

# Strukturen in der Plasmaturbulenz

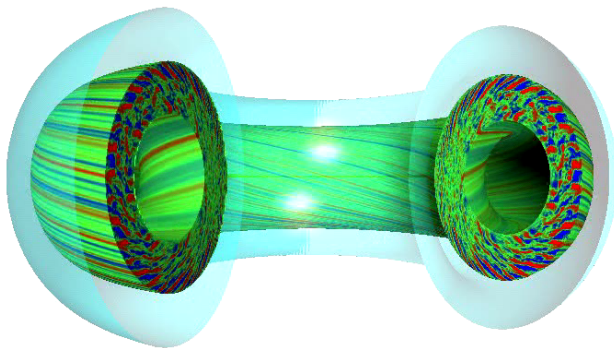
Holger Zimmermann

Institut für Theoretische Physik

27.08.2007



# Vergleich zu 3D Numerik



## Inhalt

- Gleichungen
- Tracerteilchen in zonal flows
- Turing-Instabilitäten

# Die Grundgleichungen

$$\underbrace{\left(\frac{\partial}{\partial t} + D\right)} (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \nu (\nabla_{\perp}^6) \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} - \alpha \Phi^3$$

$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \chi \nabla_{\perp}^4 p + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) - \{\Phi, p\} - \alpha p^3$$

Für endliche Werte von  $k_y$ ,  $\delta(k_y) = 1$ .

$\delta(0) = 0$ : ITG,

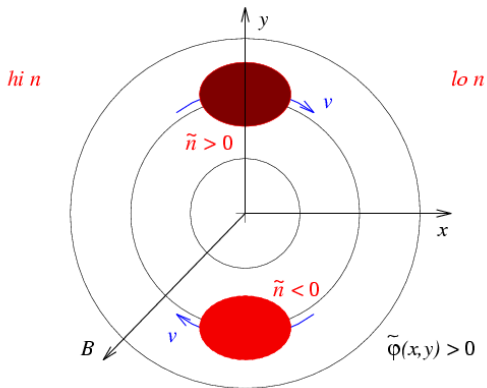
$\delta(0) = 1$ : ETG.

## ExB-Drift

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = \underbrace{-\frac{\partial \Phi}{\partial y}} + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \nu (\nabla_{\perp}^6) \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} - \alpha \Phi^3$$

$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \chi \nabla_{\perp}^4 p + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) - \{\Phi, p\} - \alpha p^3$$

## E x B Motion in a Background Gradient



--> excitation of  $\tilde{n}$  ahead of  $\tilde{\varphi}$  in  $v$ -direction

## Kopplung der Felder

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \underbrace{\epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right)} + \nu (\nabla_{\perp}^6) \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} - \alpha \Phi$$

$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \chi \nabla_{\perp}^4 p + \underbrace{\epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right)} - \{\Phi, p\} - \alpha p^3$$

# Diffusion

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \underbrace{\nu (\nabla_{\perp}^6)}_{\text{diffusion}} \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} - \alpha \Phi^3$$

$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \underbrace{\chi \nabla_{\perp}^4}_{\text{diffusion}} p + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) - \{\Phi, p\} - \alpha p^3$$



# Kopplung

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \epsilon \left(\frac{\partial \rho}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \nu (\nabla_{\perp}^6) \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} - \alpha \Phi^3$$

$$\left(\frac{\partial}{\partial t} + D\right) \rho = \underbrace{-(1 + \eta) \frac{\partial \Phi}{\partial y}} - \chi \nabla_{\perp}^4 \rho + \epsilon \left(\frac{\partial \rho}{\partial y} + \frac{\partial \Phi}{\partial y}\right) - \{\Phi, \rho\} - \alpha \rho^3$$

## Nichtlinearitäten

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \nu (\nabla_{\perp}^6) \Phi - \underbrace{\{\Phi, \nabla_{\perp}^2 \Phi\}} - \alpha \Phi^3$$

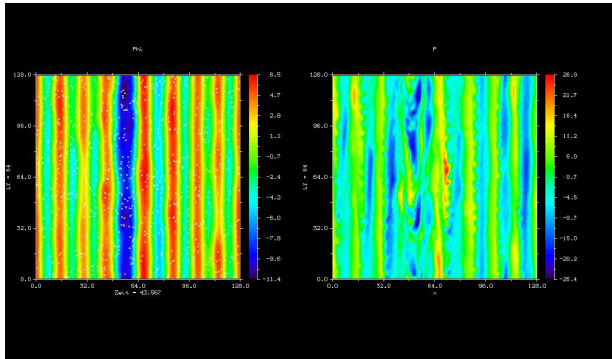
$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \chi \nabla_{\perp}^4 p + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) \underbrace{-\{\Phi, p\}} - \alpha p^3$$

