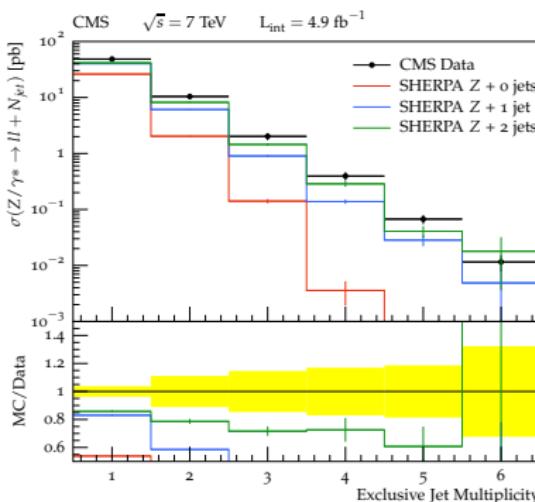
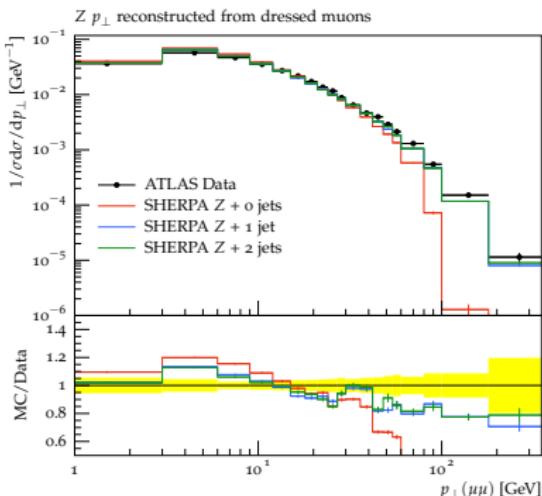
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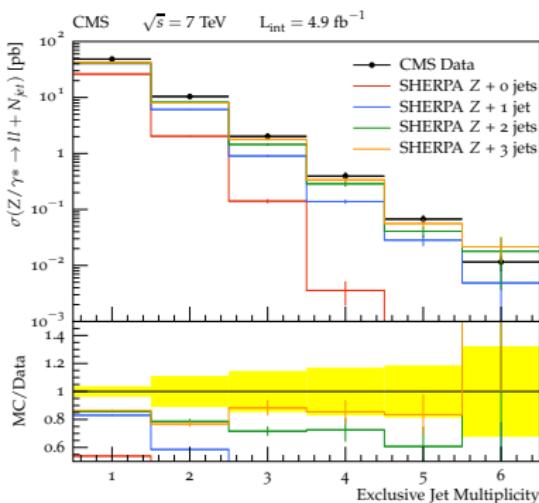
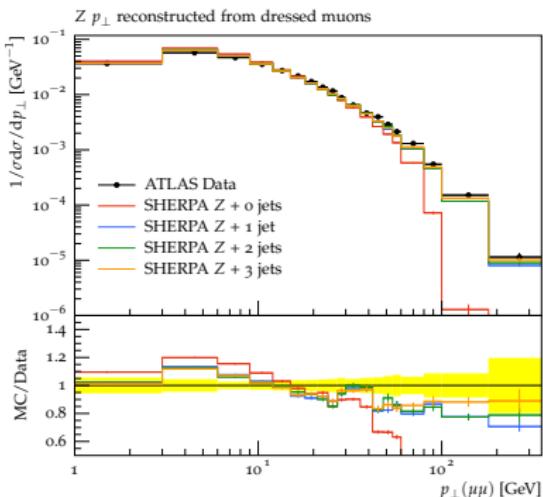
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ATLAS, Phys. Lett. B 705 (2011) 415; CMS, Phys. Rev. D 91 (2015) no.5, 052008

