



# Energy loss models and jet measurements with ALICE

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Seminar Munster 23-11-2012

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# Outline

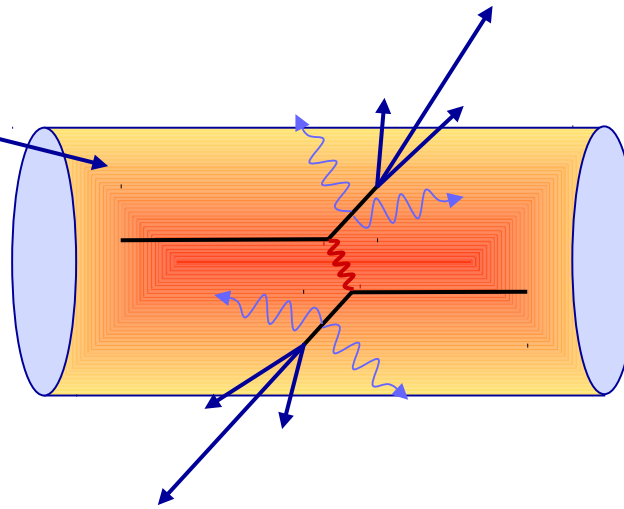
- In-medium energy loss models
  - Parton energy loss in realistic geometry
  - Systematic comparison of models
- Jets with ALICE in Pb-Pb collisions
  - Jet spectra
  - Jet suppression
  - Jet broadening

# Hard Probes in QCD matter

Heavy-ion collisions produce  
dense QCD matter

Dominated by soft partons

$\rho \sim T \sim 100\text{-}300 \text{ MeV}$



Hard-scatterings produce high energetic partons

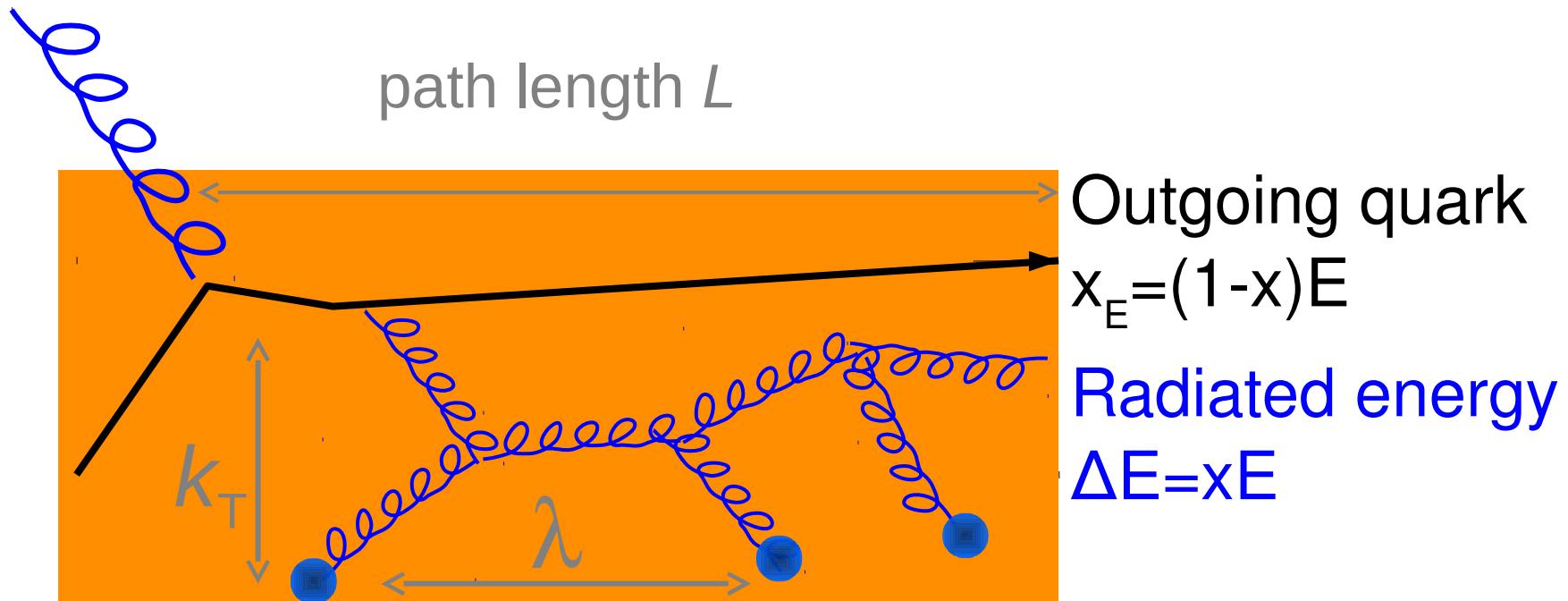
⇒ Initial-state production known from pQCD

⇒ Probe medium through energy loss

**Use hard partons to explore QCD matter**

Sensitive to properties of the medium

# Schematic picture of energy loss mechanism in hot dense matter



- Energy loss due to gluon bremsstrahlung in a hot dense medium
- What can we learn from Pb-Pb measurements & comparison to models?

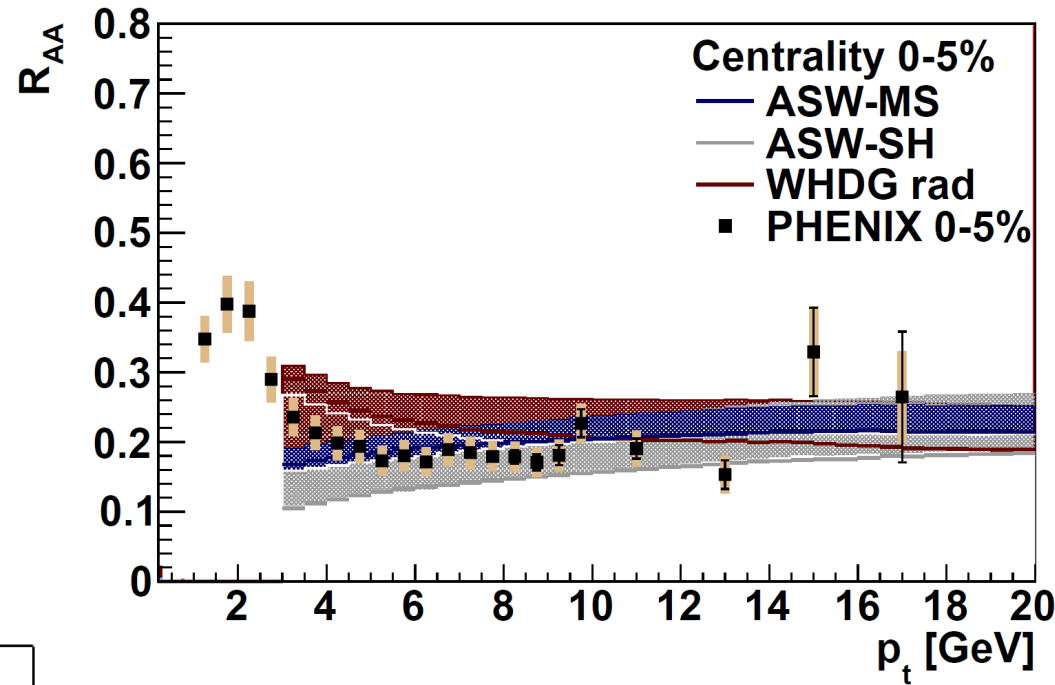
# Comparison of energy loss models with data

# $R_{AA}$ at RHIC

$$R_{AA} = \frac{dN / dp_T |_{Au+Au}}{N_{coll} dN / dp_T |_{p+p}}$$

- Common input parameter for all models: **medium temperature**
- **All models can be fitted to  $R_{AA}$**

	If $\tau < \tau_0 \hat{q} = \hat{q}_0$	
	$\hat{q}_0$ (GeV/fm <sup>2</sup> )	$T_0$ (MeV)
ASW-MS	$20.3^{+0.6}_{-5.1}$	$973^{+6}_{-90}$
WHDG rad	$5.7^{+0.3}_{-1.9}$	$638^{+11}_{-81}$
ASW-SH	$3.2^{+0.3}_{-0.3}$	$524^{+17}_{-18}$

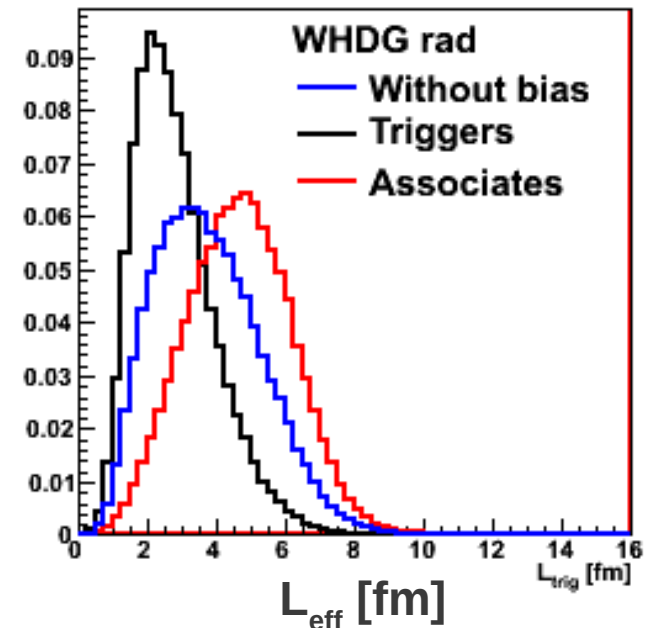
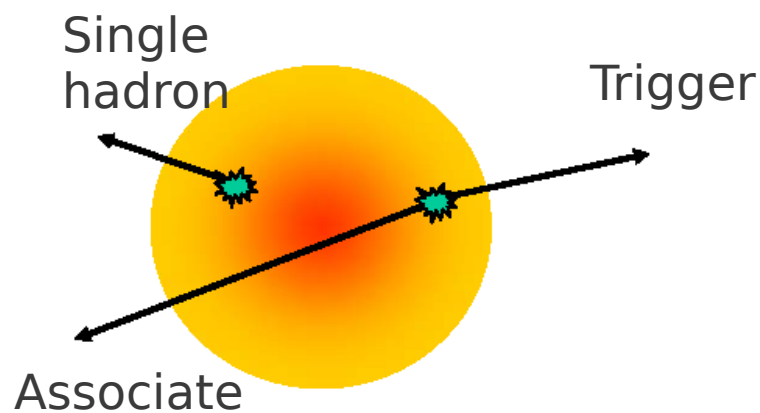


**Factor 4-5 difference in estimated medium density between different models**

PHENIX data: *Phys. Rev. C*77, 064907 (2008)

# Path length bias for di-hadrons

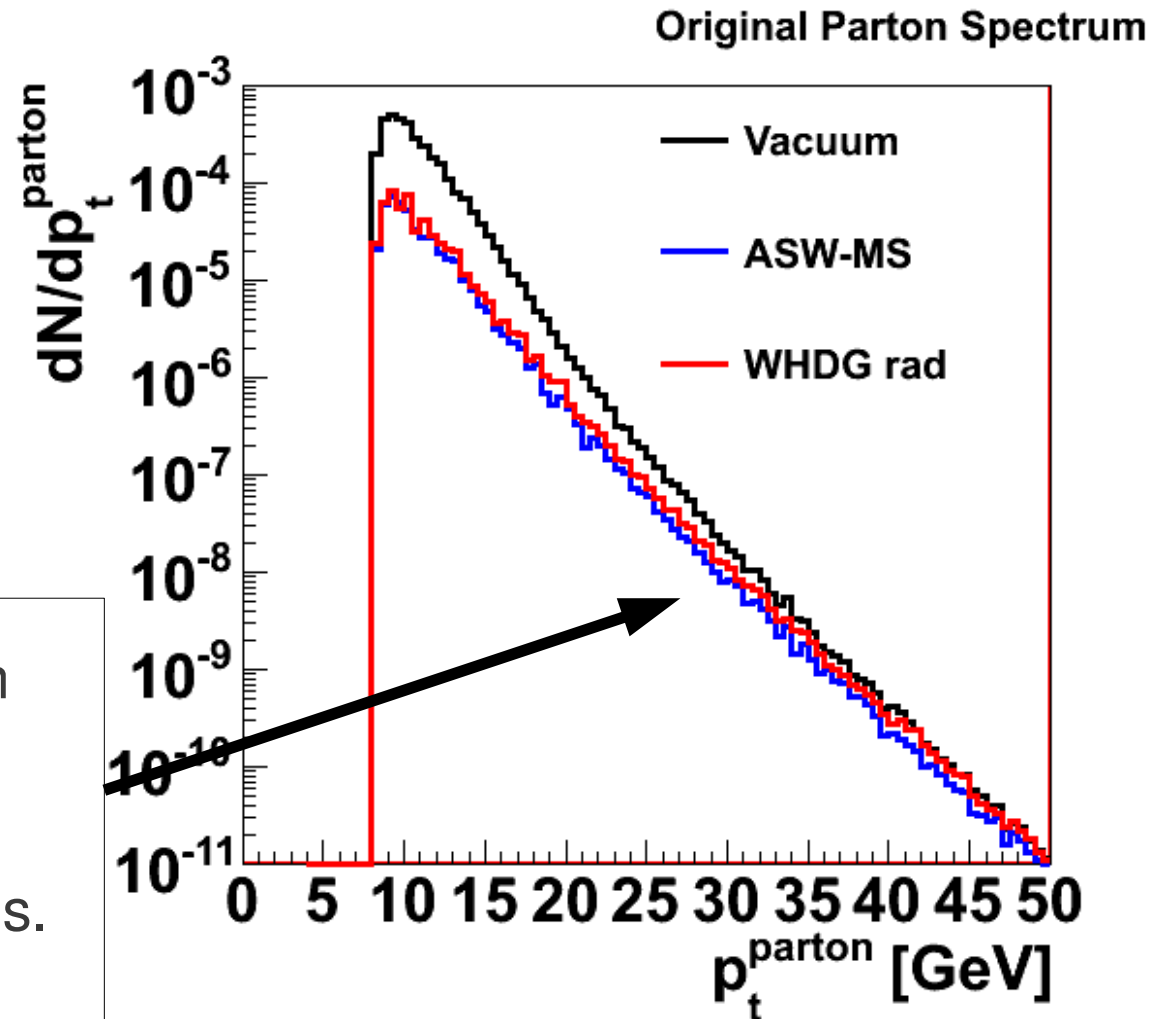
- $p_T \text{ Trigger} > p_T \text{ Assoc}$
- For  $R_{AA}$  and  $I_{AA}$  different mean path length.
- **Trigger:** bias towards smaller  $L$
- **Associate:** bias towards longer  $L$



# $R_{AA}$ vs $I_{AA}$

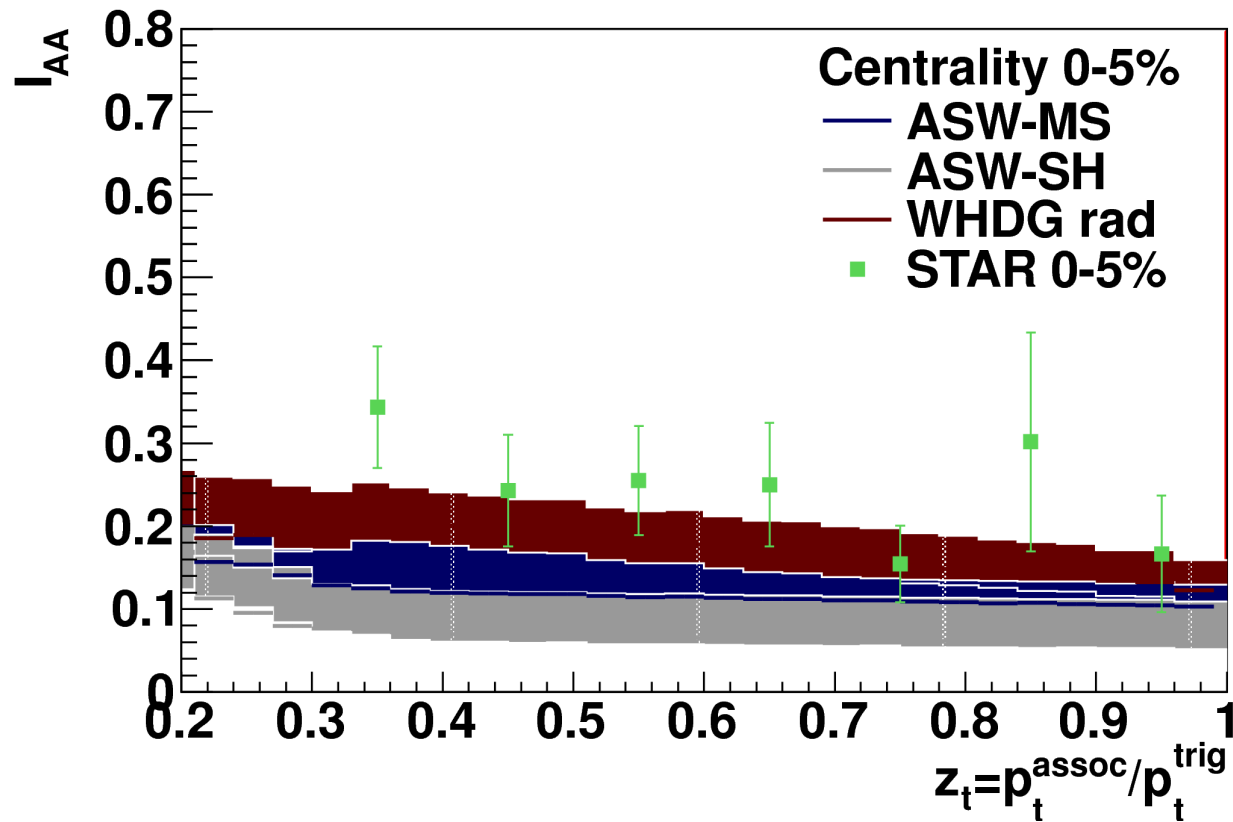
- What is the difference between  $R_{AA}$  and  $I_{AA}$ ?
- Different part of the parton spectrum is probed.

Original parton spectra resulting in hadrons with  $8 < p_t^{\text{hadron}} < 15$  GeV for without (vacuum) and with (ASW-MS/WHDG) energy loss.