## zusätzliche Dämpfung

$$\left(\frac{\partial}{\partial t} + D\right) (\delta - \nabla_{\perp}^2) \Phi = -\frac{\partial \Phi}{\partial y} + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) + \nu (\nabla_{\perp}^6) \Phi - \{\Phi, \nabla_{\perp}^2 \Phi\} \underbrace{-\alpha \Phi^3}$$

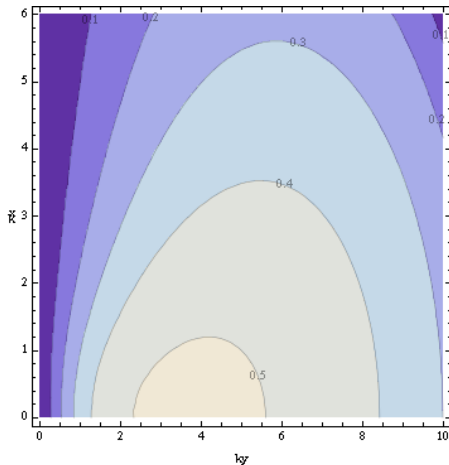
$$\left(\frac{\partial}{\partial t} + D\right) p = -(1 + \eta) \frac{\partial \Phi}{\partial y} - \chi \nabla_{\perp}^4 p + \epsilon \left(\frac{\partial p}{\partial y} + \frac{\partial \Phi}{\partial y}\right) - \{\Phi, p\} \underbrace{-\alpha p^3}$$

## ITG-Turbulenz ohne Korrekturterm, $D=0$

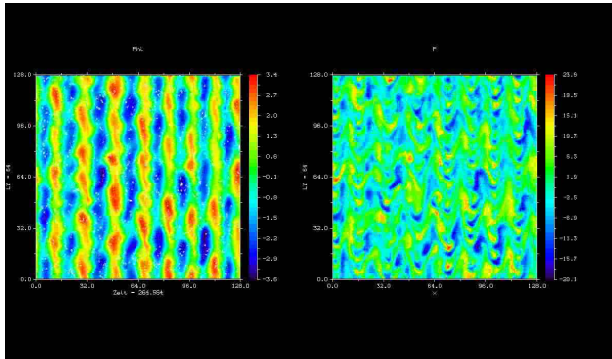


## Berechnung der linearen Wachstumsraten:

$$\phi = \phi_0 \cdot e^{-i(\omega t + k_x x + k_y y)}, \quad p = p_0 \cdot e^{-i(\omega t + k_x x + k_y y)}$$



## Gedämpfte zonal flows, $D=0,04$



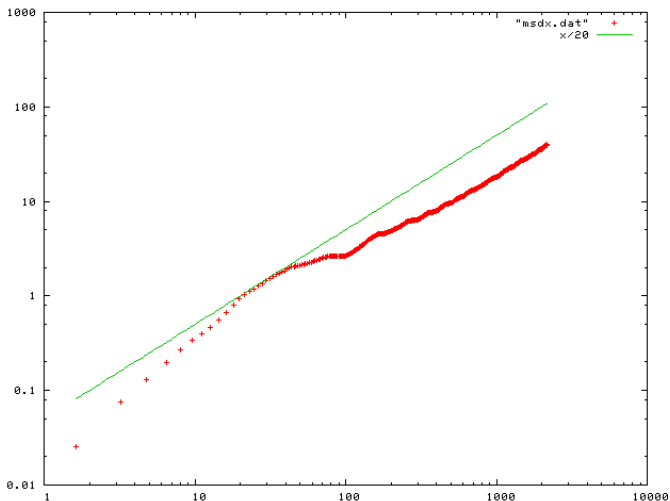
# Energiebilanz

$$\frac{\partial E}{\partial t} = \underbrace{-(1 + \eta) \int dA \frac{\partial \phi}{\partial y} p}_{=+(1+\eta)Q} - \nu \int dA (\nabla^3 \phi)^2 - \chi \int dA (\nabla_{\perp}^2 p)^2$$
$$-D \int dA p^2 = 0$$