LHC: $Z + \text{jets}$

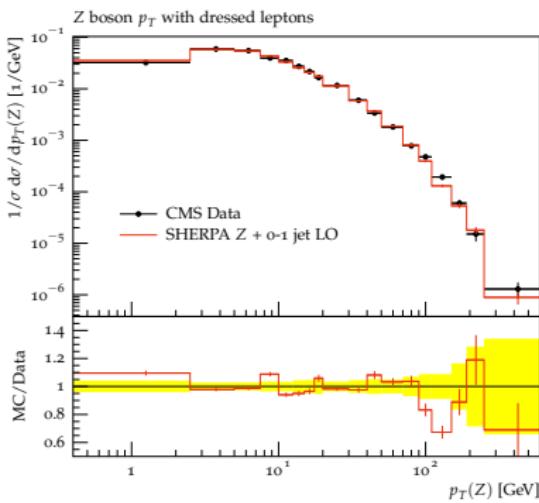
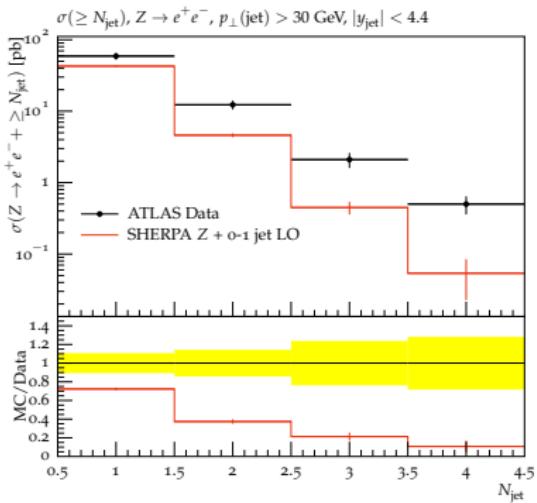
Now let's do LO multi-jet merging



ATLAS, Phys. Lett. B 705 (2011) 415; CMS, Phys. Rev. D 91 (2015) no.5, 052008

LHC: $Z + \text{jets}$

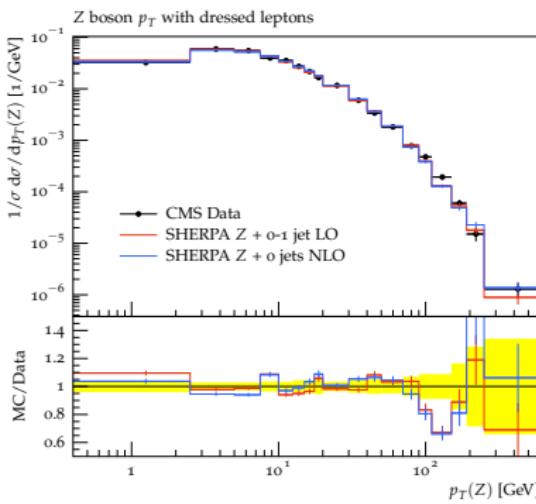
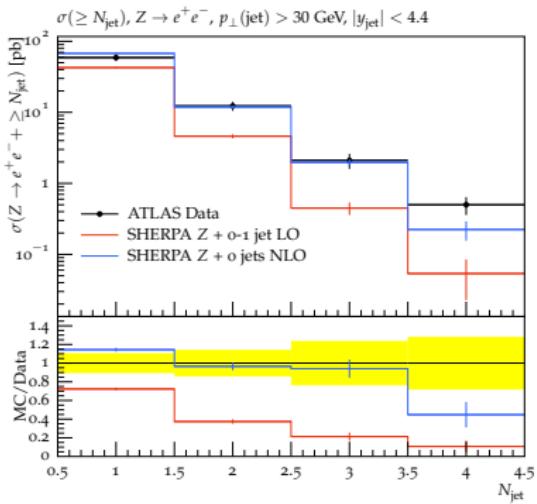
Adding NLO corrections