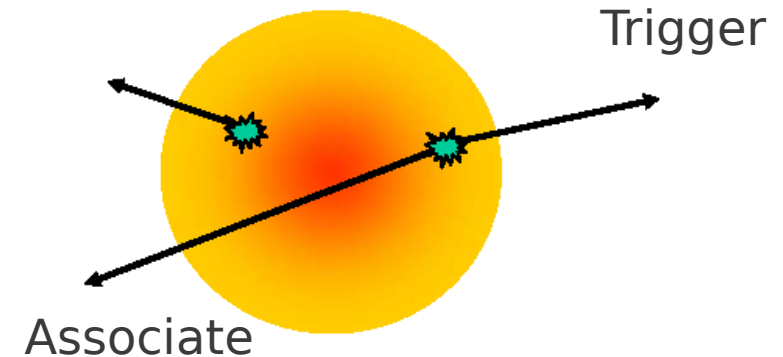




# $I_{AA}$ at RHIC



- Calibrate density using  $R_{AA}$
- Most models underestimate  $I_{AA}$



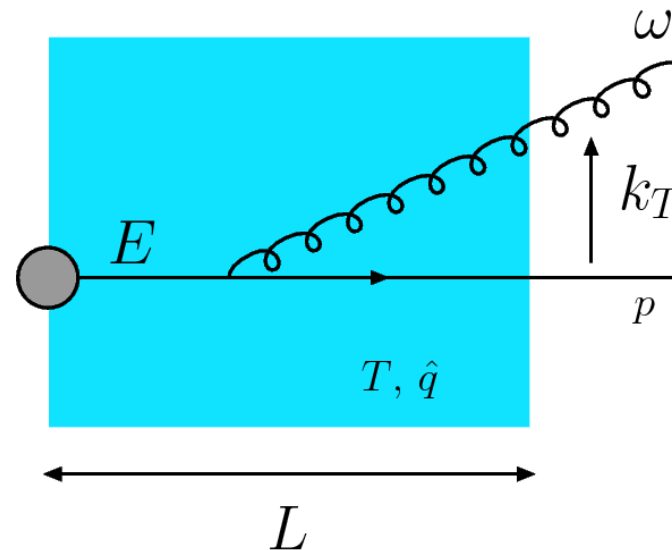
# Brick Problem

Goal: understand discrepancy in estimated medium density by models

# Brick Problem

TECHQM: Theory-Experiment Collaboration on Hot Quark Matter

arXiv:1106.1106



Compare energy loss models in a well-defined system:

- Fixed medium length  $L$  and temperature  $T$  (or  $\hat{q}$ )
- Parton (quark) propagates through brick,  $E_{\text{parton}} = 10, 20 \text{ GeV}$

Compare outgoing radiated gluon and parton distributions  
2 cases: same density, same suppression

# Four formalisms

- **Hard Thermal Loops (AMY)**

- Dynamical (HTL) medium
- Single gluon spectrum: BDMPS-Z like path integral
- No vacuum radiation

Multiple gluon emission

Fokker-Planck  
rate equations

- **Multiple soft scattering (BDMPS-Z, ASW-MS)**

- Static scattering centers
- Gaussian approximation for momentum kicks
- Full LPM interference and vacuum radiation

Poisson ansatz

(independent emission)

- **Opacity expansion ((D)GLV, ASW-SH)**

- Static scattering centers, Yukawa potential
- Expansion in opacity  $L/\lambda$   
( $N=1$ , interference between two centers default)
- Interference with vacuum radiation

- **Higher Twist (Guo, Wang, Majumder)**

- Medium characterised by higher twist matrix elements
- Radiation kernel similar to GLV
- Vacuum radiation in DGLAP evolution

DGLAP  
evolution

*Hard Probes 2010, M. van Leeuwen*

# Four formalisms

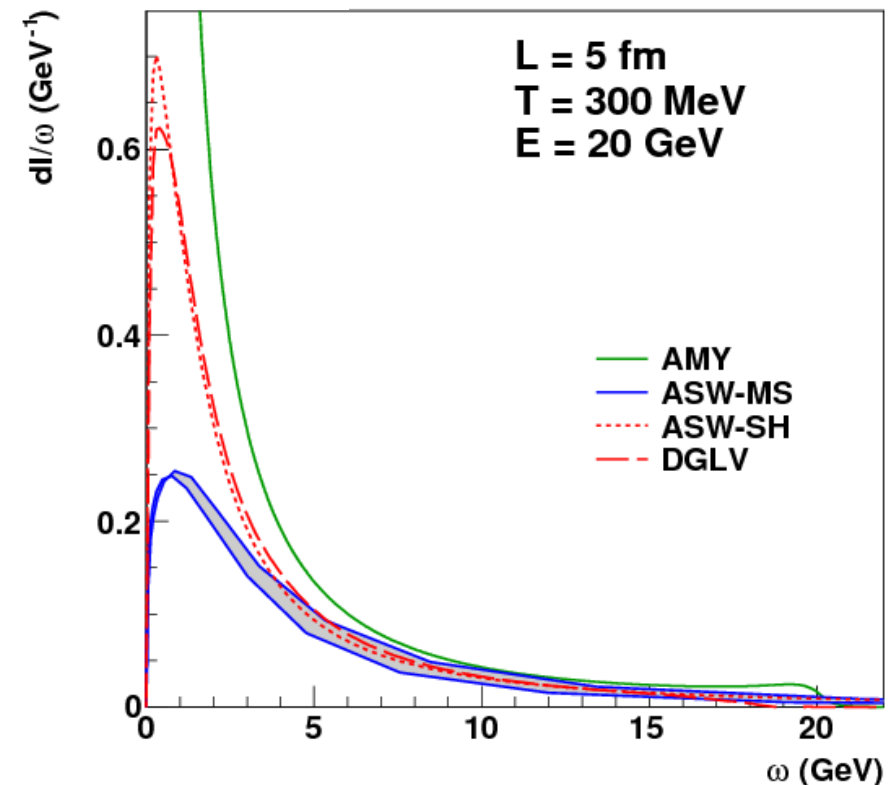
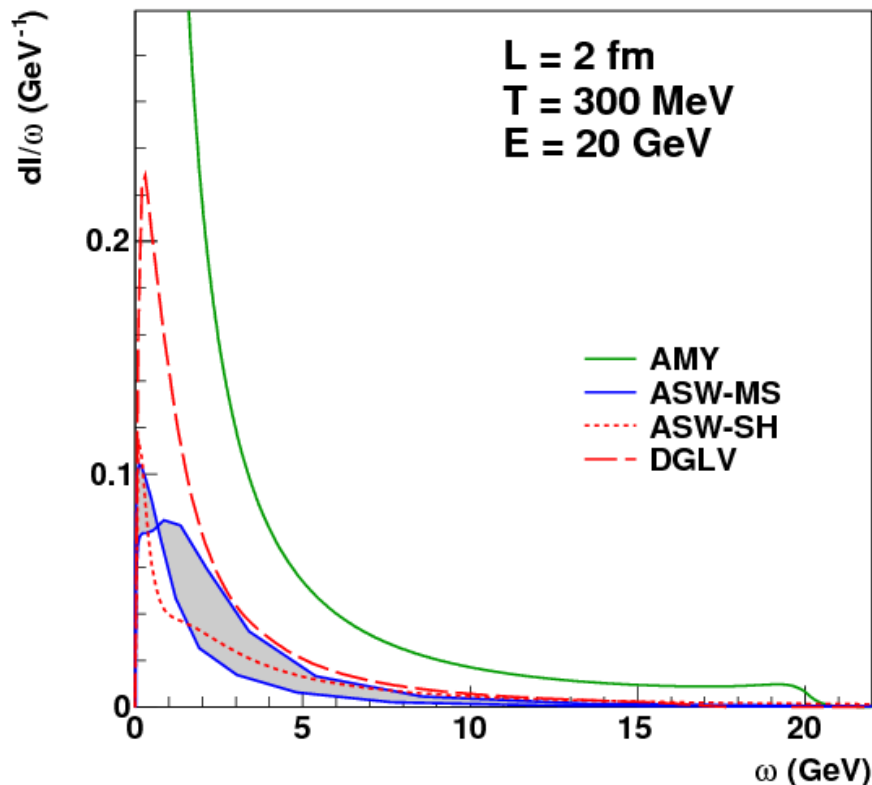
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  - Medium characterised by higher twist matrix elements
  - Radiation kernel similar to GLV
  - Vacuum radiation in DGLAP evolution

Today focus on these two models

# Single gluon spectrum

## fixed medium temperature

- Energy spectrum for 1 radiated gluon: for all models this is the starting point
- Clear hierarchy between models. Radiation AMY > GLV > ASW-MS
- Average number of emitted gluons:  $\langle N_g \rangle = \int d\omega \frac{dI}{d\omega}$ .

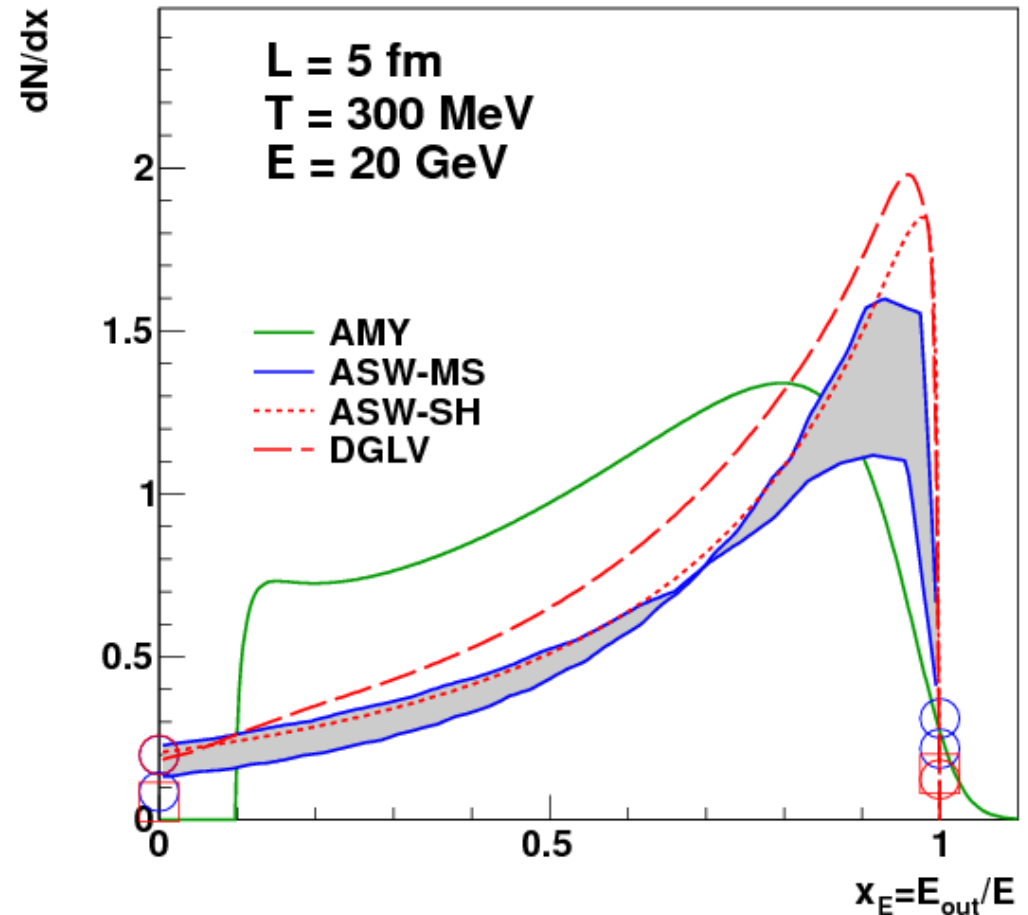


# Outgoing quark spectrum

Same temperature

Energy fraction of quark after leaving the medium.  
Fixed length, fixed temperature for all models

- $x_E = 1 - \Delta E/E$
- $x_E = 0$ : Absorbed quarks
- $x_E = 1$ : No energy loss



For fixed temperature:

- $\langle N_{\text{gluons}} \rangle$  larger for opacity expansion than multiple soft scattering approximation
- Suppression:  $\text{AMY} > \text{DGLV} > \text{ASW-MS}$

# Suppression in a brick vs qhat

Temperature  $T$  is the common variable in all models.

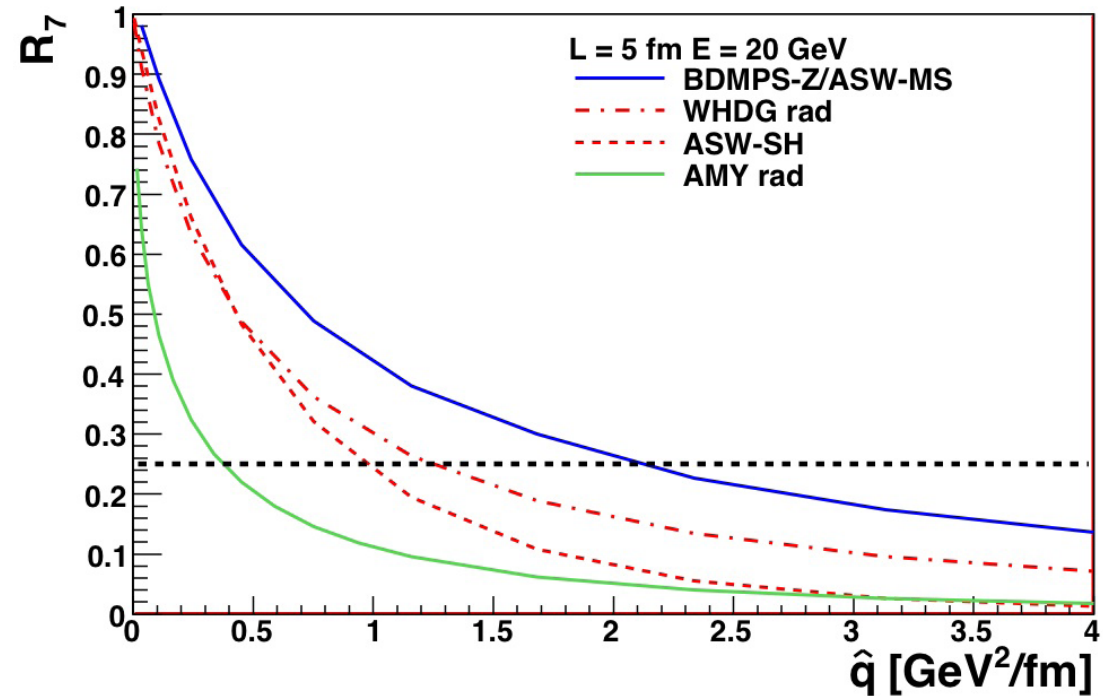
$R_7$  = approximation for  $R_{AA}$

$$R_n = \int_0^1 d\epsilon (1 - \epsilon)^{n-1} P(\epsilon)$$

$$\epsilon = \Delta E / E$$

$R_7 = 0.25$		$T$ (MeV)	$\hat{q}$ ( $\text{GeV}^2/\text{fm}$ )
$L = 2 \text{ fm}$	ASW-MS	1030	23.2
	WHDG	936	17.8
	ASW-SH	727	8.86
	AMY	480	2.7
$L = 5 \text{ fm}$	ASW-MS	434	2.11
	WHDG	358	1.23
	ASW-SH	326	0.95
	AMY	235	0.4

Gluon gas  $N_f = 0$



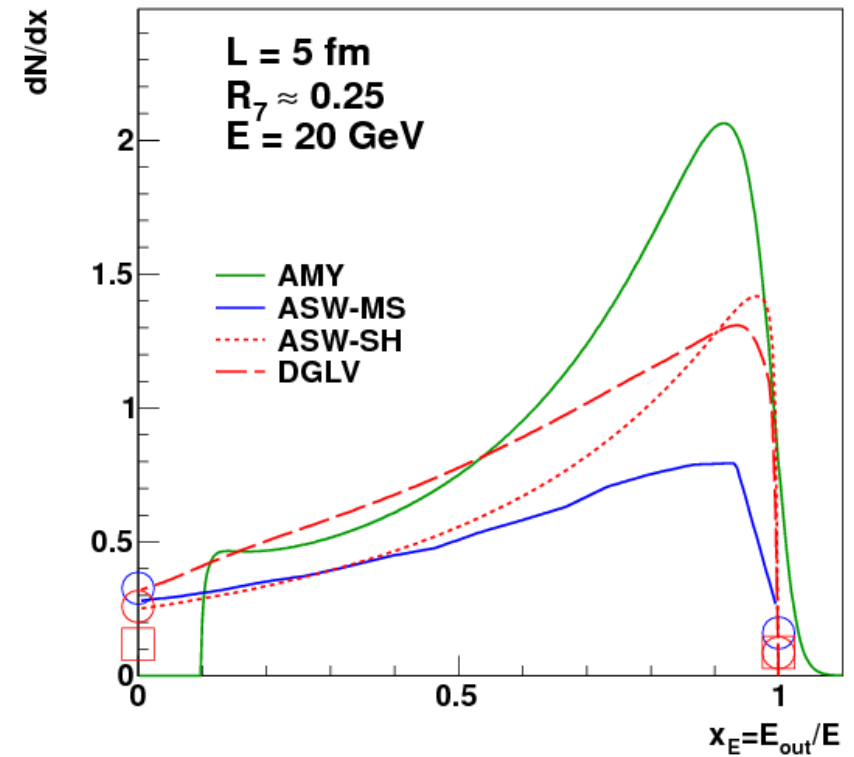
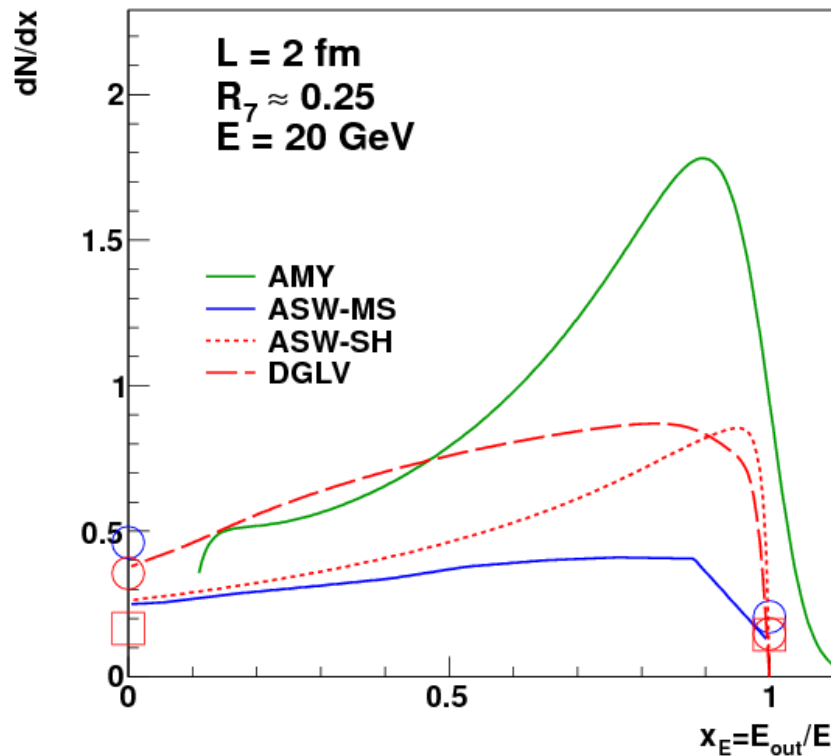
In simple geometry:

Large differences in medium density for  $R_7 = 0.25$



# Outgoing quark spectrum

Same suppression

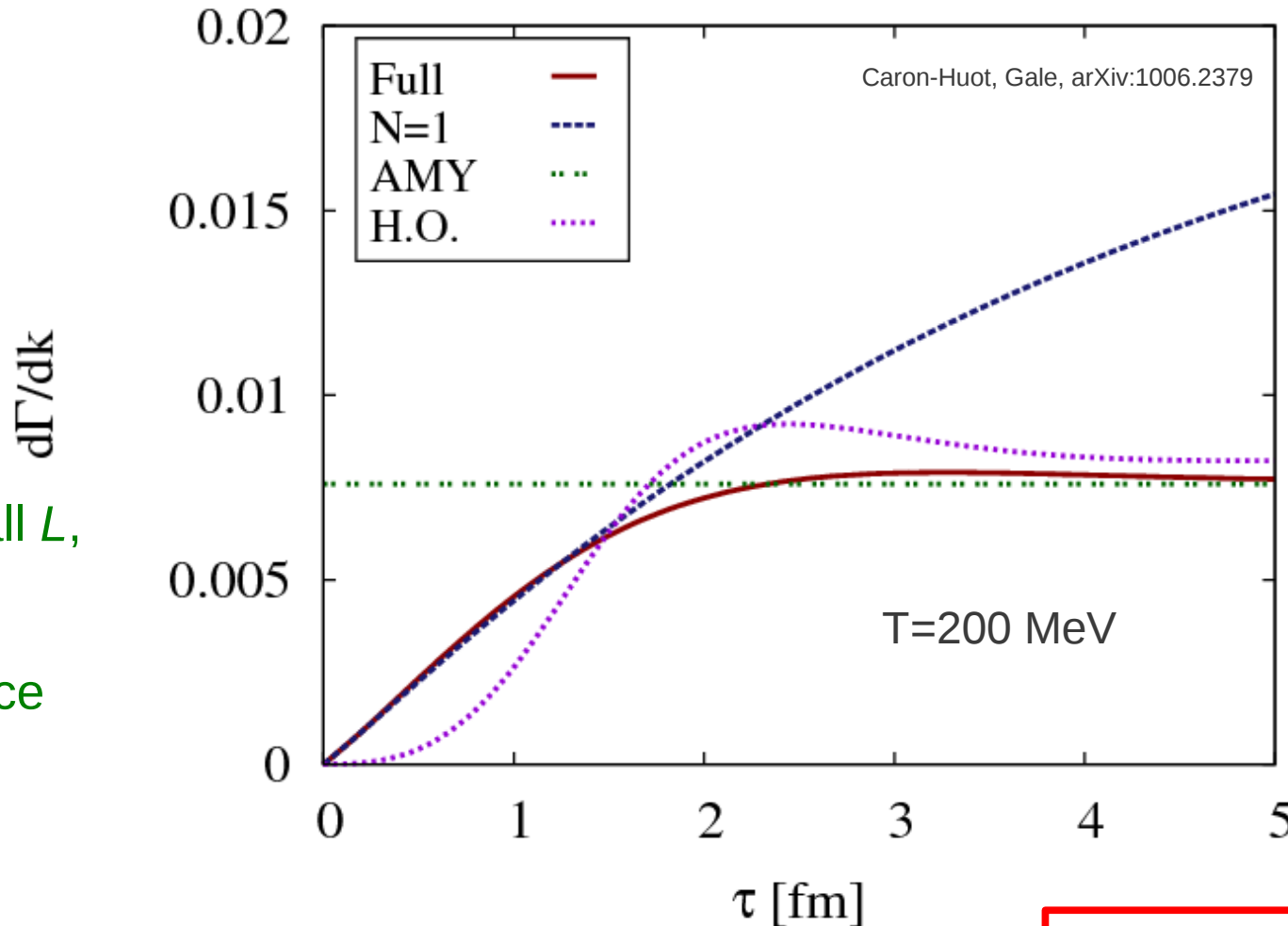


- Fixed suppression:  $N_{\text{gluons}}$  similar, but different mean energy loss

