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Kolloquium des Mathematischen Instituts

# Combinatorial Morse Theory: how and why

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25.11.2010, 16:30 Uhr, Hörsaal M 5

Abstract: "The idea of Morse theory is that the topology of a manifold  $M$  can be understood with the aid of a sufficiently nice smooth function  $h : M \rightarrow \mathbf{R}$ . We think of  $h$  as a height on  $M$  and consider sublevel sets  $M_r := \{x \in M \mid f(x) \leq r\}$ . As the level  $r$  increases, the sublevel sets  $M_r$  grow; and the goal is to control how the homotopy type of  $M_r$  changes during this process.

The goal of combinatorial Morse theory is to understand the homotopy types of a simplicial or CW-complex  $X$  by means of a function  $h : X \rightarrow \mathbf{R}$ . Instead of sublevel sets, one considers sublevel complexes, i.e., subcomplexes  $X_r$  spanned by all vertices up to height  $r$ . Under favorable conditions, one can again control the change how the homotopy type of  $X_r$  varies as  $r$  increases.

I shall explain and demonstrate the method, giving plenty of examples and applications. The complexes arising will be mostly Eilenberg-MacLane spaces for groups. Hence, understanding their homotopy type yields information about the homology of the underlying group."

Tee wird ab 16:00 Uhr im Sitzungszimmer SR o des Mathematischen Instituts serviert.

Fachbereich 10

Mathematik und Informatik

<http://wwwmath.uni-muenster.de>