ATLAS, Phys. Rev. D 85 (2012) 032009; CMS, Phys. Rev. D 85 (2012) 032002

LHC: $Z + \text{jets}$

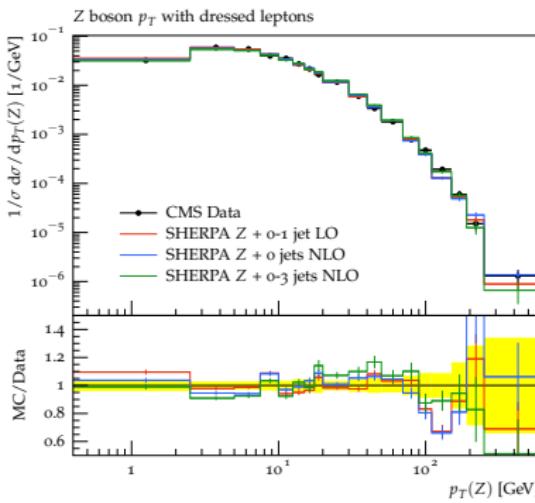
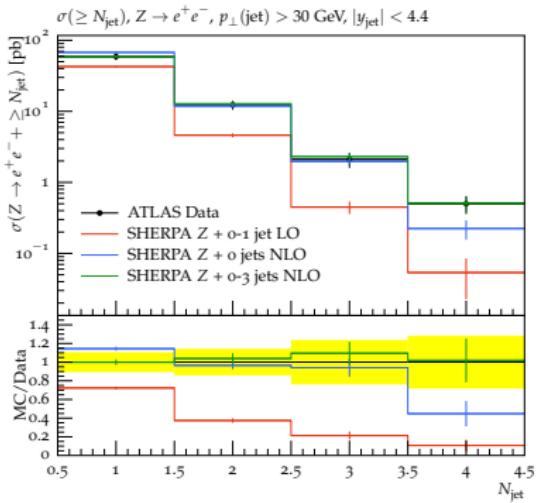
Adding NLO corrections



ATLAS, Phys. Rev. D 85 (2012) 032009; CMS, Phys. Rev. D 85 (2012) 032002

LHC: $Z + \text{jets}$

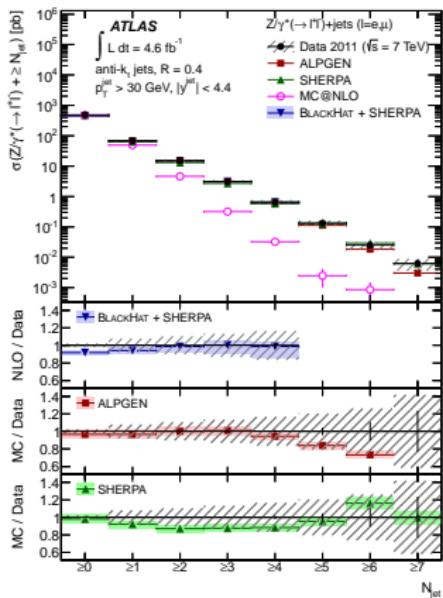
Adding NLO corrections



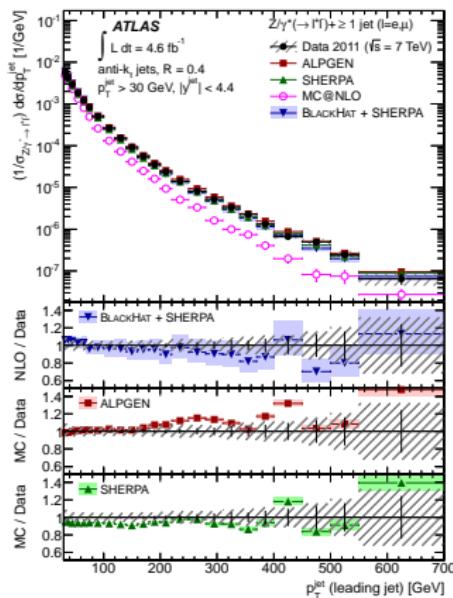
ATLAS, Phys. Rev. D 85 (2012) 032009; CMS, Phys. Rev. D 85 (2012) 032002