For detailed discussion, see  
brick report arXiv:1106.1106

# Validity of models

Gluon radiation rate vs  $\tau (=L)$



GLV N=1  
Too much radiation at large L (no interference between scattering centers)

Full = numerical solution of Zakharov path integral

AMY, small  $L$ , no  $L^2$ , no vacuum interference

H.O = ASW/BDMPS like (harmonic oscillator)  
Too little radiation at small  $L$  (ignores 'hard tail' of scatt potential)

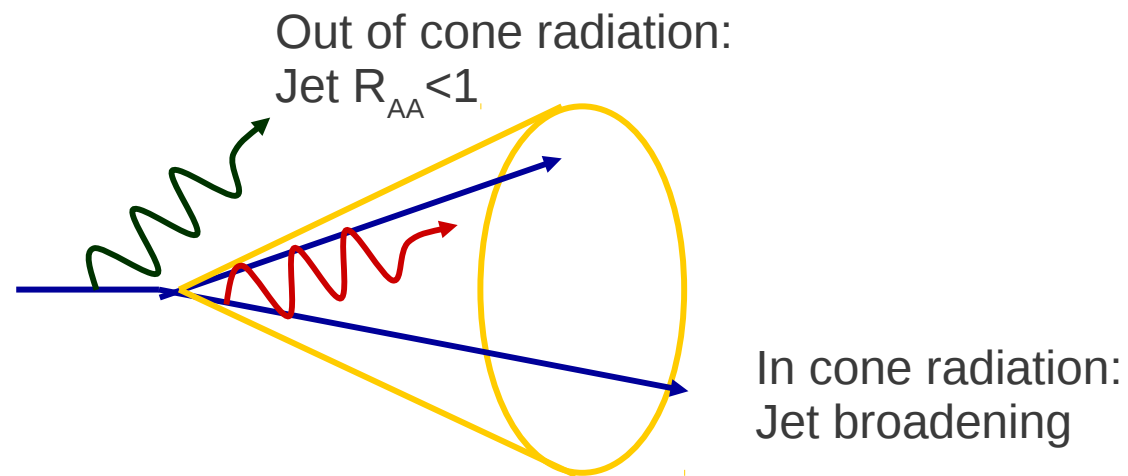
Each model is valid for different medium lengths

# Jets with ALICE in Pb-Pb collisions

# Jets in Heavy Ion Collisions

- Probes to study properties of medium
- Due to interaction of the jet with the medium, the jet is modified:

## Jet Quenching



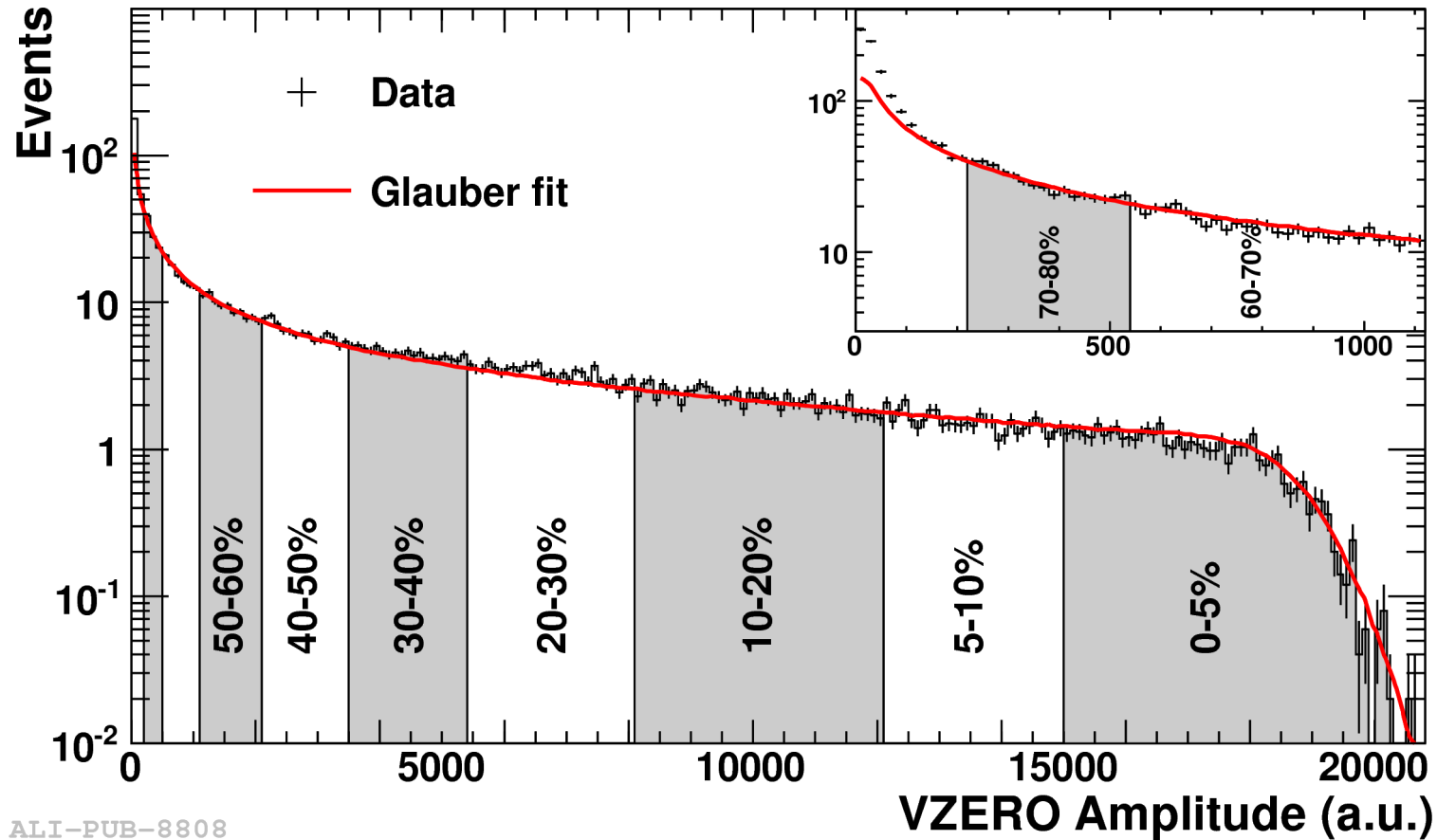
Experimental challenge in HI collisions:

**Separate jet signal from large soft background originating from bulk**

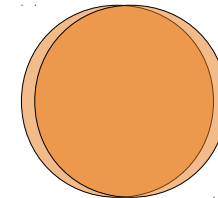
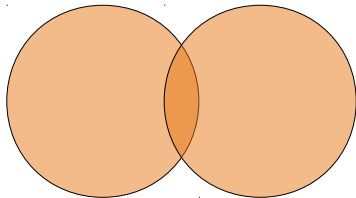
# Jet Reconstruction

- ALICE uses sequential recombination algorithms from FastJet package [Phys Lett B 641 (2006) 57]:
  - anti- $k_T$  for signal (stable area)
  - $k_T$  to estimate background density
  - Boost invariant  $p_T$  recombination scheme
  - Transverse momentum track cut-off  $p_T > 0.15 \text{ GeV}/c$
- Charged jet reconstruction with tracks reconstructed in tracking detectors:
  - High precision on particle level
  - Uniform  $\eta$ - $\phi$  acceptance
  - Neutral energy missing, eg.  $\pi^0$ ,  $n$ ,  $\gamma$

# Centrality of HI collisions



Peripheral collisions

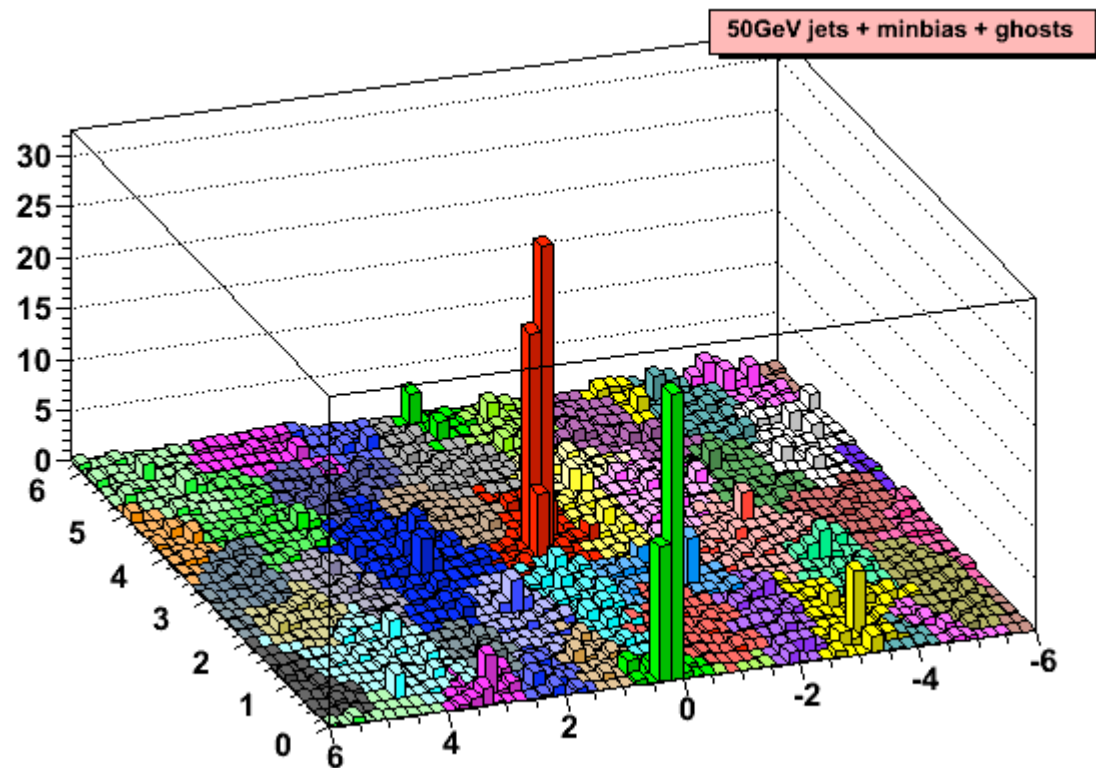


Central collisions

# Jets in HI events: background

- Jet sits on top of a soft background
- 2 step procedure to correct for UE contaminating the jet:

- 1) Background density  $\rho$ :  
 $k_T$  algorithm excluding the 2 leading clusters.
- 2) Background fluctuations:  
inhomogeneous structure of events.  
Quantified by embedding high  $p_T$  probes on top of the measured PbPb events.



# Jets in HI events: background

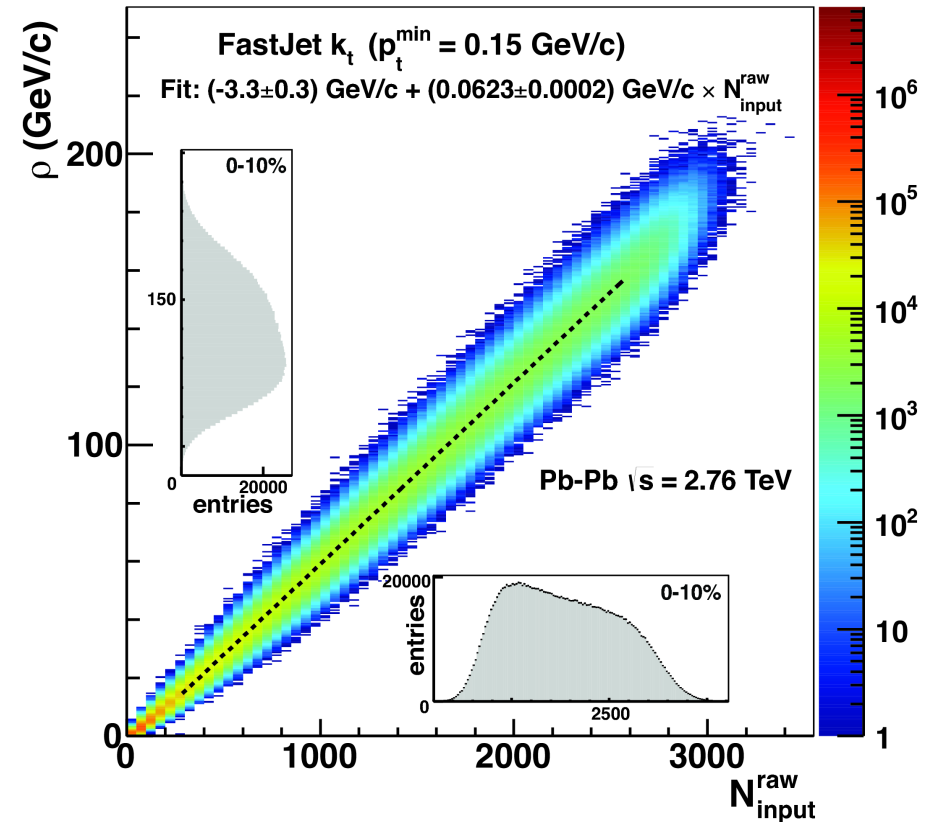
Event-by-event subtraction of average background momentum density  $\rho$ .

Background fluctuations quantified by embedding high  $p_T$  probes in Pb-Pb events

Width of fluctuations for jets with constituent  $p_T > 150$  MeV/c:

$$\sigma(\delta p_T, R=0.2) = 4.5 \text{ GeV}$$

$$\sigma(\delta p_T, R=0.3) = 7.1 \text{ GeV}$$

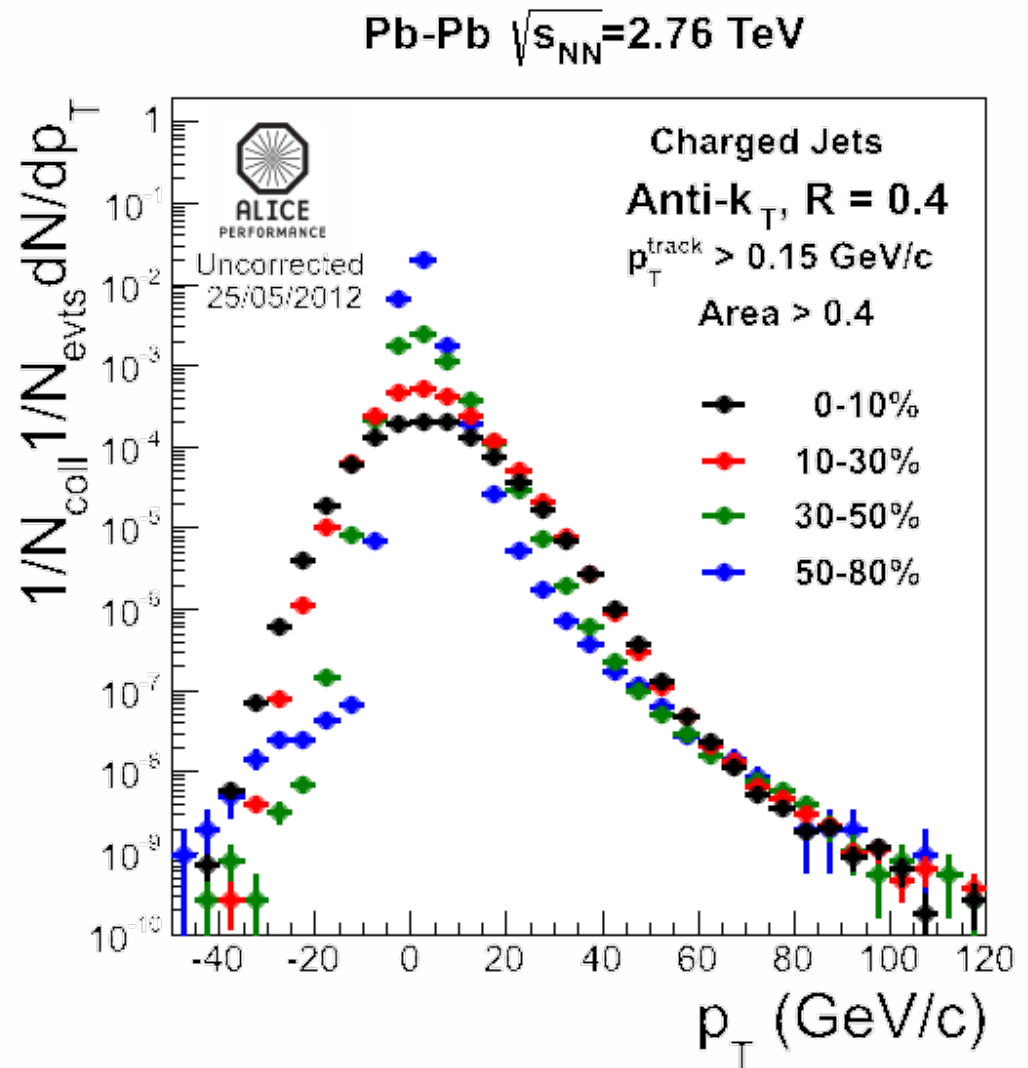


*JHEP, vol 1203, p 053 2012*



# Uncorrected Jet Spectrum

- Average background subtraction: event-by-event background density for central events  $\sim 140$  GeV/c/A
- Low  $p_T$  jets collect a lot of background energy and appear at very high  $p_T$  after clustering

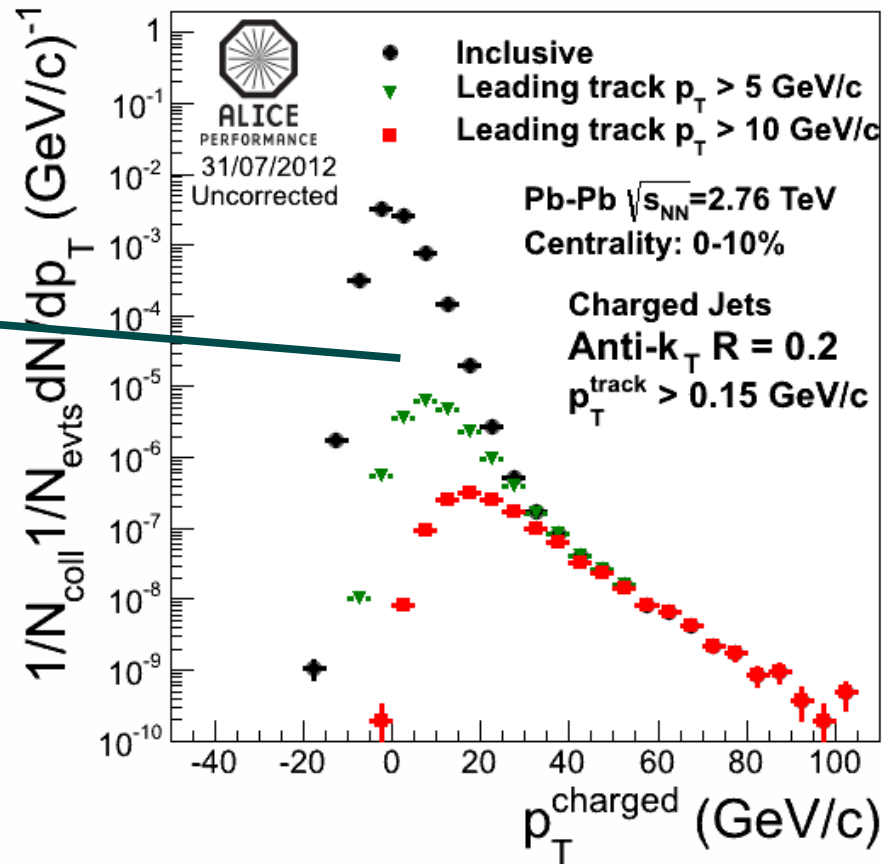


$p_{T,\text{track}} > 0.15$  GeV/c

# Jets in HI events: background

Combinatorial jets: clusters which do not originate from a hard process.  
Reduced by triggering jets with a leading track of  $p_T > 5$  and 10 GeV/c.

Combinatorial /  
fake jets



Jets reconstructed from charged particles with  $p_T > 150$  MeV/c.