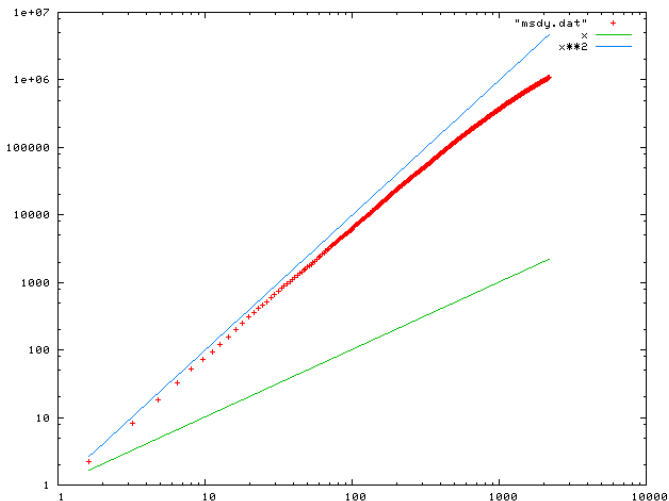
# Transport in ITG-Turbulenz



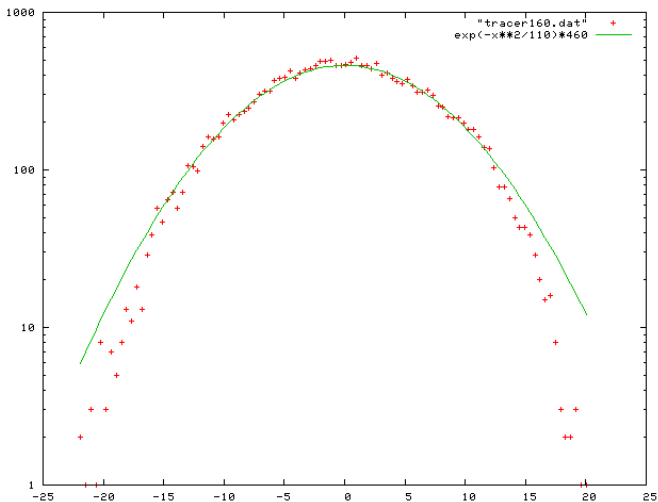
## Mean square displacement in x-Richtung für schwache zonal flows.