LHC: $Z + \text{jets}$

Different merging schemes



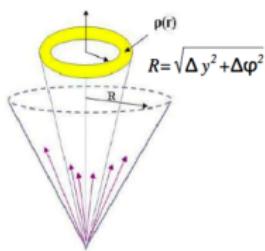
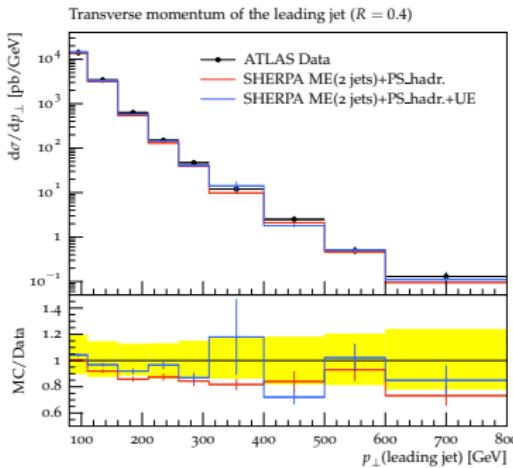
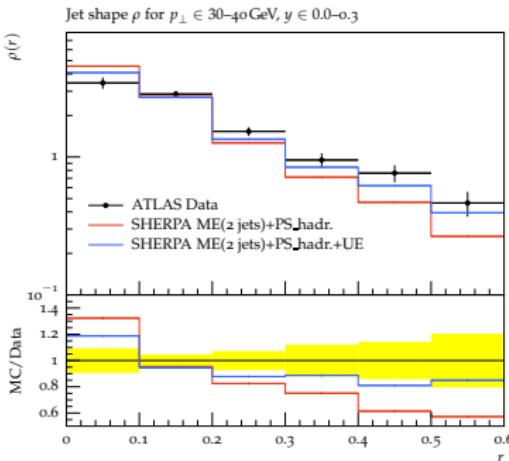
- ▶ ALPGEN: LO with MLM merging
 - ▶ SHERPA: LO with CKKW merging



ATLAS, JHEP 1307 (2013) 032

LHC: jets

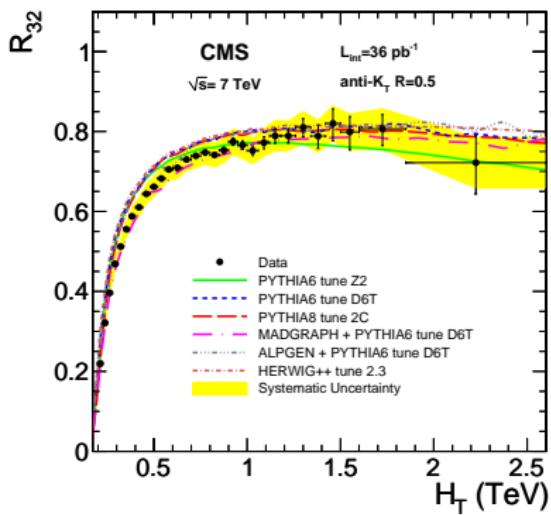
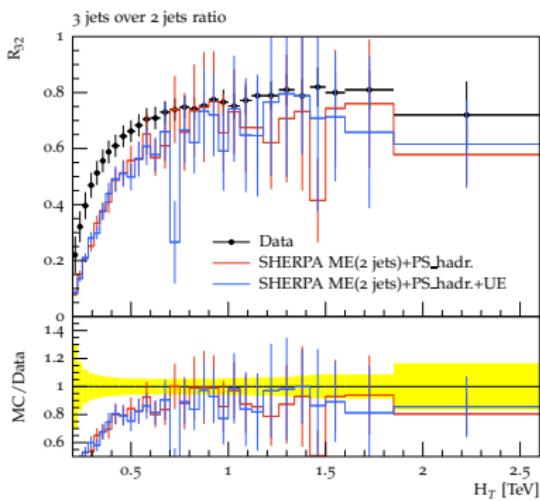
Effect of underlying event