# Background Fluctuations

- Background fluctuations estimated by studying the response of embedded high  $p_T$  probe in heavy ion event.
- Data driven approach to estimate influence of background fluctuations on jet reconstruction.
- We embed different kind of probes:
  - Random cones
  - Single tracks
  - Jets from full detector simulation pp @ 2.76 TeV
- Response is quantified by comparing the reconstructed jet to the embedded probe:

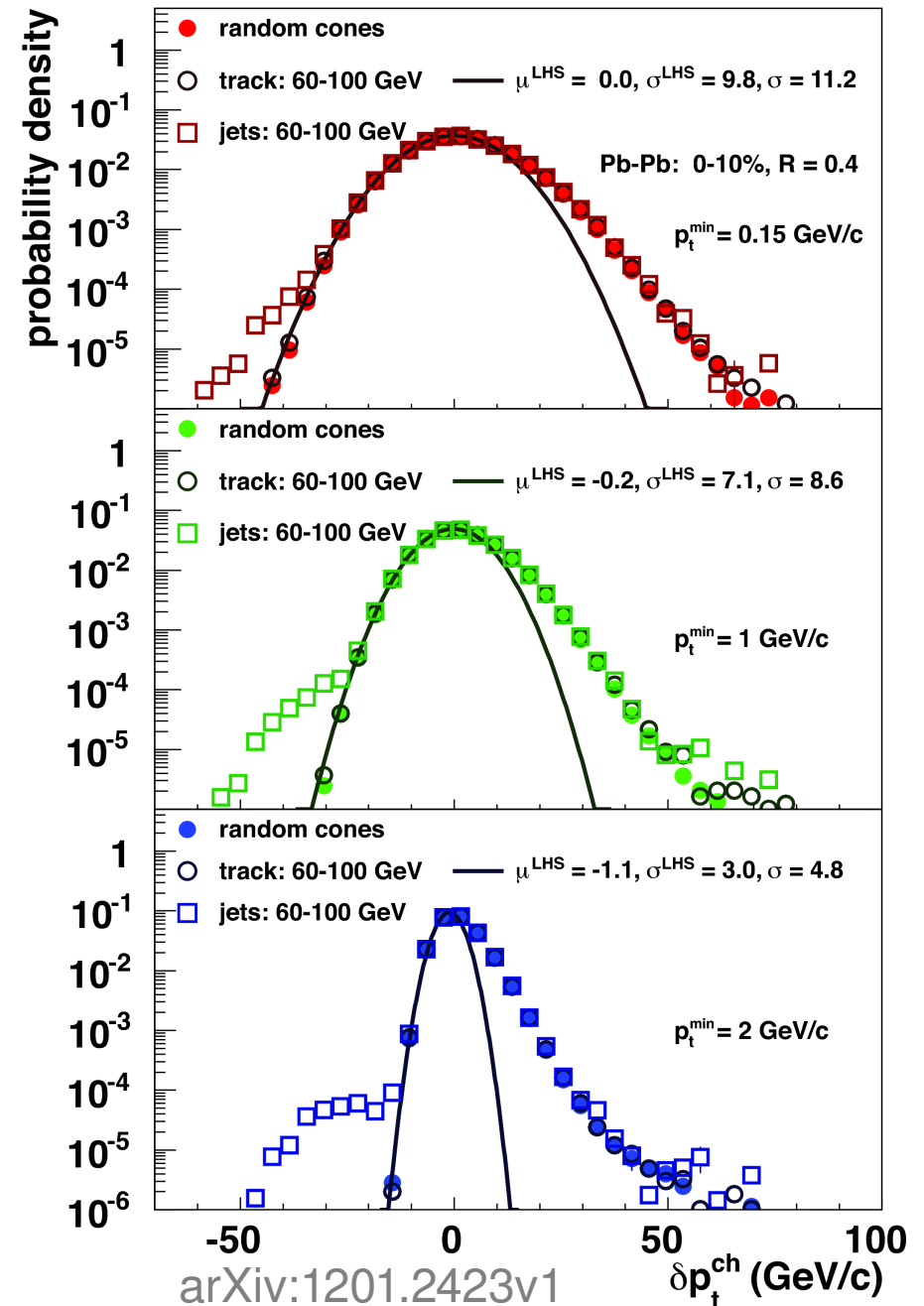
$$\delta_{p_T} = p_{T,jet}^{rec} - \rho A - p_T^{probe}$$

# Background Fluctuations

## Comparison of Probes

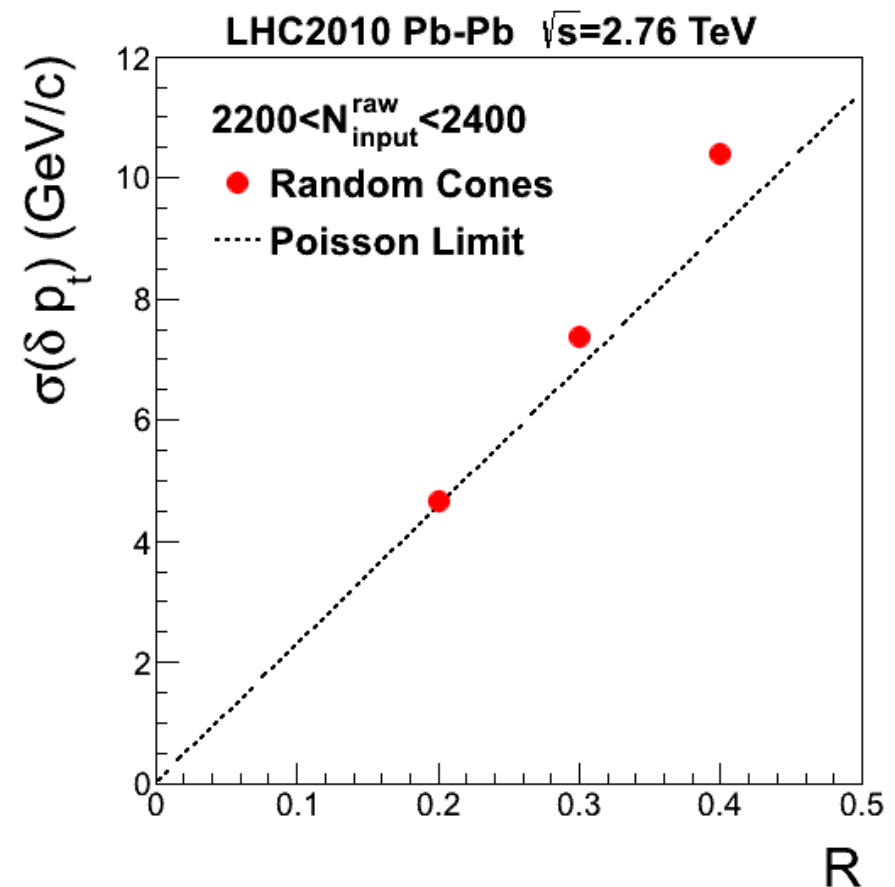
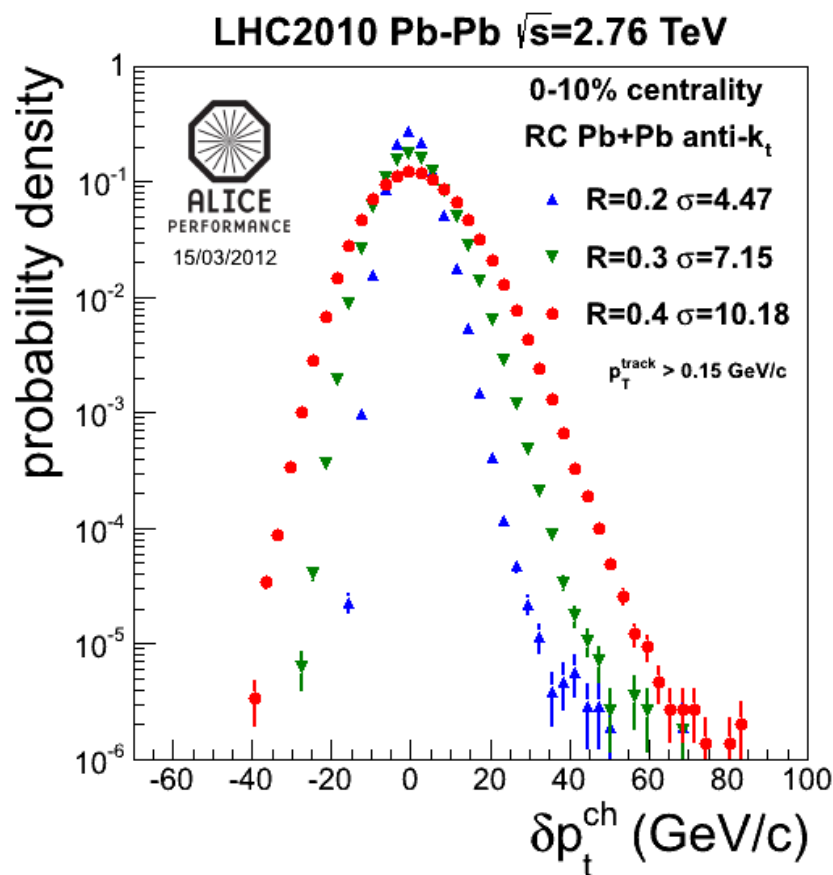
Random Cones  
Single Tracks  
Pythia jets

- No dependence on fragmentation pattern observed
  - Small back-reaction effect
- Fluctuations reduced by increasing minimum particle  $p_T$
- High  $p_T$  tail same shape as jet spectrum
  - Challenging for unfolding



# Background Fluctuations

## Comparison of jet radii



Reduced background fluctuation for smaller jet areas

Measured  $\sigma(\delta p_T)$  larger than naive expectation from only statistical fluctuations

# Unfolding the background

- Need to **unfold** measured jet spectrum to obtain 'real' jet spectrum (**Truth**)
- **Refolded** = unfolded jet spectrum smeared with background fluctuations

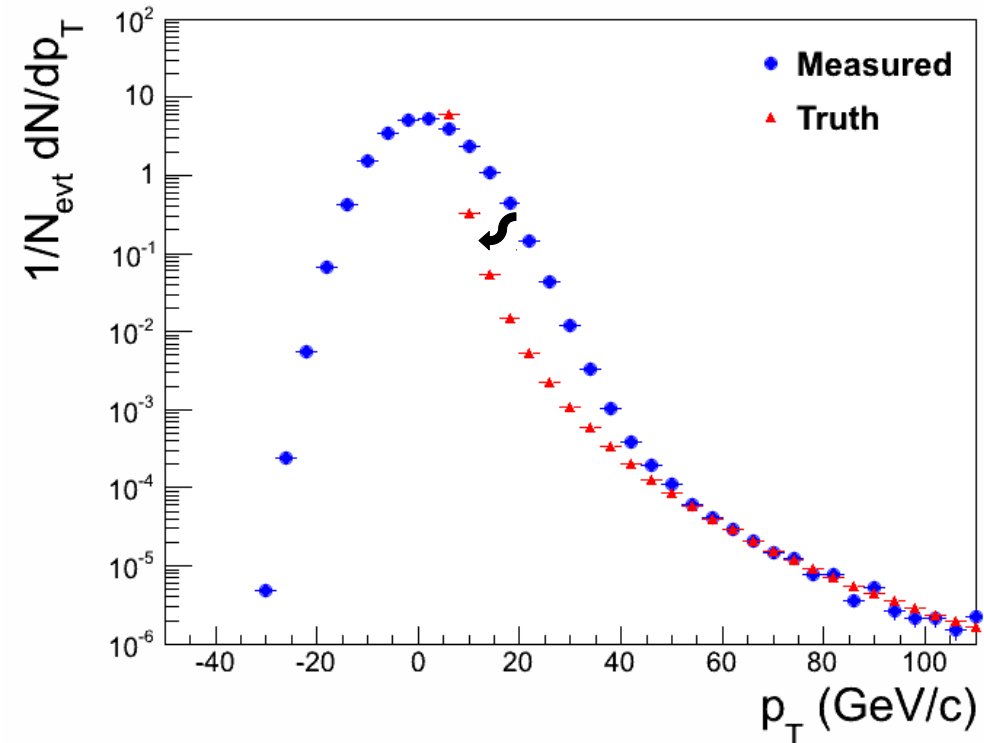
Assume:

$$\left. \frac{dN}{dp_T} \right|_{meas} = P(\delta p_T) \otimes \left. \frac{dN}{dp_T} \right|_{jet}$$

Unfolding done with  $\chi^2$  minimization

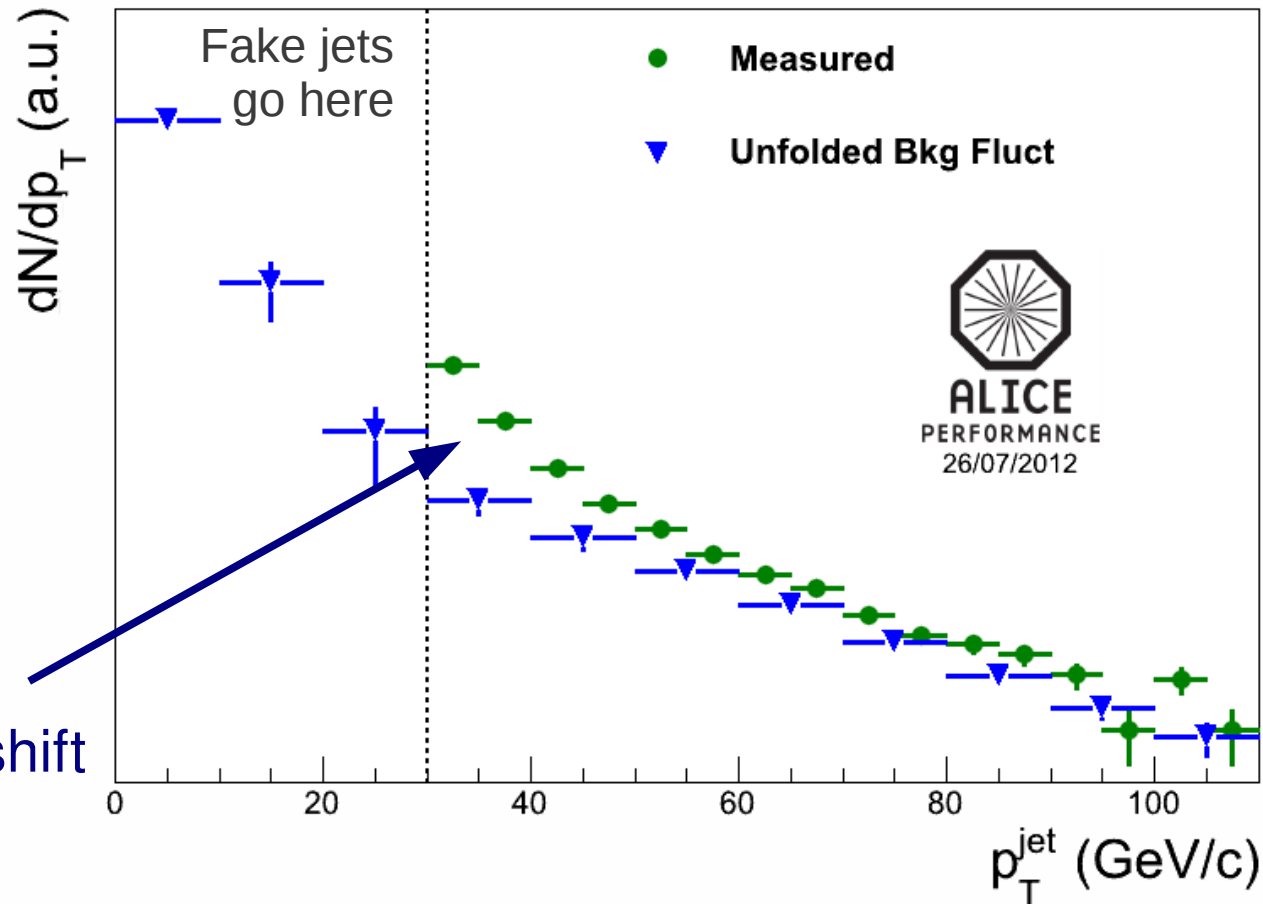
$$\chi^2 = \sum_{refolded} \left( \frac{y_{refolded} - y_{measured}}{\sigma_{measured}} \right)^2 + \beta \sum_{unfolded} \left( \frac{d^2 \log y_{unfolded}}{d \log p_t^2} \right)^2$$

$\chi^2$ -term
Regularization/penalty



# Background and detector corrections

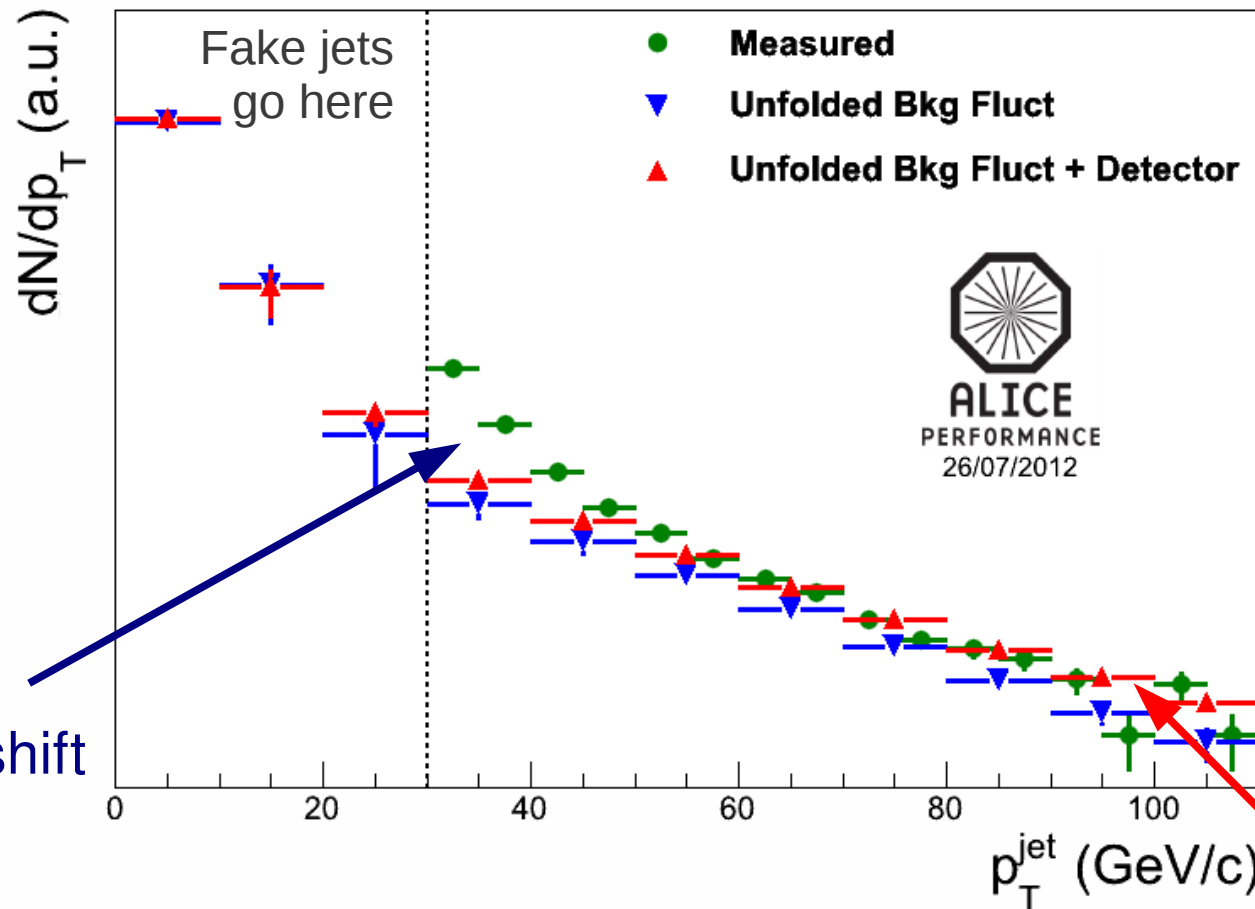
Raw jet spectra need to be corrected for background fluctuations



Background fluctuations shift low  $p_T$  jets to high  $p_T$

# Background and detector corrections

Raw jet spectra need to be corrected for background fluctuations and detector effects.