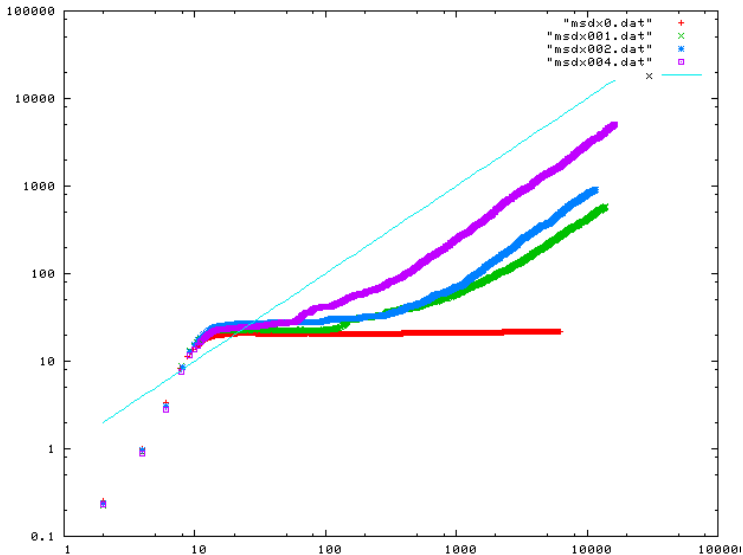


## Mean square displacement in y-Richtung für schwache zonal flows.

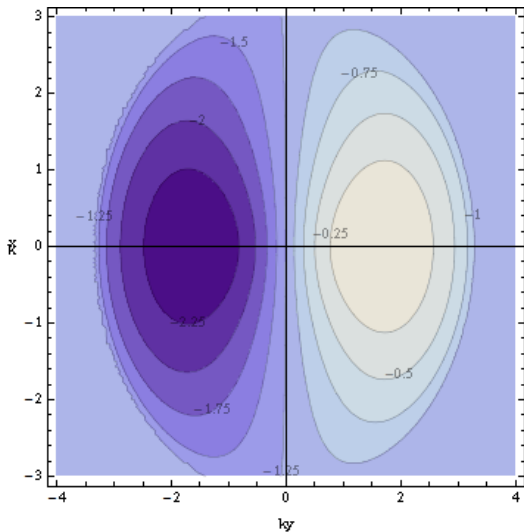


## PDF in x-Richtung



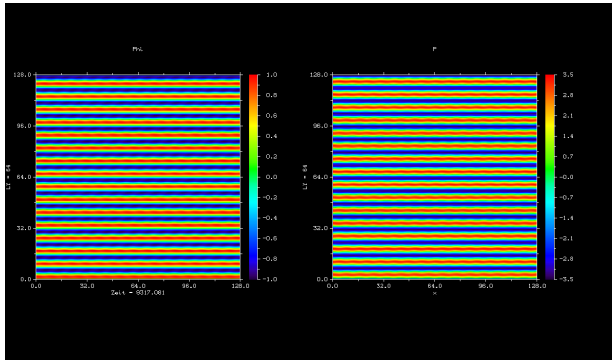


# Turingartige Instabilitäten

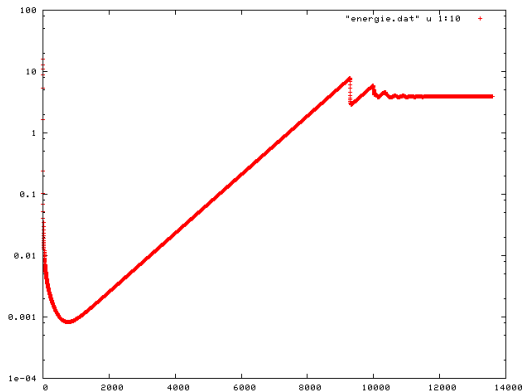


Schwelle:  $D=1,2322$

$D=1,231$

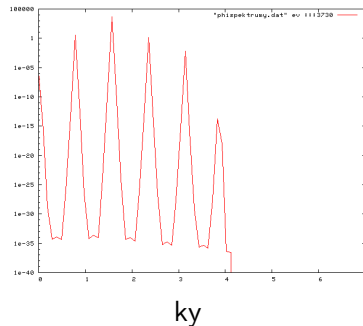
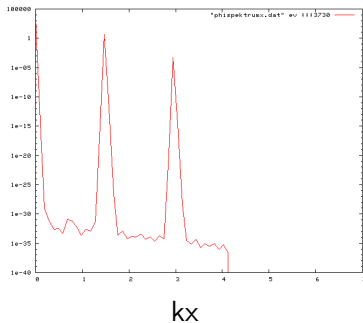


## Zeitlicher Verlauf der Gesamtenergie im System bei $D=1,2315$

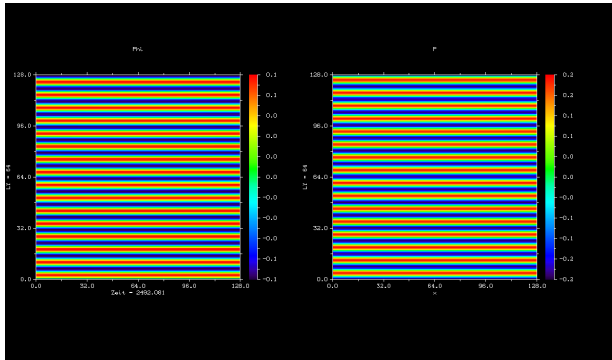




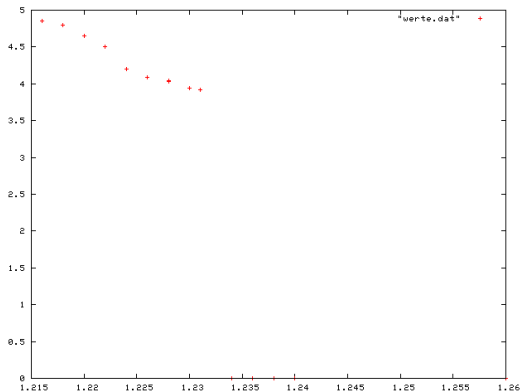
## Spektren der Turing-Instabilitäten für $D=1,231$



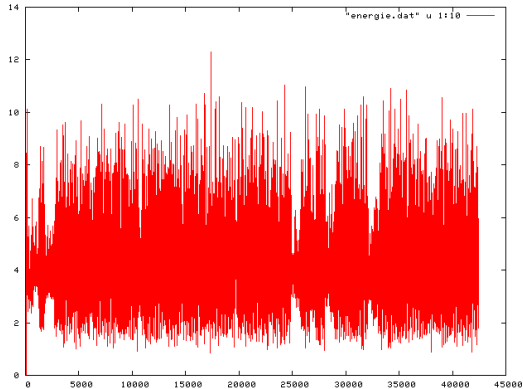
$D=1,121$



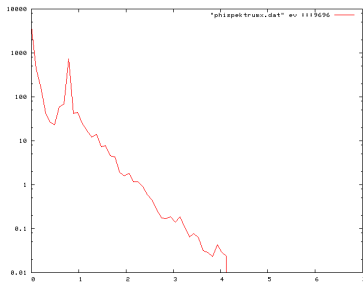
## Sättigungsniveaus für verschiedene Wachstumsraten



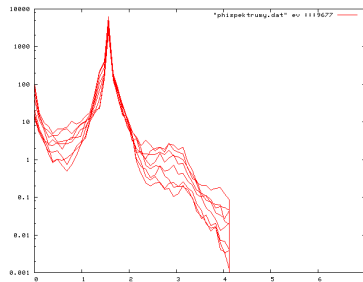
## Starke Fluktuationen für größere Wachstumsraten



## Spektren der Turing-Instabilitäten für $D=1,19$



$k_x$



$k_y$

# Zusammenfassung

- Gleichungen zeigen wesentliche Phänomene
- Transporteigenschaften werden qualitativ reproduziert
- Weitere Untersuchungen der Turing-artigen Strukturen notwendig

Vielen Dank für die Aufmerksamkeit!