ATLAS, Phys. Rev. D 83 (2011) 052003 & Eur. Phys. J. C 71 (2011) 1763

LHC: jets

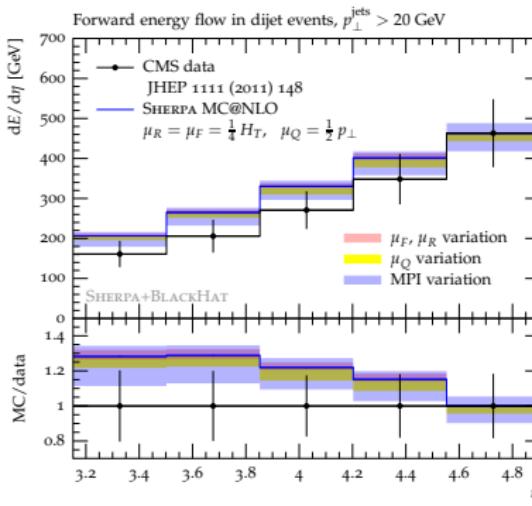
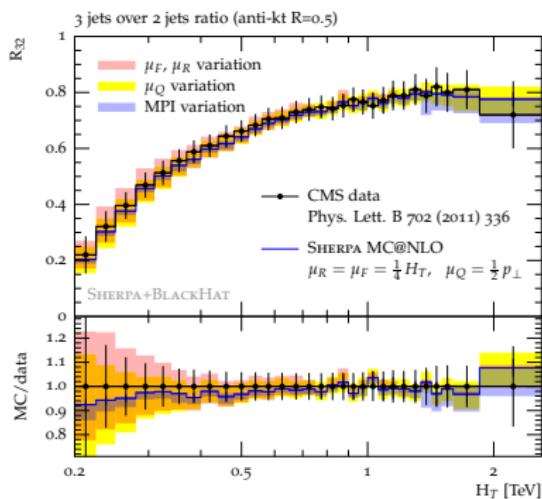
Shower vs. matrix element



CMS, Phys. Lett. B 702 (2011) 336

- ▶ H_T : scalar sum of jet p_\perp 's
 - ▶ jet $p_\perp > 50 \text{ GeV}$

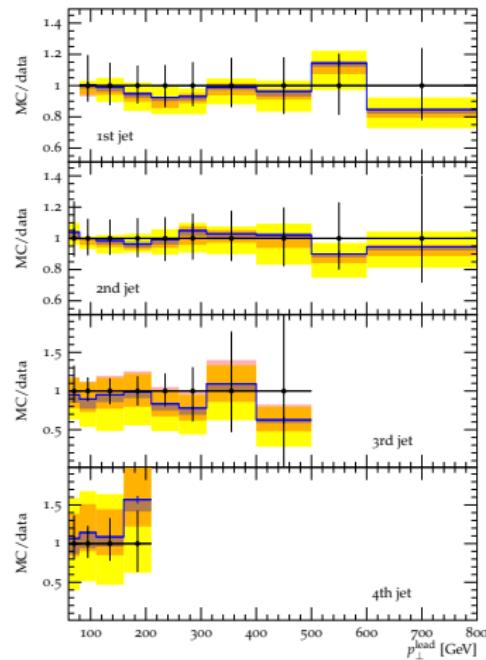
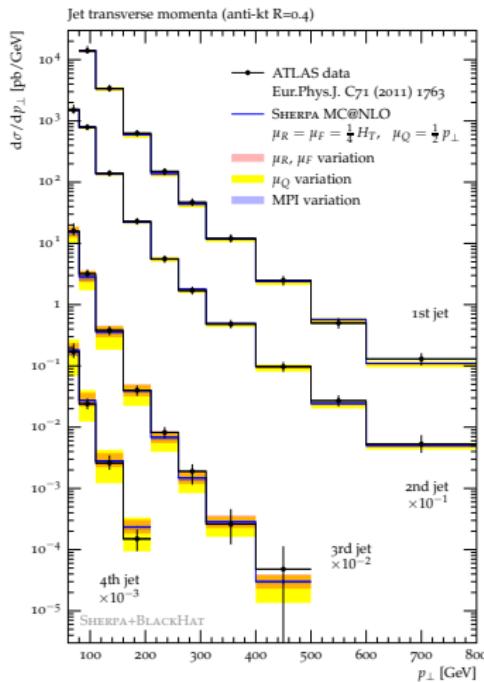
Theoretical uncertainties