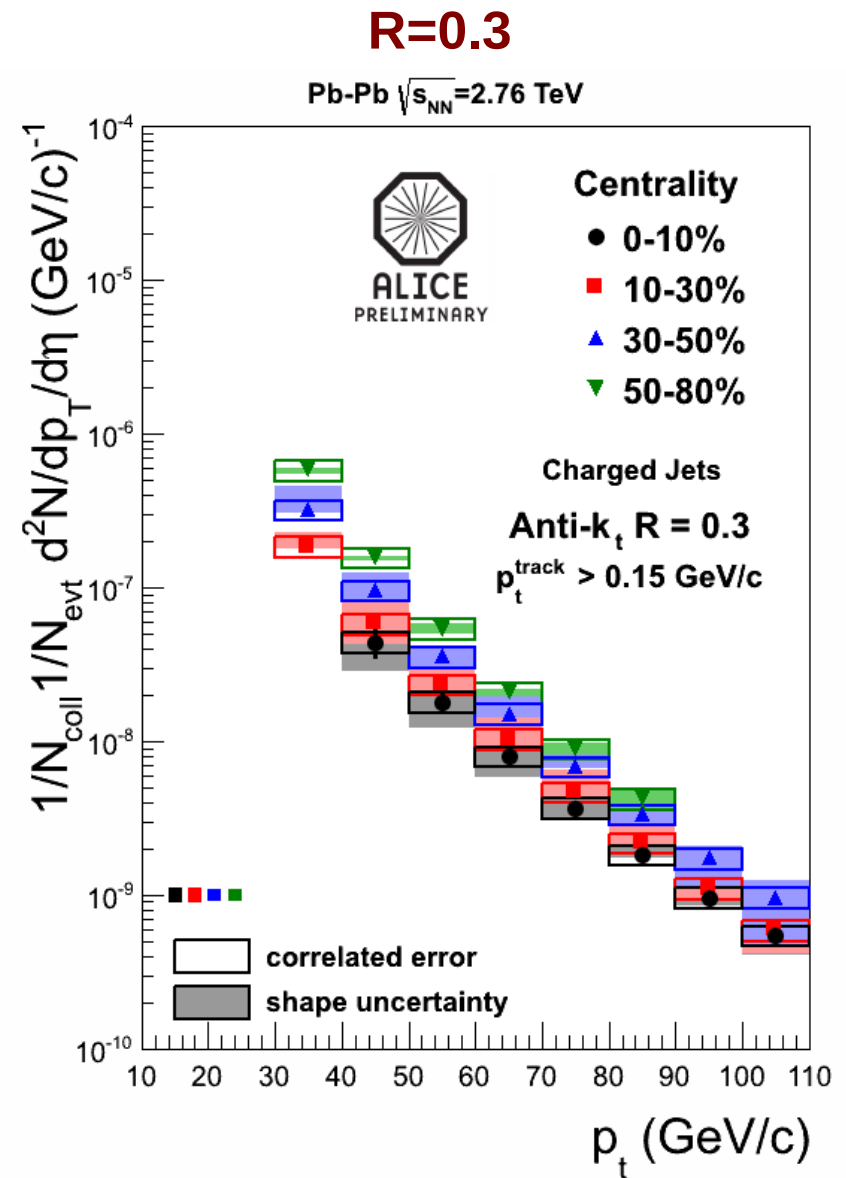
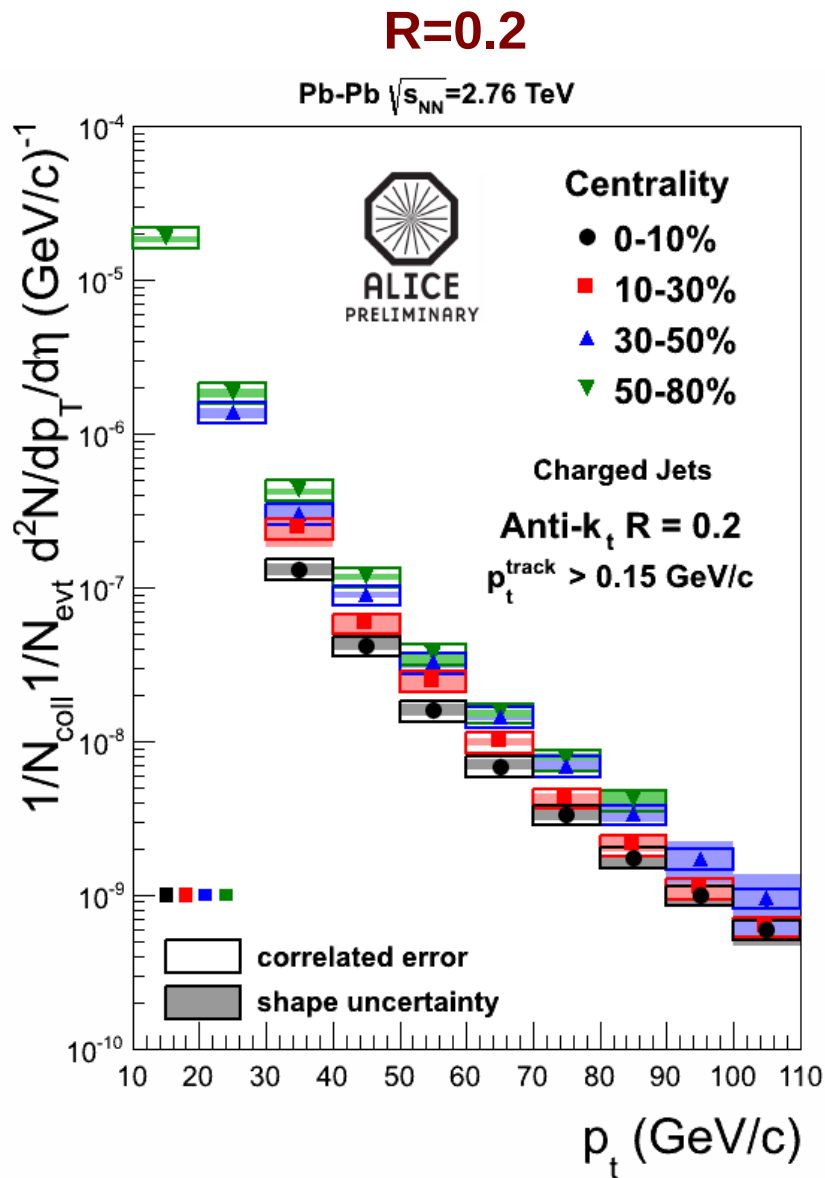


Background fluctuations shift low  $p_T$  jets to high  $p_T$

Detector effects shift jets to lower  $p_T$



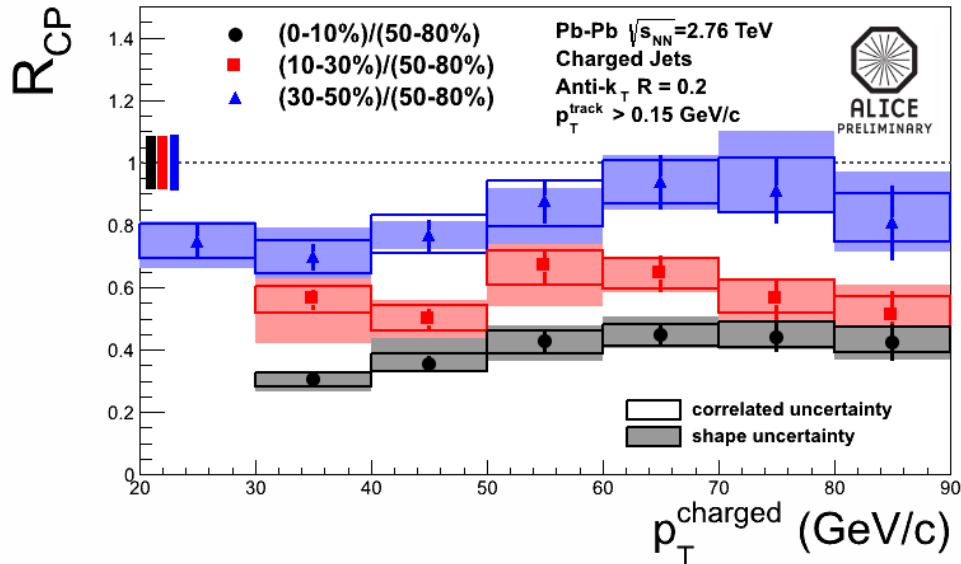
# Pb-Pb Jet Spectrum



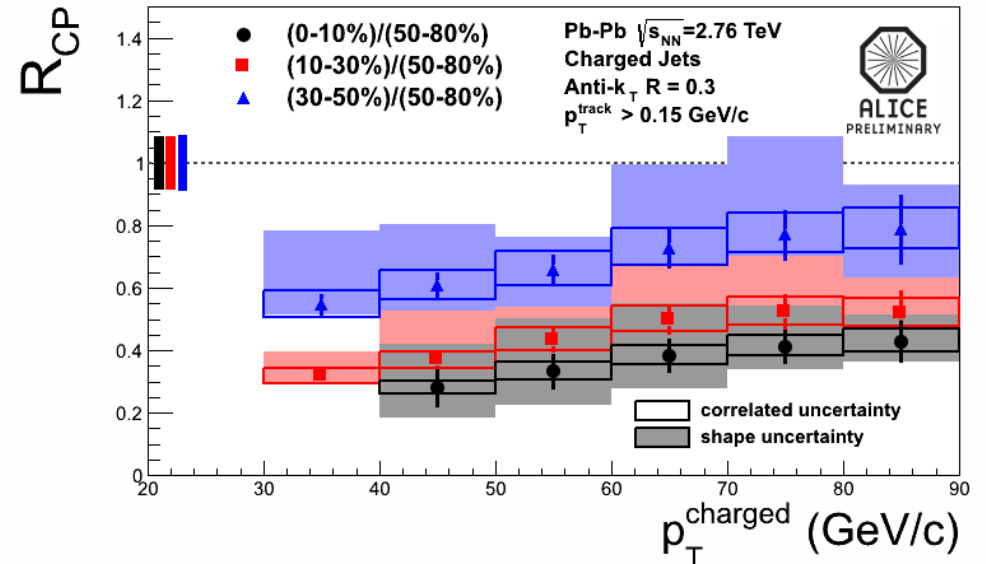
Jet spectra have been measured for 2 cone radii and 4 centrality bins

# Jet $R_{CP}$

**R=0.2**



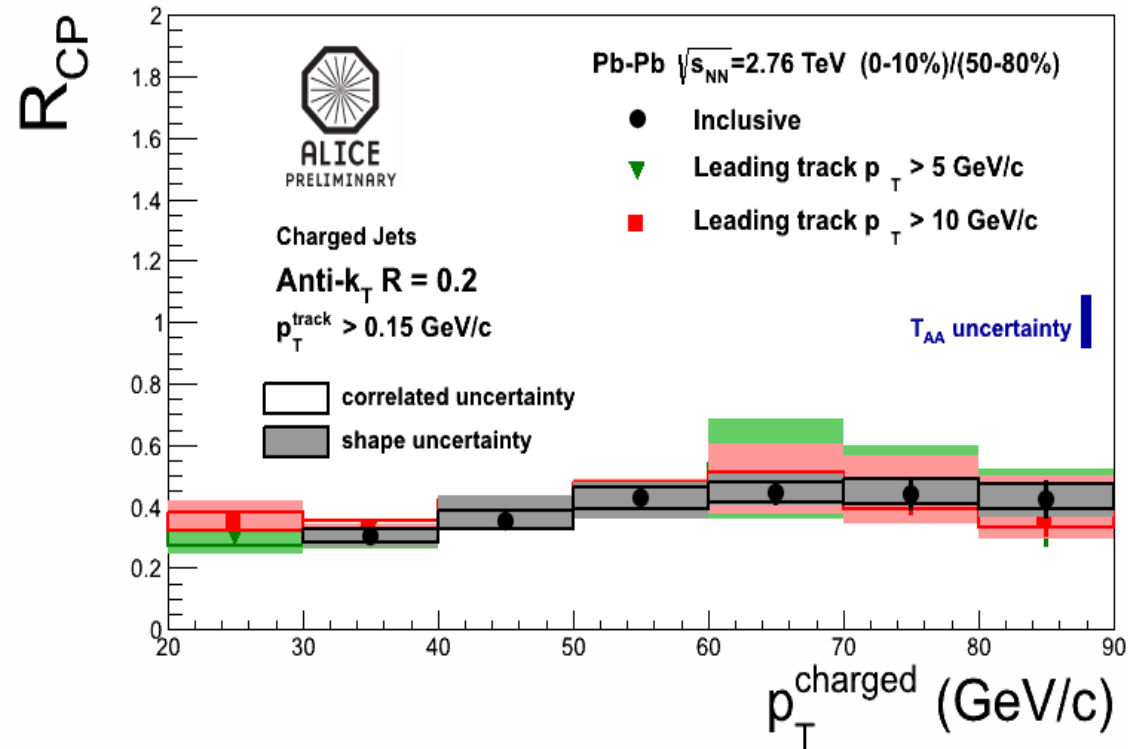
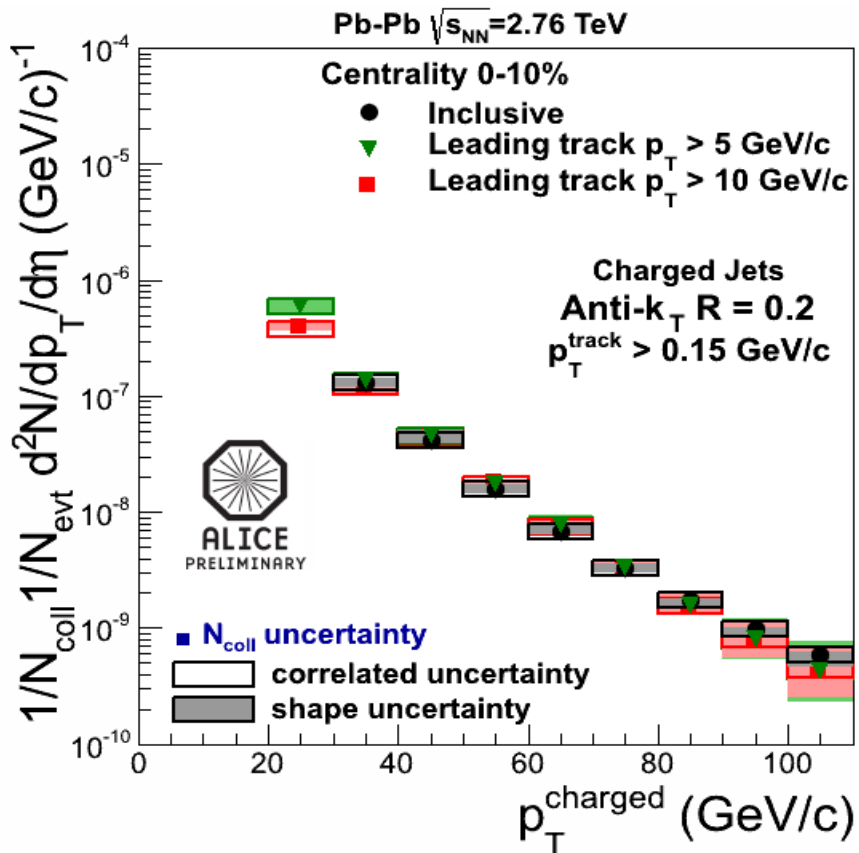
**R=0.3**



Strong suppression for jets  
No strong  $p_T$  dependence  
Similar suppression for jet radii  
 $R=0.2$  and  $R=0.3$

Central events jet  $R_{CP} \sim 0.5$   
Peripheral closer to 1

# Jet Suppression

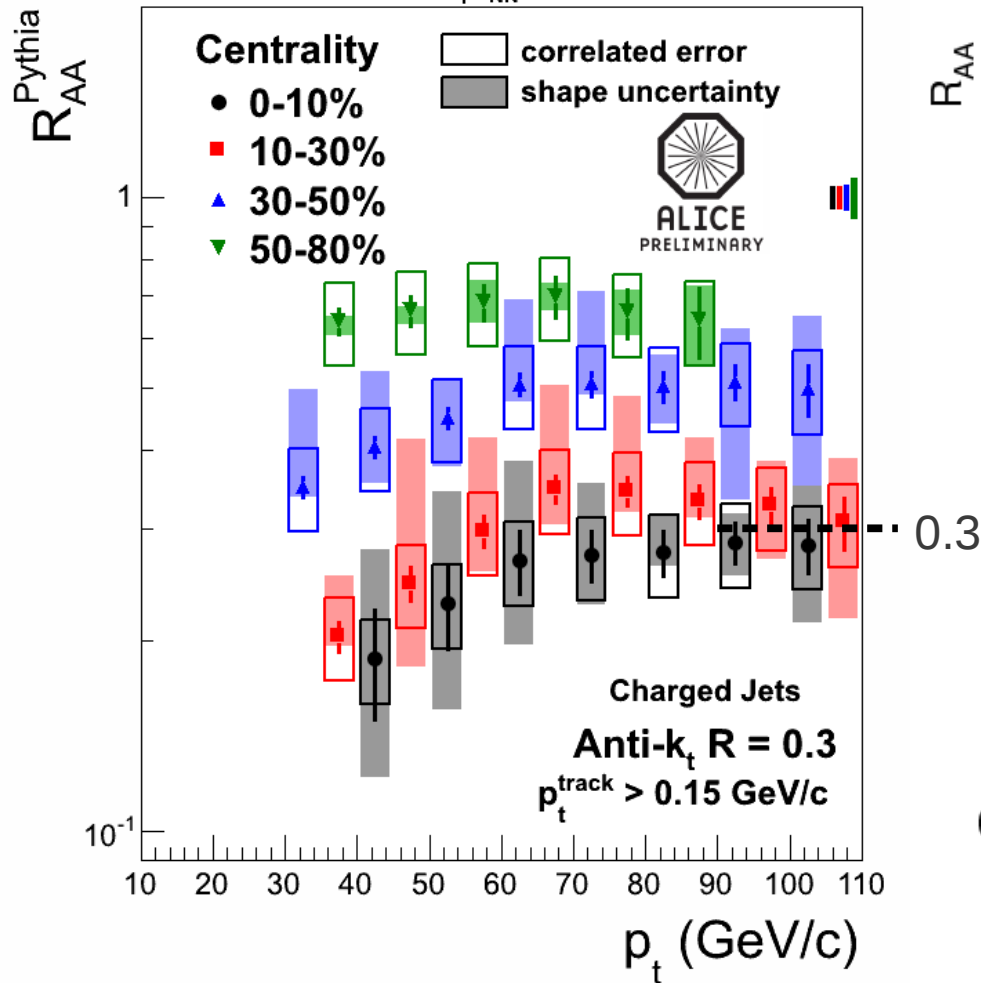


- Leading track requirement  $\rightarrow$  fragmentation bias at low  $p_T$   
 $\rightarrow$  potentially modified by jet quenching

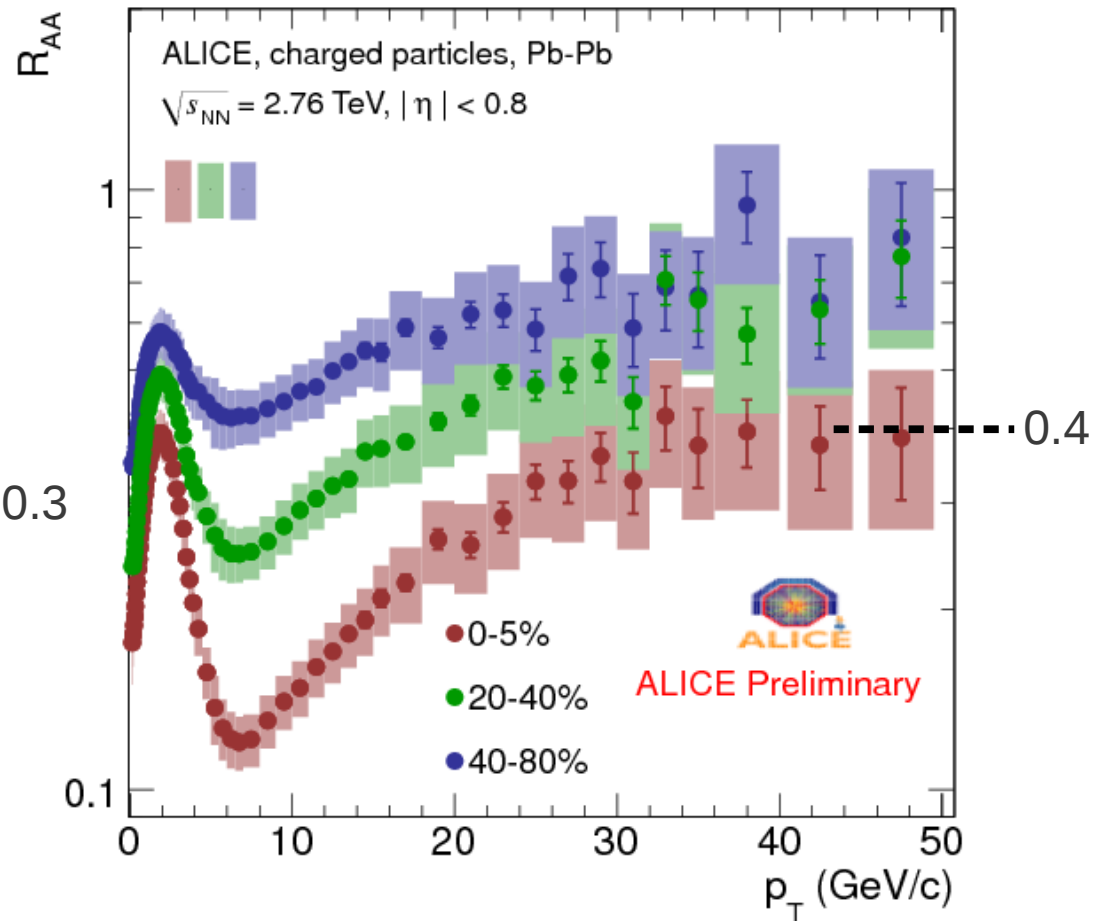
Fragmentation bias the same for central and peripheral events.

# Jet $R_{AA}$ vs Hadron $R_{AA}$

Jet  $R_{AA}^{Pythia} R=0.3$   
 Pb-Pb  $\sqrt{s_{NN}}=2.76$  TeV



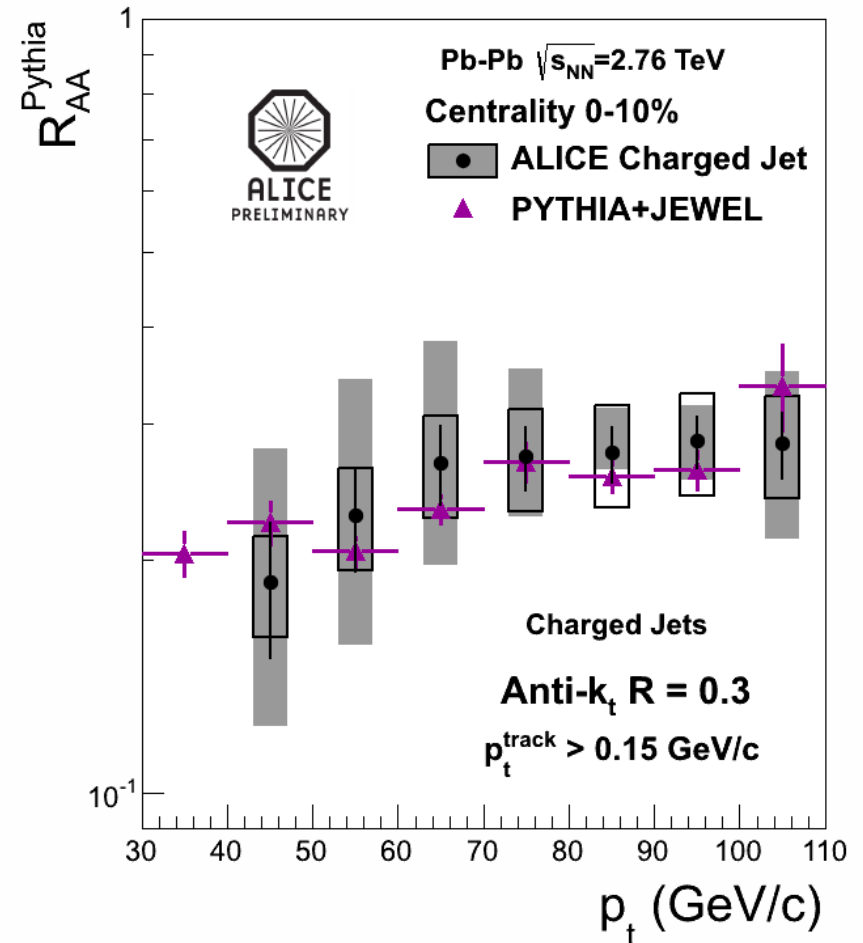
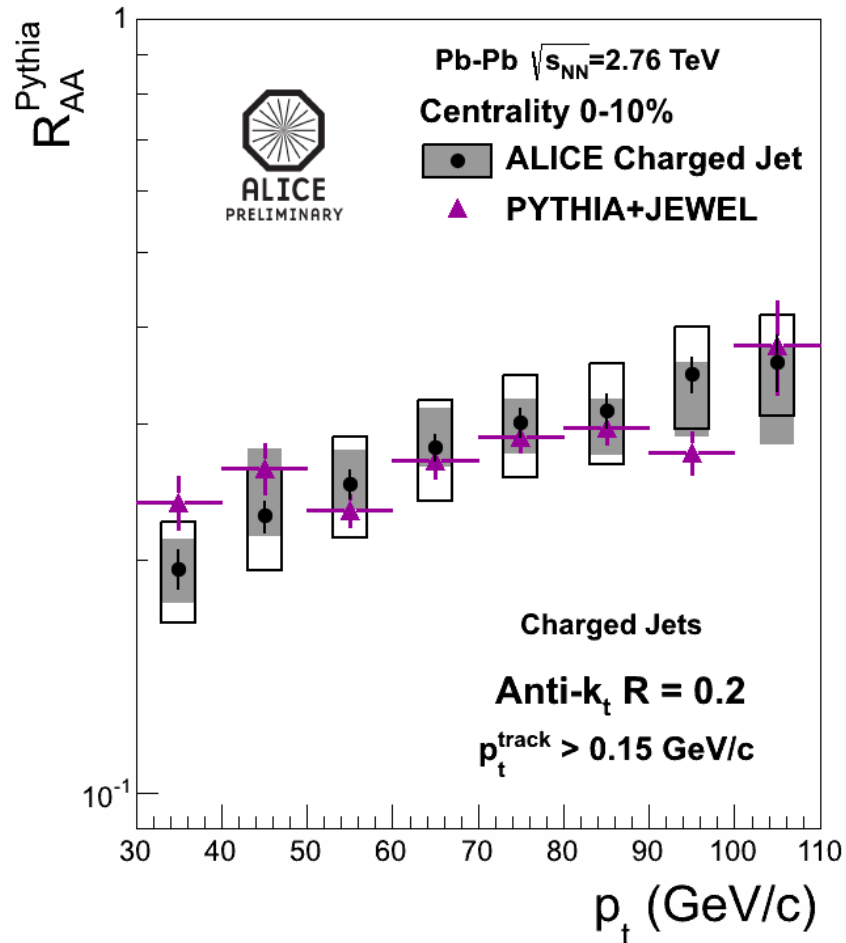
Charged Particle  $R_{AA}$



Jet  $R_{AA}^{Pythia} \leq$  Hadron  $R_{AA}$

# Model Comparison

## Jet $R_{AA}$ : ALICE vs JEWEL



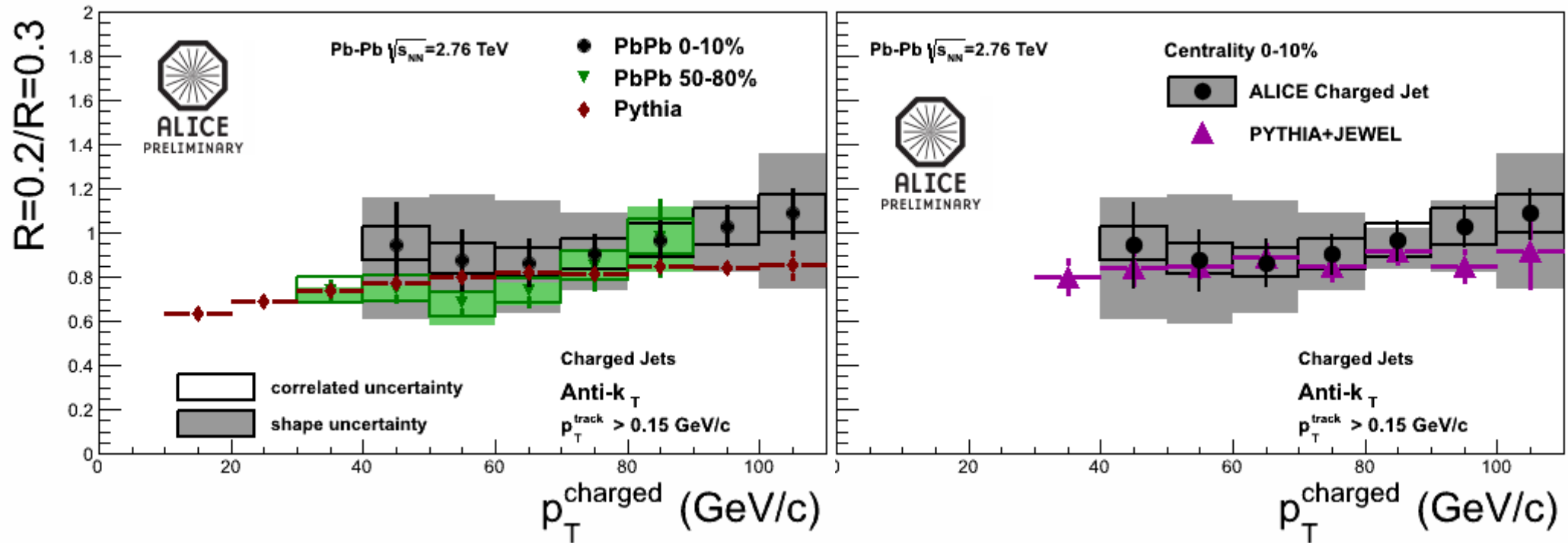
JEWEL (radiative + elastic energy loss MC) reproduces

→ Hadron  $R_{AA}$  (Zapp, Krauss, Wiedemann arXiv:1111.6838)

→ Charged jet  $R_{AA}$  for  $R=0.2$  and  $R=0.3$  JEWEL jet results: private communication

# Ratio of jet cross sections

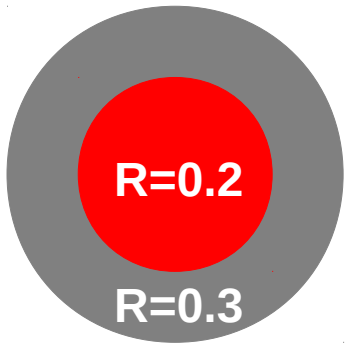
## $R=0.2/R=0.3$



$\sigma(R=0.2)/\sigma(R=0.3)$  consistent with vacuum jets  
for **peripheral** and **central** collisions  
→ no sign of jet broadening

Good agreement with energy loss MC JEWEL.

JEWEL: Zapp, Krauss, Wiedemann arXiv:1111.6838



# Summary

- TECHQM Brick: differences between formalisms identified. Not physics but approximations
- Jets with ALICE
  - Strong jet suppression in central events
  - No signs of modified jet structure observed in ratio of jet cross section  $R=0.2/R=0.3$
  - Jet  $R_{AA} \leq$  Hadron  $R_{AA}$

backup



# Track Selection

## Requirements for jet analysis

- Uniform acceptance in eta and phi
- **Avoid outliers** (tracks with low  $p_T$  generated which are reconstructed at very high  $p_T$ )

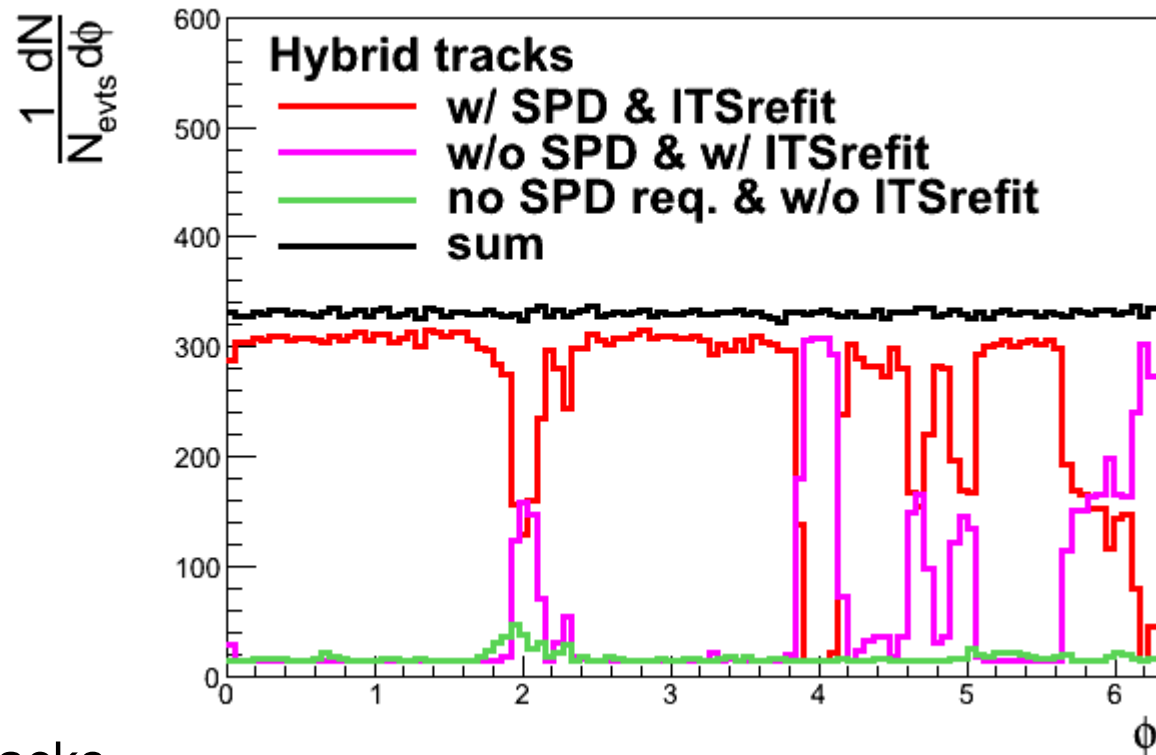
**Jet clustering**

- **Track momentum resolution**
- **High tracking efficiency**

**Jet energy resolution**

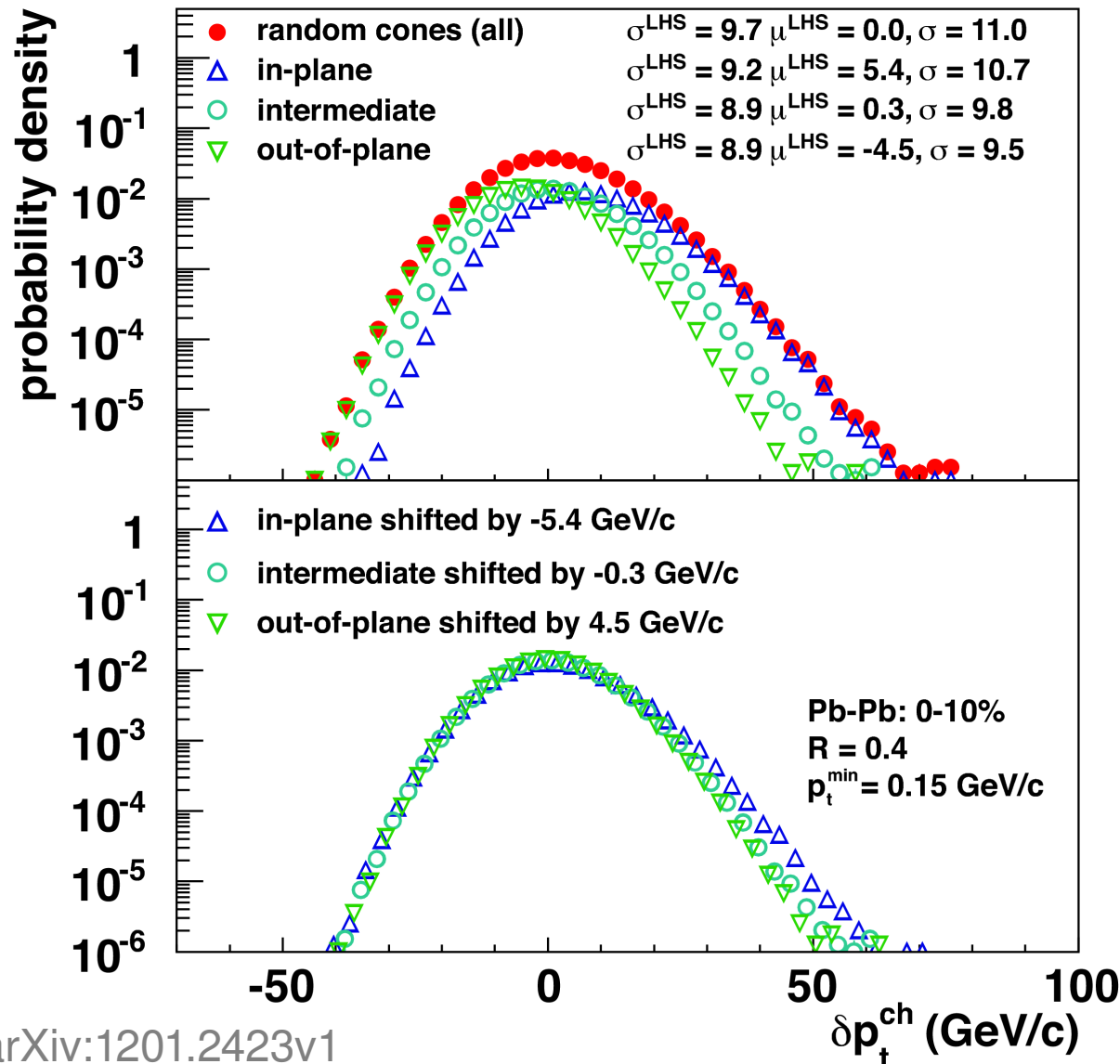
Strategy for track selection:  
Use the best available → hybrid tracks

# Hybrid Tracks



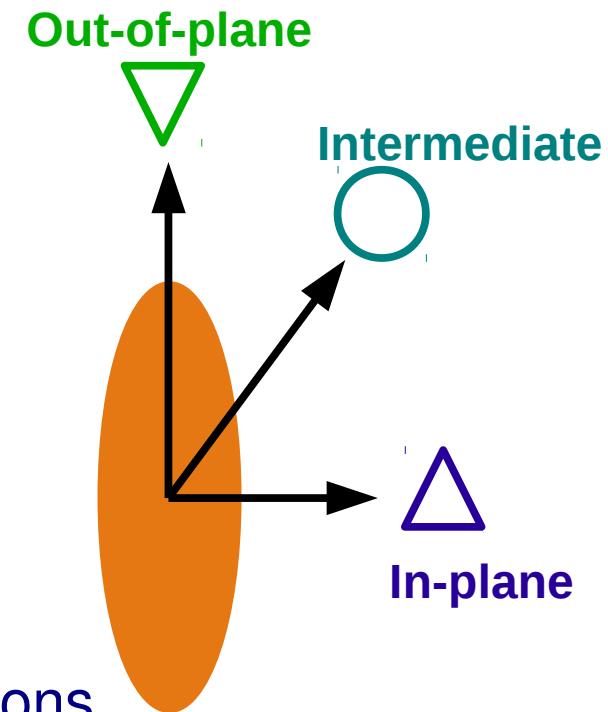
- Hybrid tracks
  - Standard global tracks: w/SPD & ITSrefit (82%)
  - Constrained global tracks: w/o SPD || w/o ITSrefit (12 + 6%)
- Constrained tracks fill the gaps in phi caused by missing SPD layers. Constrained to primary vertex to improve momentum resolution
- Tracking efficiency: 80-85% at high  $p_T$ . (~70% for global standard tracks)

# Fluctuations vs reaction plane



Goal: estimate influence of region-to-region fluctuations of correlated background.