Hoeche, Schonherr, Phys. Rev. D 86 (2012) 094042

LHC: jets

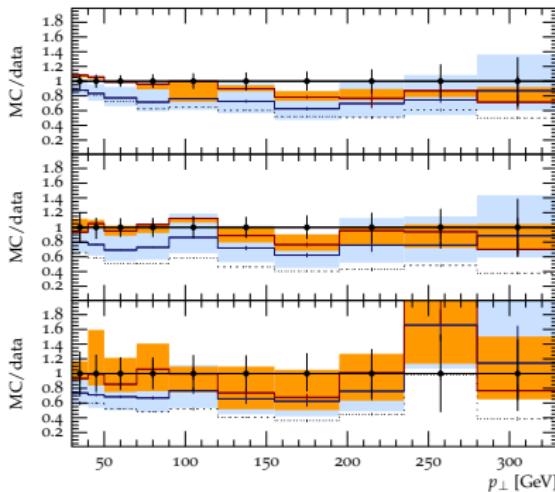
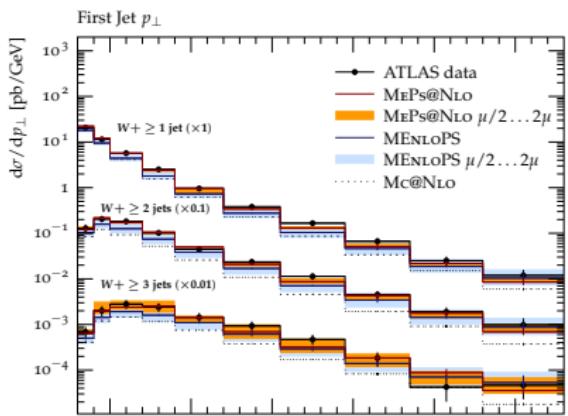
Theoretical uncertainties