~5 GeV shift for in- and out-of-plane:  $\propto v_2 \rho$



arXiv:1201.2423v1

Collective effects ( $v_n$ ) broaden background fluctuations

# Suppression Factor

in a brick

- Hadron spectrum if each parton loses  $\epsilon$  energy:

$$\frac{dN}{dp_t} = \frac{1}{[(1-\epsilon)p_t]^n} \frac{dp_t}{dp'_t} = \frac{1}{(1-\epsilon)^{n-1} p_t^n}$$

$$p'_t = (1-\epsilon) p_t$$

$$\epsilon = \Delta E / E$$

Weighted average energy loss:

$$R_n = \int_0^1 d\epsilon (1-\epsilon)^{n-1} P(\epsilon)$$

For RHIC:  $n=7$

- $R_7$  approximation for  $R_{AA}$

# Model input parameters

- Multiple soft scattering approximation (ASW-MS):

$$N_{gluon} = \int d\omega \frac{dI}{d\omega}(\omega_c, R) = \int d\omega \frac{dI}{d\omega}(\hat{q}, L)$$

“Medium density”

- Opacity expansion (GLV, etc.):

$$N_{gluon} = \frac{L}{\lambda} \int d\omega \frac{dI}{d\omega}(\mu, L)$$

#scattering centers

Debye screening mass

- No  $\hat{q}$  for opacity expansions.

$$\hat{q} = \frac{\langle q_{\perp}^2 \rangle}{\lambda} \sim \frac{\mu^2}{\lambda}$$

- In evolving medium: effective path averaged input parameters.**  
**Common variable between models: medium temperature**

# Energy loss models in realistic geometry

# Scattering rate in (D)GLV

$$x \frac{dN_g}{dx} = \frac{C_R C_g g^2}{2\pi^3} \int \frac{d^2 \mathbf{q}}{(2\pi)^2} d^2 \mathbf{k} dz C(\mathbf{q}, z) \times \mathcal{K}(\mathbf{k}, \mathbf{q}, z)$$

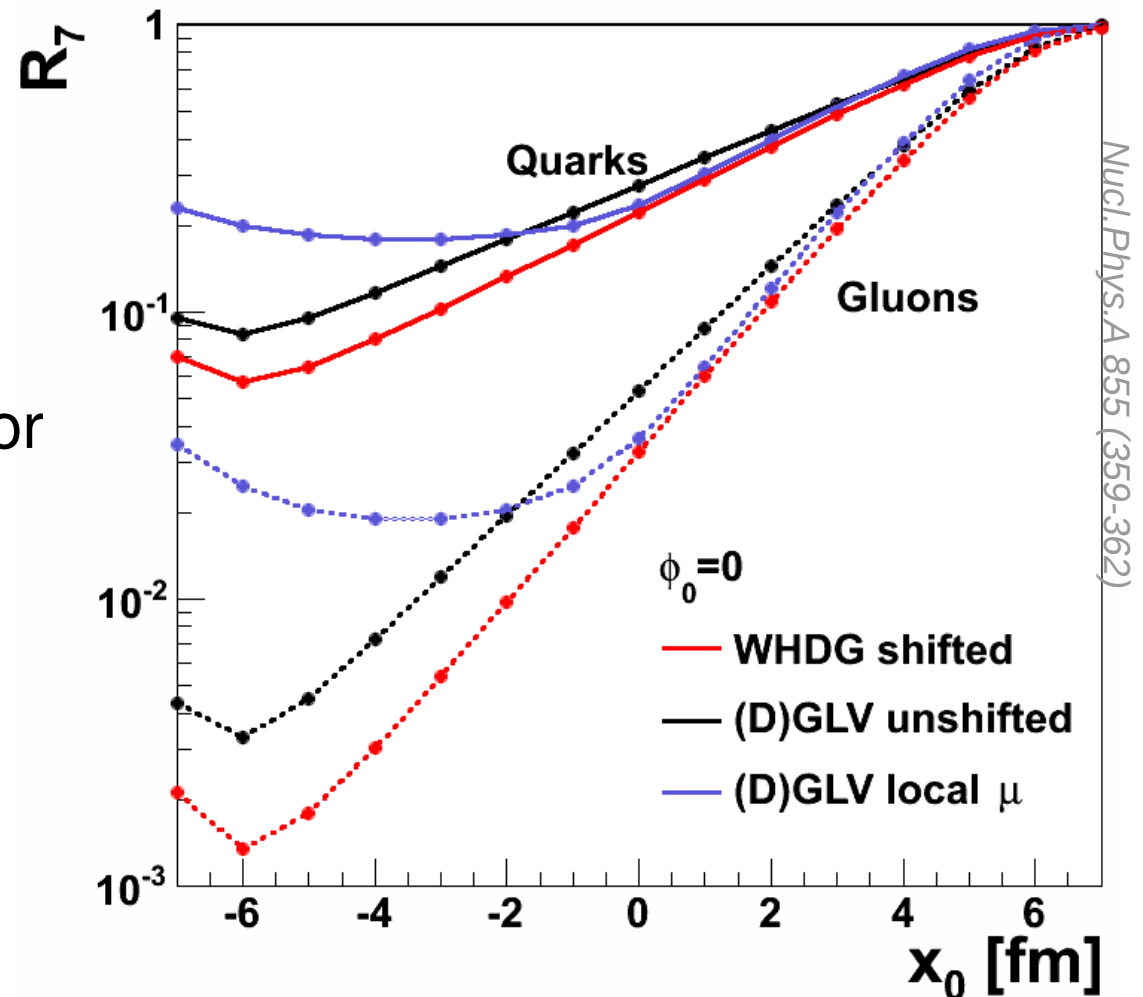
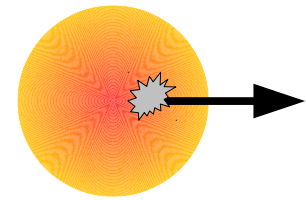
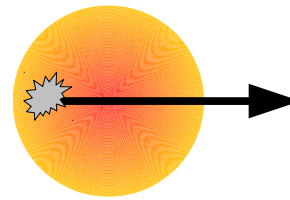
$$C(\mathbf{q}, z)^{GLV} = \frac{(2\pi)^2}{\lambda C_R} \frac{1}{\pi} \frac{\mu^2}{(q^2 + \mu^2)^2} \rho(z) \longrightarrow \text{Depends on medium properties}$$

Reference: S. Caron-Huot & C. Gale,  
arXiv:1006.2379

- Normalized Yukawa potential and  $\rho(z)$
- $\rho(z)$  is the probability to have a scattering at position  $z$   
→  $\rho/\lambda = \text{scattering rate per unit length}$
- Explore effect of constant  $C(\mathbf{q})$  (uniform medium, GLV default) vs position-dependent  $C(\mathbf{q})$  (non-uniform medium)

# Medium as seen by parton

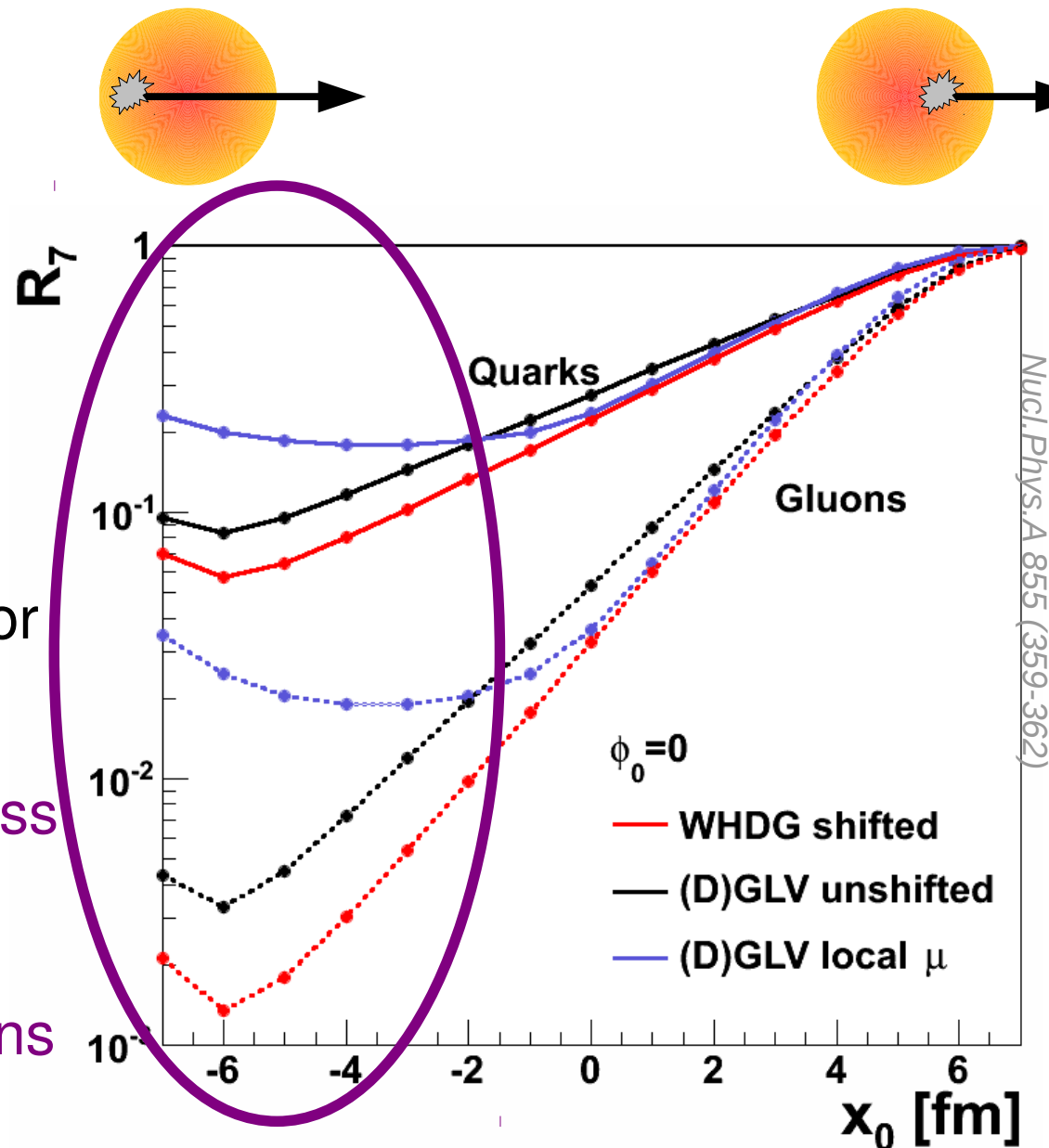
- Exercise:
  - Parton is created at  $x_0$  and travels radially through the center of the medium until it leaves the medium or freeze-out has taken place.
- Characterize energy loss of parton with suppression factor  $R_7$
- More soft gluon radiation in case of inhomogeneous distribution of scattering centers





# Medium as seen by parton

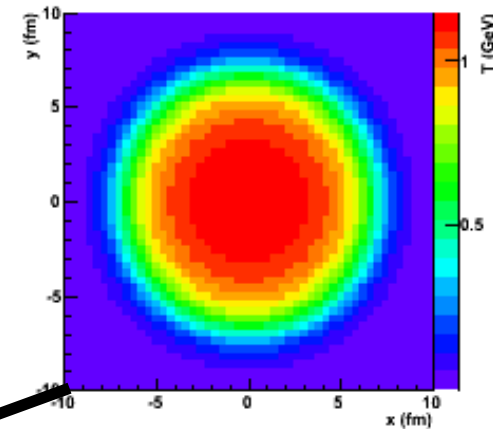
- Exercise:
  - Parton is created at  $x_0$  and travels radially through the center of the medium until it leaves the medium or freeze-out has taken place.
- Characterize energy loss of parton with suppression factor  $R_7$
- Large difference in energy loss for partons with long path lengths
  - important for  $I_{AA}$  calculations



# Geometry of HI collision

- Woods-Saxon profile
- Wounded Nucleon Scaling with optical Glauber
- Medium formation time:  $\tau_0 = 0.6$  fm
- Longitudinal Bjorken Expansion  $1/\tau$
- Freeze out temperature: 150 MeV

Temperature profile of central collision



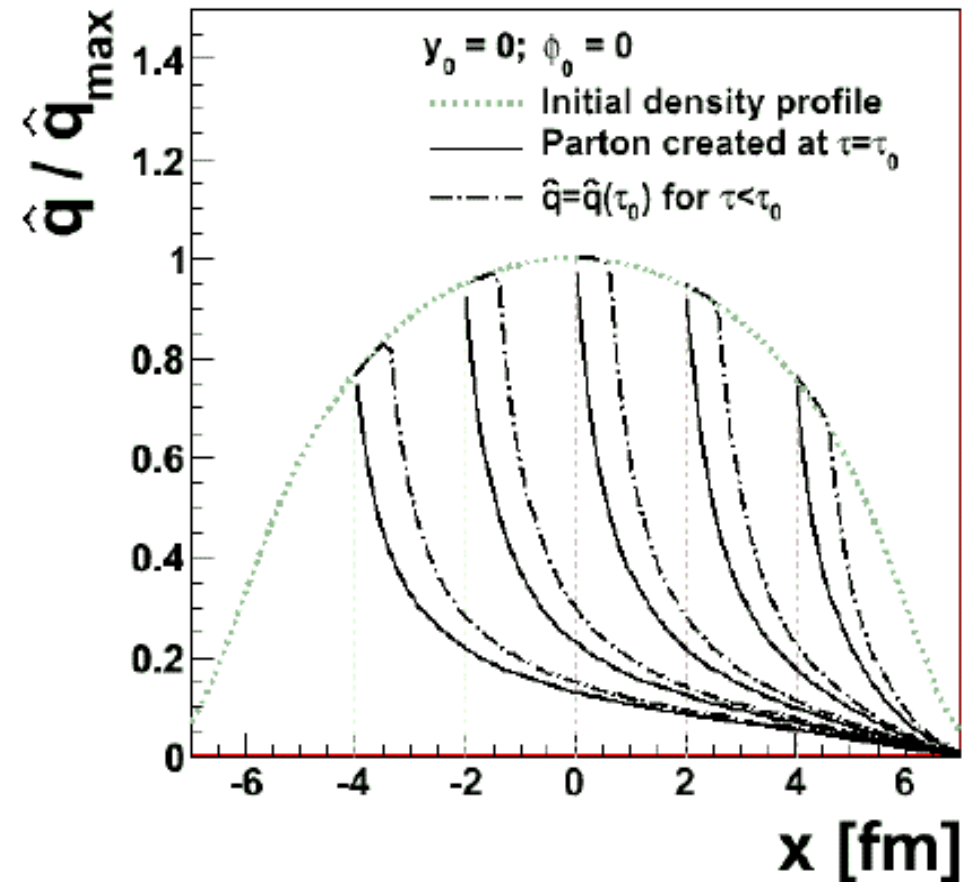
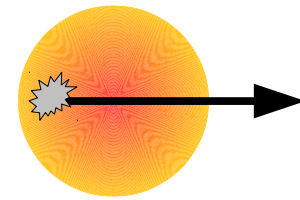
$$\frac{dN}{dp_{t,hadr}} = \frac{dN}{dp_{t,parton}} \circ P(\Delta E) \circ D(p_{t,hadr} / p_{t,parton})$$

Measurement

$\frac{dN}{dp_{t,parton}}$ Input parton spectrum Known LO pQCD	$P(\Delta E)$ Energy loss geometry medium	$D(p_{t,hadr} / p_{t,parton})$ Fragmentation Function Known from e+e-
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# Medium density profile

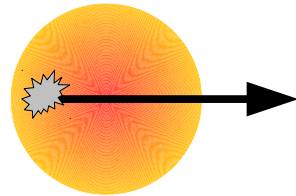
- Parton travels through evolving medium
- Parton sees different medium at each step in space and time
- Density of medium decreases as function of space and time
- In evolving medium: effective path averaged parameters which depend on  $T^n$ 
  - same treatment of geometry for different models (ASW-MS and GLV)



Local  $\hat{q}$  as function of space-time coordinate  $x$  for different starting points

# Medium as seen by parton

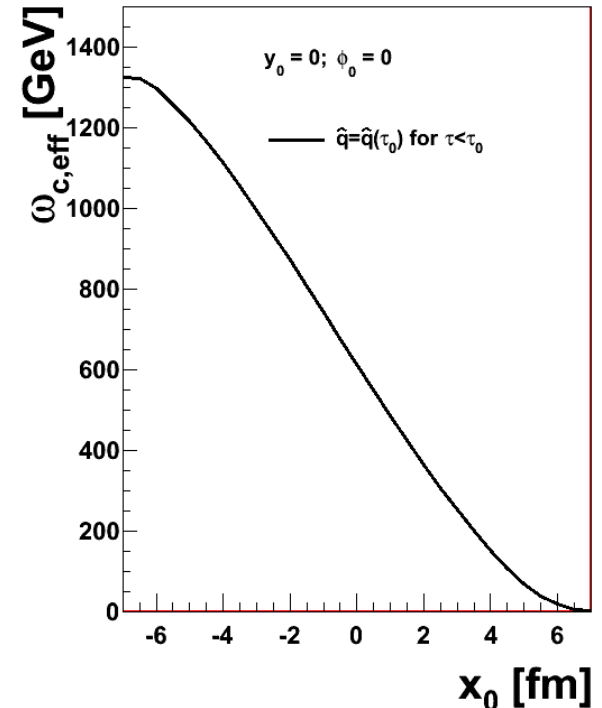
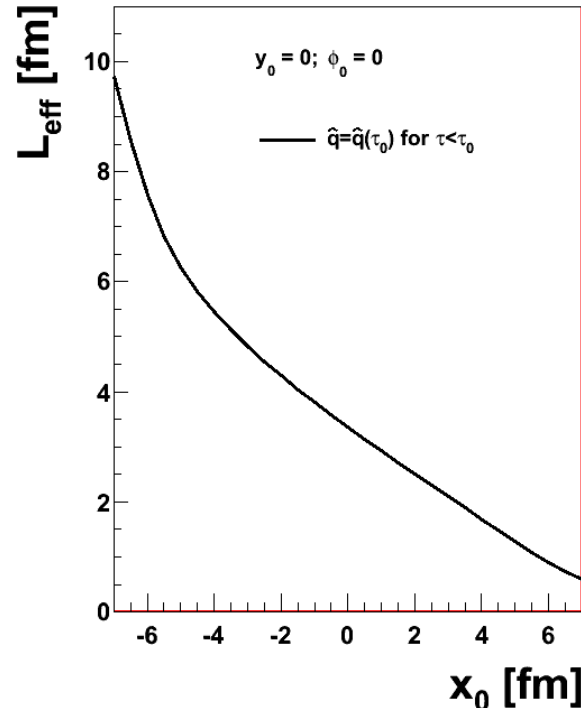
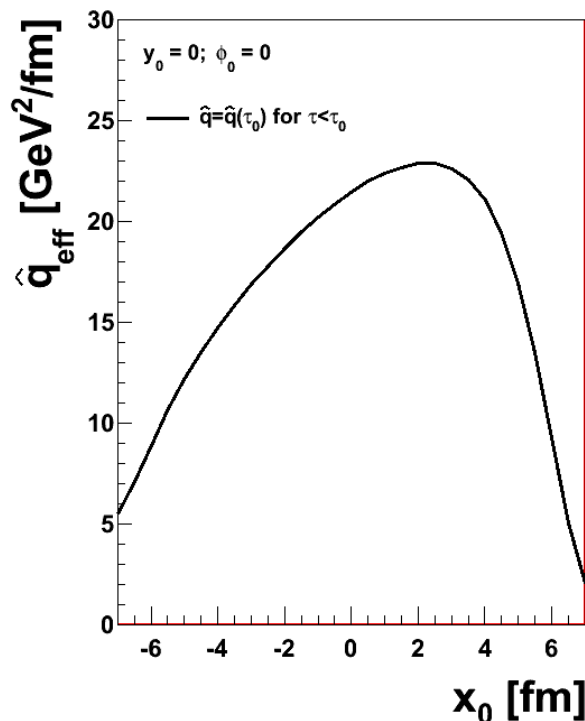
- Path average variables which characterize the energy loss.