Hoeche, Schonherr, Phys. Rev. D 86 (2012) 094042

LHC: other processes

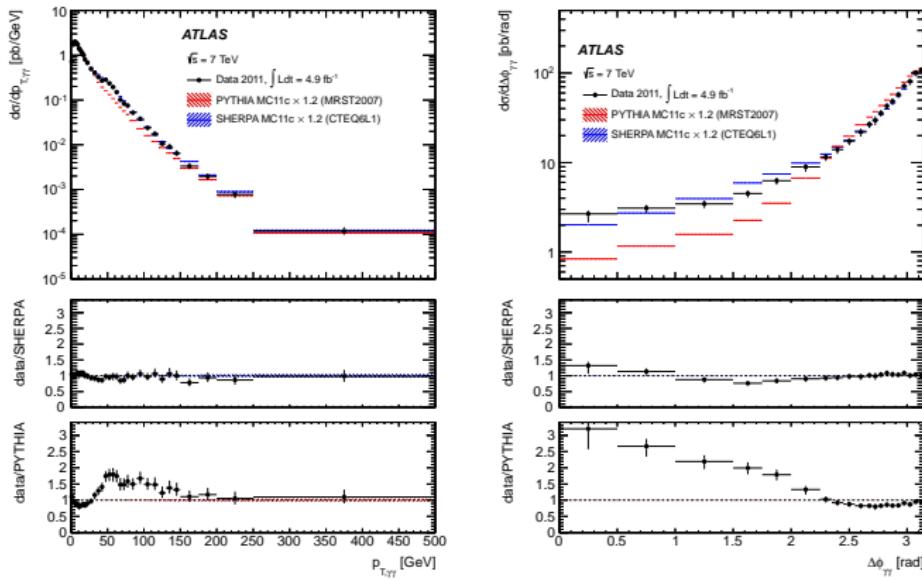
$W+jets$ – NLO merging



Hoeche, Krauss, Schonherr, Siegert, JHEP 1304 (2013) 027

LHC: other processes

Diphotons

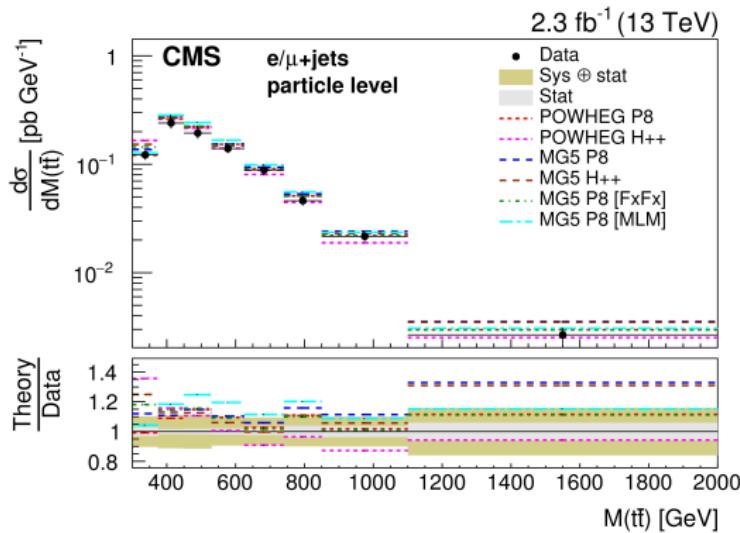


- ▶ PYTHIA: di-photon ME + PS
- ▶ SHERPA: di-photon ME merged with up to 2 jets + PS

ATLAS, JHEP 1301 (2013) 086

LHC: other processes

Top quark pairs

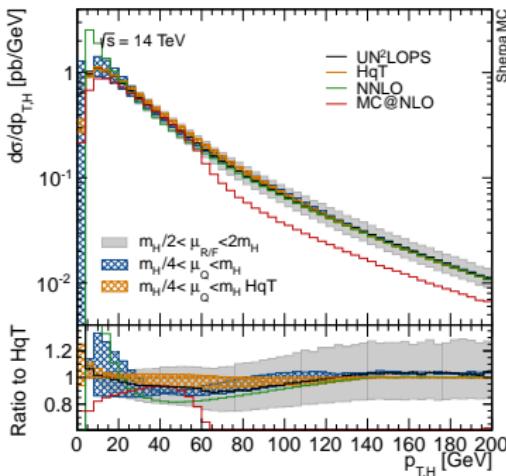
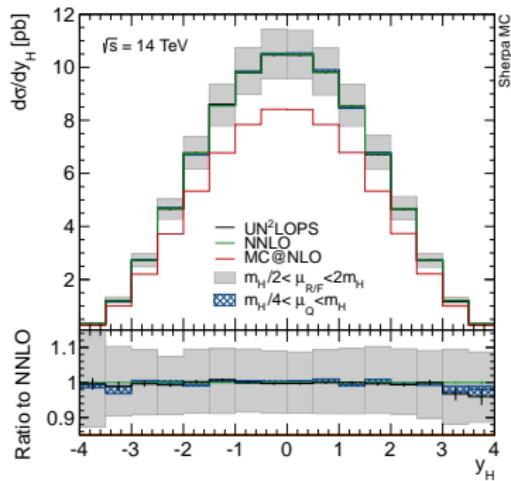