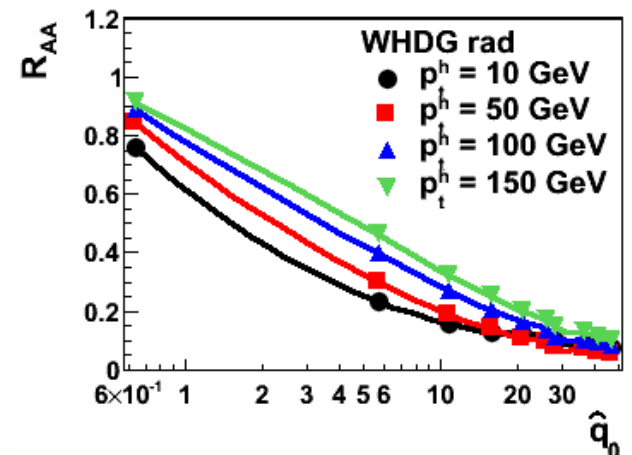
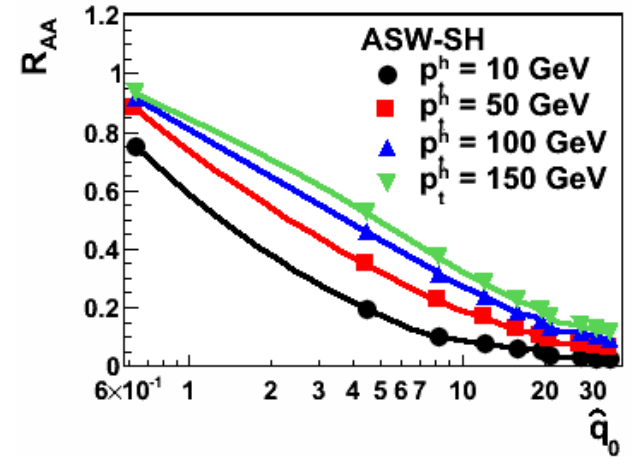
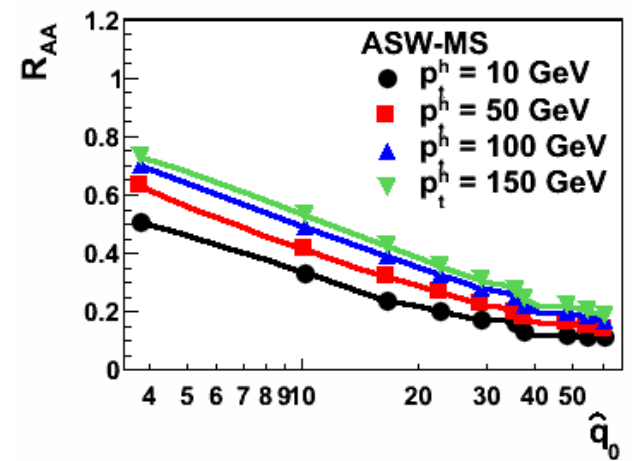
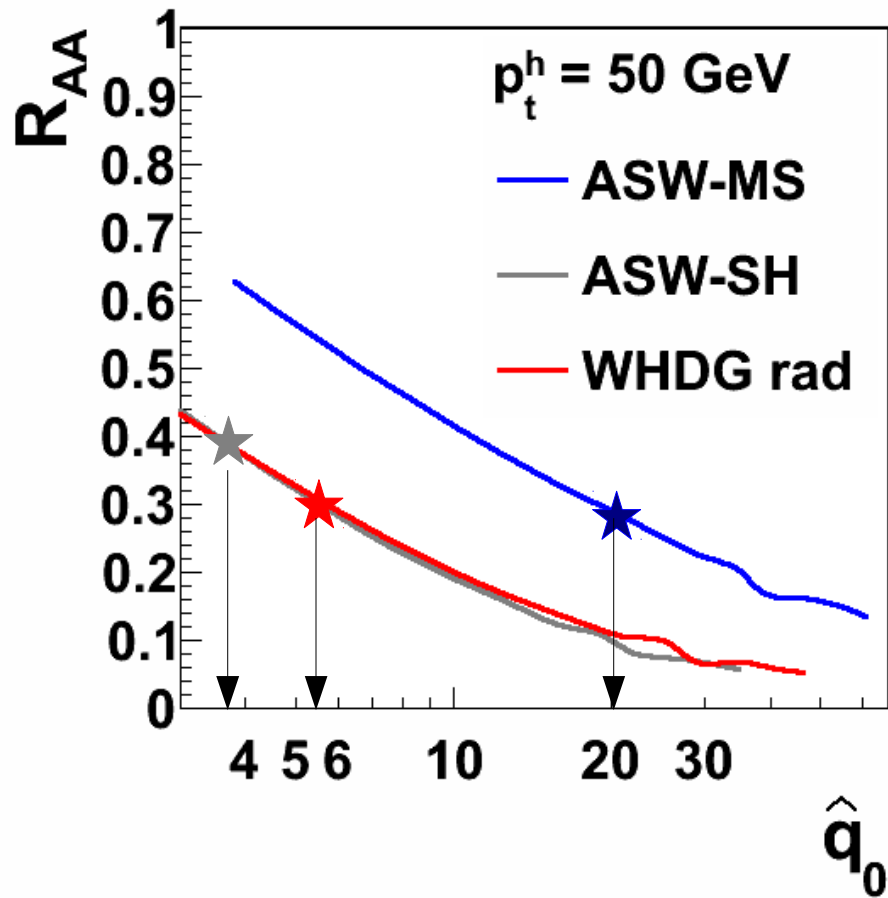
$$\langle \Delta E \rangle \propto \hat{q} L^2 \propto \omega_c$$

- Exercise:

- Parton is created at  $x_0$  and travels radially through the center of the medium until it leaves the medium or freeze out has taken place.



# LHC estimates



RHIC best fits	If $\tau < \tau_0$ $\hat{q} = \hat{q}_0$	
	$\hat{q}_0$ (GeV/fm <sup>2</sup> )	$T_0$ (MeV)
ASW-MS	$20.3^{+0.6}_{-5.1}$	$973^{+6}_{-90}$
WHDG rad	$5.7^{+0.3}_{-1.9}$	$638^{+11}_{-81}$
ASW-SH	$3.2^{+0.3}_{-0.3}$	$524^{+17}_{-18}$

# Opacity Expansion Single Gluon Spectrum

- General formula:

$$x \frac{dN_g}{dx} = \frac{C_R C_g g^2}{2\pi^3} \int \frac{d^2 \mathbf{q}}{(2\pi)^2} d^2 \mathbf{k} dz C(\mathbf{q}, z) \times \mathcal{K}(\mathbf{k}, \mathbf{q}, z)$$

in which:

$$\mathcal{K}(\mathbf{k}, \mathbf{q}, z) = \frac{\mathbf{k} \cdot \mathbf{q} (\mathbf{k} - \mathbf{q})^2 - \beta^2 \mathbf{q} \cdot (\mathbf{k} - \mathbf{q})}{[(\mathbf{k} - \mathbf{q})^2 + \beta^2]^2 (\mathbf{k}^2 + \beta^2)} \times \left[ 1 - \cos \left( \frac{(\mathbf{k} - \mathbf{q})^2 + \beta^2}{2E_x} z \right) \right]$$

$$C(\mathbf{q}) = \frac{1}{C_s} (2\pi)^2 \frac{d^2 \Gamma_{\text{el}}(\mathbf{q})}{d^2 \mathbf{q}}$$

Reference: S. Caron-Huot & C. Gale,  
*arXiv:1006.2379*

- $C(\mathbf{q})$  depends on medium properties.
- Explore effect of constant  $C(\mathbf{q})$  (uniform medium) vs position-dependent  $C(\mathbf{q})$  (non-uniform medium).

# Local $\rho$ and $\mu$

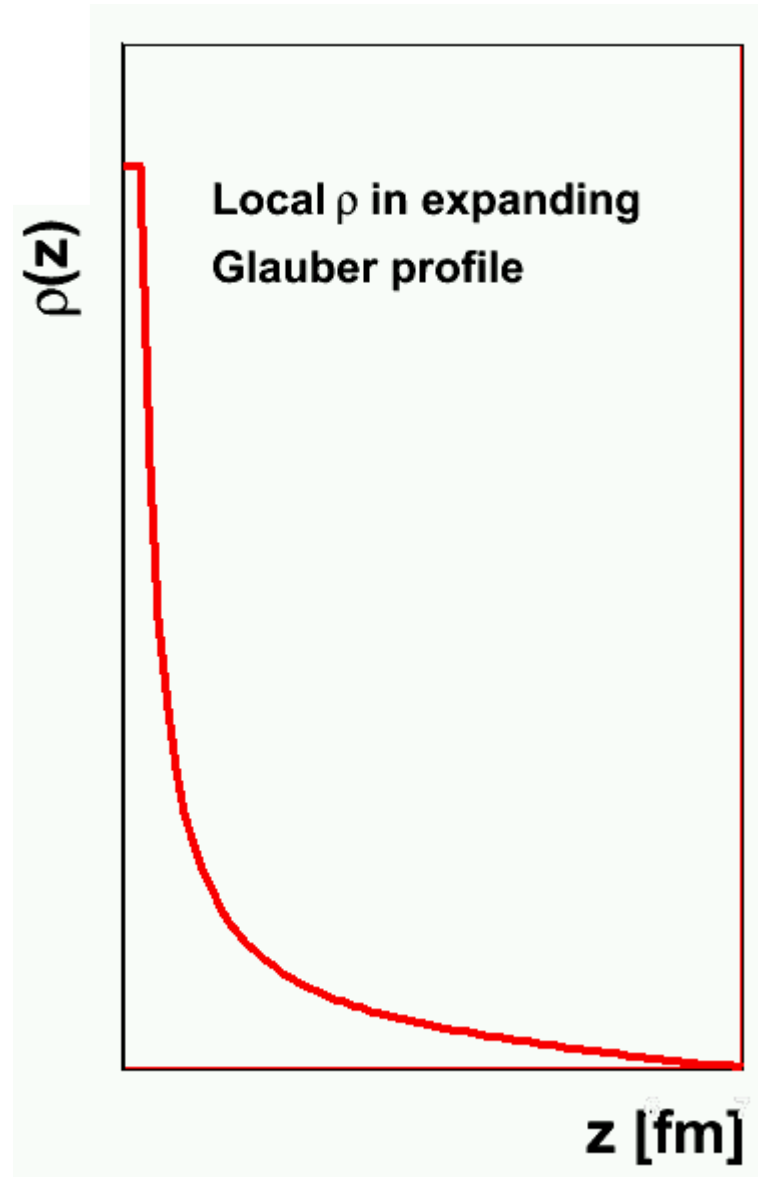
- $\rho(z)$  = medium density =  $\mathcal{N}(z) \sim T^3$
- Differential cross-section temperature dependent while the parton propagates through the medium.

$$C(\mathbf{q}, \mathbf{z}) = \frac{g^4 \mathcal{N}(\mathbf{z})}{(\mathbf{q}^2 + \mu(\mathbf{z})^2)^2}$$

$$\mathcal{N}(\mathbf{z}) = \frac{\zeta(3)}{\zeta(2)} \left(1 + \frac{1}{4} N_f\right) \mathbf{T}(\mathbf{z})^3$$

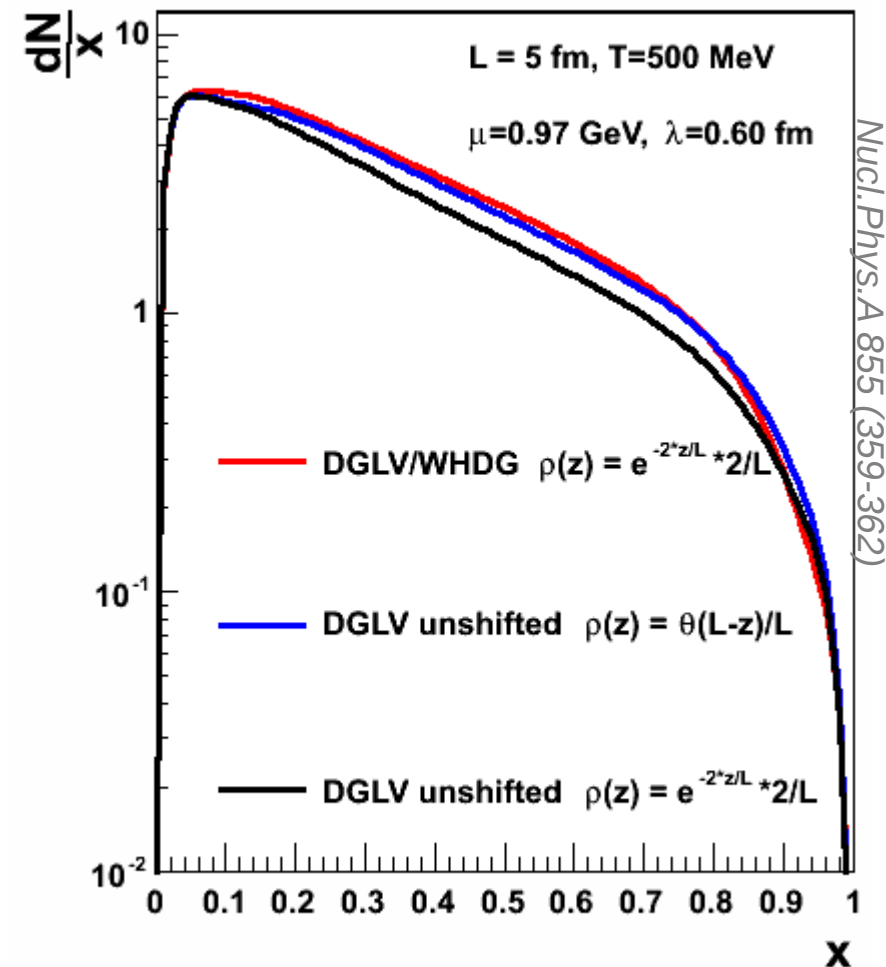
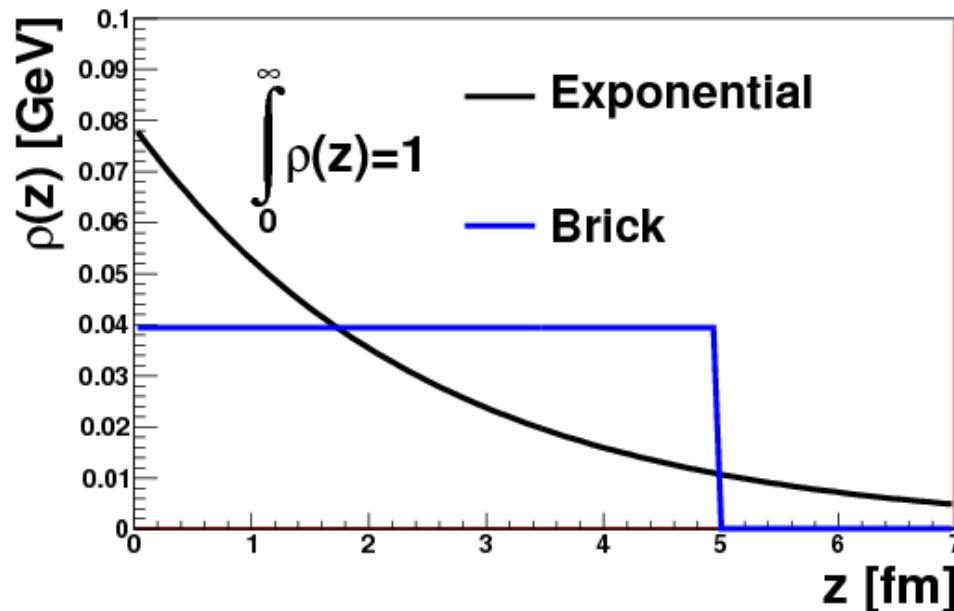
$$\mu(\mathbf{z})^2 = \left(1 + \frac{1}{6} N_f\right) g^2 \mathbf{T}(\mathbf{z})^2$$

- Medium: participant scaling + Bjorken expansion + constant medium density prior to formation time



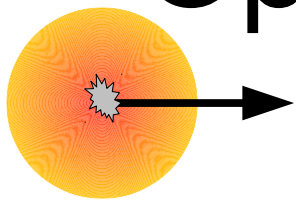
# Single gluon spectrum (D)GLV

- Normalized  $\rho(z)$  is varied and compared to the WHDG result
- In **WHDG** radiative change of variables  $\mathbf{q} \rightarrow \mathbf{q}+\mathbf{k}$  is applied
- **Similar spectrum in case of exponentially decaying and uniform (brick) distribution of scattering centers.**



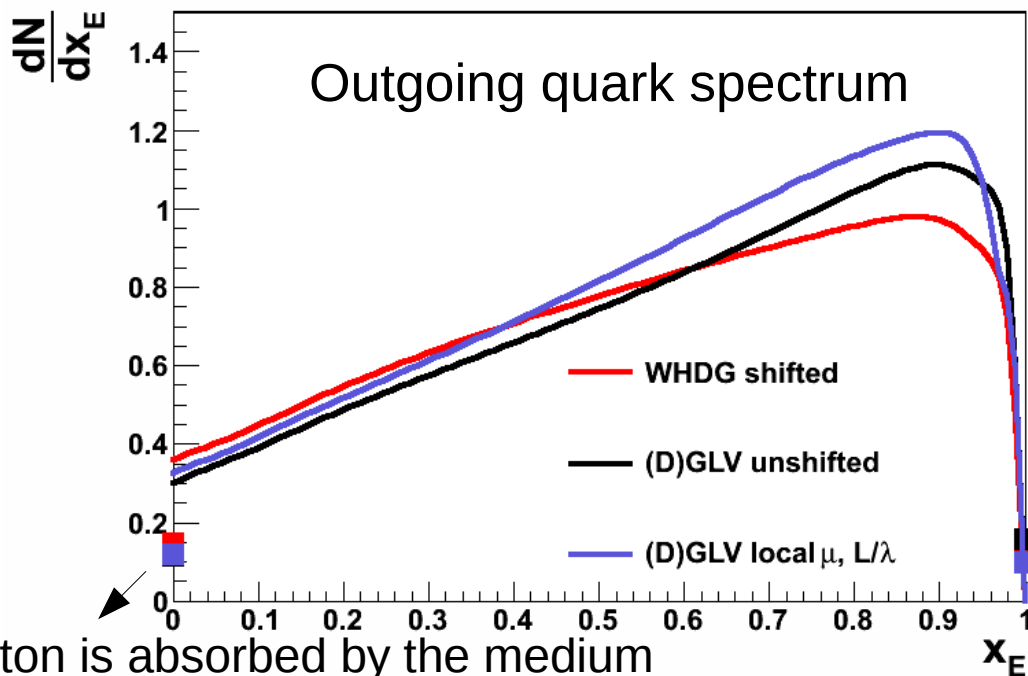
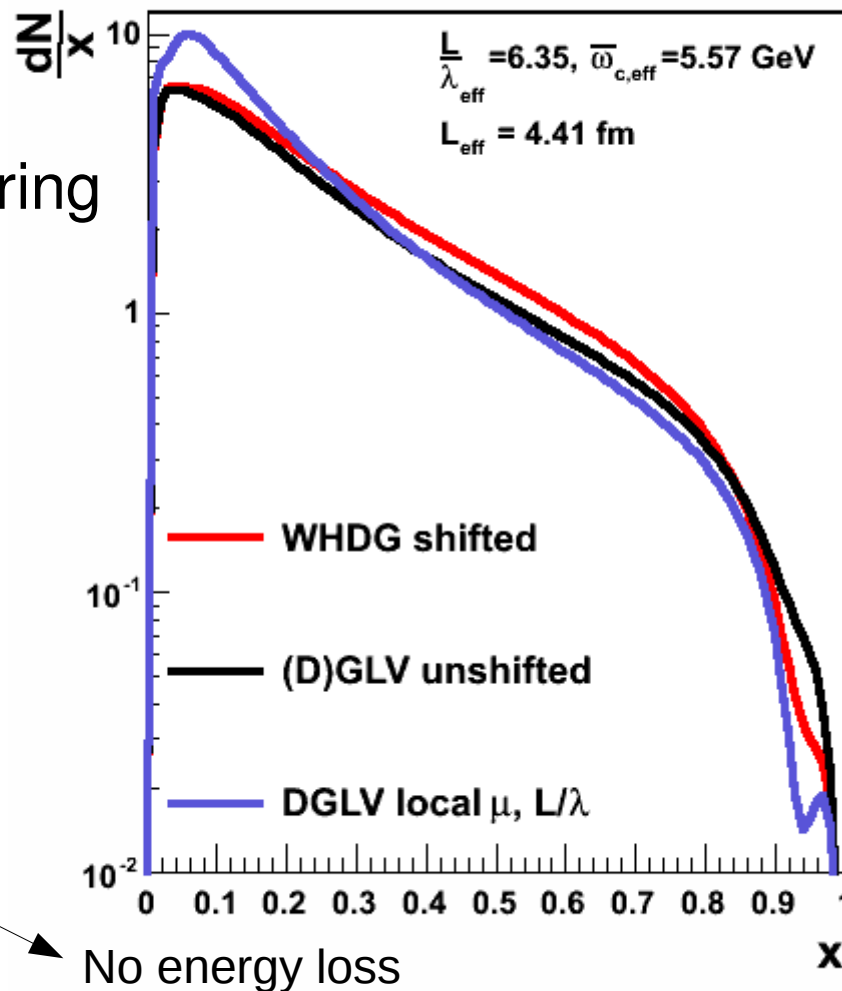


# Opacity expansion + evolving participant scaling



- Parton starts at center of medium and moves radially outwards.
- More soft gluon radiation in case of inhomogeneous distribution of scattering centers

Single gluon spectrum



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