CMS, arXiv:1610.04191

MG5: MadGraph5_aMC@NLO (NLO matrix element generator including matching/merging); **P8:** PYTHIA8; **H++:** HERWIG++

LHC: other processes

Higgs – NNLO event generation



Höche, Li, Prestel, Phys. Rev. D 90 (2014) no.5, 054011

Outline

Higher order corrections in event generators

- Next-to-leading order matrix elements

- Matrix element corrections

- NLO matching

- Multi-jet merging

MC event generators at work

- LEP: $e^+ + e^- \rightarrow \text{jets}$

- LHC: $Z + \text{jets}$

- LHC: jets

- LHC: other processes

Other tools

Summary

RIVET

<http://rivet.hepforge.org>

- ▶ HEP tool for analysing Monte Carlo events
 - ▶ generator independent code due to “industry standard” for simulated events (HepMC)
 - ▶ powerful library of predefined calculators (e.g. event shapes, jets, Z- finder, . . .)
 - ▶ analyses are based on physical objects
 - ▶ final state hadrons
 - ▶ muons, electrons (dressed)
 - ▶ bosons reconstructed from particles
 - ▶ ...
 - ▶ allows for fair comparison with (unfolded) collider data
- rather than taken from event record

RIVET

- ▶ version 2.5 contains ~ 350 Analyses (195 LHC)
- ▶ plugin system for new analyses
- ▶ lightweight histogramming (YODA), quite ok plotting
- ▶ exploration of BSM physics (UFO + Herwig7/Sherpa)

RIVET serves twofold purpose

- ▶ Monte Carlo validation and tuning
- ▶ data preservation

data are useless without detailed information about analysis

PROFESSOR

<http://professor.hepforge.org>

- ▶ phenomenological models in event generators have to be tuned to data
- ▶ many parameters → brute force doesn't work
- ▶ PROFESSOR procedure:
 1. random sampling: N parameter points in n -dimensional space
 2. run generator and fill histograms
 3. for each bin: use N points to fit interpolation (2nd or 3rd order polynomial)
 4. construct overall $\chi^2 \approx \sum_{\text{bins}} \frac{(\text{interpolation} - \text{data})^2}{\text{error}^2}$
 5. numerically minimise

Other tools and standards

HepMC: generator independent event record for MC events

<http://hepmc.web.cern.ch/hepmc/>

LHAPDF: general purpose interpolator for evaluating PDFs from discretised data files, provides PDFs to MC generators

<http://lhapdf.hepforge.org/>

FASTJET: provides jet finding algorithms and related tools like taggers, used by RIVET

<http://www.fastjet.fr/>

DELPHES/GEANT: detector simulation

<http://cp3.irmp.ucl.ac.be/projects/delphes>; <http://geant4.web.cern.ch/geant4/>

Binoth LHA/LHEF: standard for passing matrix element configurations between generators

arXiv:1003.1643

PDG particle codes: system for numbering particles
many more ...

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LHC: $Z + \text{jets}$

LHC: jets

LHC: other processes

Other tools

Summary

Summary

- ▶ double counting has to be avoided when combining higher order matrix elements with each other and parton showers
- ▶ NLO ME + PS matching: POWHEG & MC@NLO
- ▶ merging of MEs of different multiplicity (combined with parton showers): different techniques available at LO and NLO
 - MLM, CKKW(-L), MEPS@NLO, ...
- ▶ MC event generators are controlled and quantitative tools
- ▶ MC generators essential for
 - ▶ interpretation of collider data
 - ▶ correction of detector effects
- ▶ additional tools are needed around generators, in particular RIVET for analysis and data preservation